NUMERICAL AND EXPERIMENTAL INVESTIGATION OF THE FLOWFIELD NEAR A WRAP-AROUND FIN

DISSERTATION
Carl Patrick Tilmann
USAF/Wright Laboratory/Flight Dynamics Directorate

 ${\rm AFIT/DS/ENY/97-1}$

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DISSERTATION

Presented to the Faculty of the School of Engineering
of the Air Force Institute of Technology
Air University
in Partial Fulfillment of the
Requirements for the Degree of
Doctor of Philosophy

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USAF/Wright Laboratory/Flight Dynamics Directorate

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Carl Patrick Tilmann

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List of Symbols

a = local speed of sound

 a_k, b_k = constants for King's Law

d = diameter of cylindrical hot-film probe

c = chord length of missile fin, 2.03cm

 Cm_x = rolling moment coefficient about missile axis, $8M_x/\rho U\pi D^3$

 C_p = specific heat coefficient at constant pressure

 C_v = specific heat coefficient at constant volume

E = total internal energy

e = internal energy per unit mass

H = total enthalpy

 h_0 = stagnation enthalpy per unit volume

i = current

k =thermal conductivity

 k_0 = power law reference conductivity

 ℓ = reference length

 ℓ_f = hot-film length

M = Mach number

 M_e = Mach number at boundary layer edge

 m_i^T = turbulent mass components

n = direction normal to surface

Nu = Nusselt number

P = static pressure

 $P_{10^{\circ}}$ = 10° cone-static pressure

 $P_{20^{\circ}}$ = 20° cone-static pressure

 P_{t2} = pitot pressure

Pr = Prandtl number

 Pr_t = turbulent Prandtl number

 q_i = heat flux components

 q_{∞} = freestream dynamic pressure

 q_f = hot-film power and heat transfer

R = gas constant

 R_0 = mass flux ratio, $\overline{\rho v}/\overline{\rho u}$

 $R_{\rm ref}$ = hot-film resistance at reference temperature

 R_f = hot-film operating resistance

 R_s = anemometer resistance in series with hot-film

 R_L = hot-film lead resistance

r = model fin radius of curvature, 1.59cm

 ${\rm Re} \hspace{1cm} = \hspace{1cm} {\rm reference} \hspace{1cm} {\rm Reynolds} \hspace{1cm} {\rm number}, \hspace{1cm} \frac{\rho_{\infty} u_{\infty} \ell}{\mu_{\infty}}$

 Re_e = effective Reynolds number, $\frac{\rho U d}{\mu_0} cos \varphi$

t = time

T = temperature (K)

 T_f = hot-film temperature

 T_e = equilibrium hot-film temperature

U = magnitude of velocity vector

 \vec{U} = velocity vector

 u_{τ} = friction velocity, $\sqrt{\frac{\tau_{w}}{\rho_{w}}}$

 u^+ = inner turbulent velocity \overline{u}/u_{τ}

u, v, w = mean Cartesian velocity components

 $u_1, u_2, u_3 = u, v, w$

 E_f = hot-film voltage

x, y, z =Cartesian coordinates

Y = distance from body surface y direction

 y^+ = inner turbulent coordinate yu_{τ}/ν

 α = $T/T_t = [1 + \frac{1}{2}(\gamma - 1)M^2]^{-1}$

 $\beta = (\gamma - 1)\alpha M_{\infty}^2$

 γ = ratio of specific heats, 1.4 for air

 δ = boundary layer thickness, defined by location where M=0.95M_e

 δ_0 = reference boundary layer thickness at M=2.8 (6.1mm)

 δ_{∞} = reference boundary layer thickness at M=4.9 (10.2mm)

 \mathcal{E}_X = error associated with measurement of X

 ε_X = normalized uncertainty associated with the measurement or calculation of X

 ν = molecular kinematic viscosity, μ/ρ

 ρ = density

 τ = hot film temperature loading factor

 τ_{ij} = shear stress tensor components

 τ_{ij}^T = turbulent shear stress tensor components

 θ = horizontal flow angularity, $tan^{-1}(v/u)$

 $\phi \hspace{1.5cm} = \hspace{.5cm} \text{azimuthal flow angularity, } tan^{-1}(w/u)$

 φ = hot-film incidence angle

Subscripts

e = equilibrium

f = hot-film

L = length of hot-film probe

 L_2 = Euclidean norm

 $\max = \max$

ref = reference

t = total condition

w = wall

,i = partial derivative in x_i direction

 ∞ = free stream condition

Superscripts

 $()^T = \text{turbulent}$

()' = Reynolds fluctuating component

()" = Favré fluctuating component

 $\overline{()}$ = Reynolds averaged component

() = Favré averaged component

Abstract

A wall-mounted semi-cylindrical model fitted with a single wrap-around fin (WAF) has been investigated both numerically and experimentally, with the objective of characterizing the mean and turbulent flowfield in the vicinity of the fin. Numerical and experimental results are used to determine the nature of the flowfield and quantify the effects of fin curvature on the character of the flow near WAFs. This research has been motivated by the need to identify possible sources of a rolling moment reversal observed at high speeds in sub-scale flight tests.

Detailed mean flow and turbulence measurements were obtained in the AFIT Mach 3 wind tunnel using conventional probes and cross-wire hot-film anemometry at a series of stations upstream of and aft of the fin shock/boundary layer interaction. Hot-film anemometry results showed the turbulence intensity in the fuselage boundary layer to be far greater on the concave side of the fin than on the convex side. Similarly, the Reynolds shear stress rises dramatically on the concave side of the fin and is reduced on the convex side. These results are consistent with the stabilizing and destabilizing effects of pressure gradient distortion on supersonic boundary layers. Mean flow was also obtained in the AFIT Mach 5 wind tunnel using conventional pressure probes. Shadowgraph and schlieren photography were used for flow visualization in both wind tunnels.

Numerical results were obtained at Mach numbers of 2.8 and 4.9 ($Re/\ell=18\times10^6m^{-1}$ and $50-75\times10^6m^{-1}$) employing the algebraic eddy viscosity model of Baldwin and Lomax. Correlation with experimental data suggests that the calculations have captured the flow physics involved in this complicated flowfield. The calculations, corroborated by experimental results, indicate that a vortex exists in the fin/body juncture region on the convex side of the fin. This juncture vortex, not predicted in previous inviscid simulations, can greatly influence the pressure loading on the fin near the root. Changes in this vortex structure may contribute to the rolling moment reversal observed at high supersonic speeds in recent flight test experiments.

NUMERICAL AND EXPERIMENTAL INVESTIGATION OF THE FLOWFIELD NEAR A WRAP-AROUND FIN

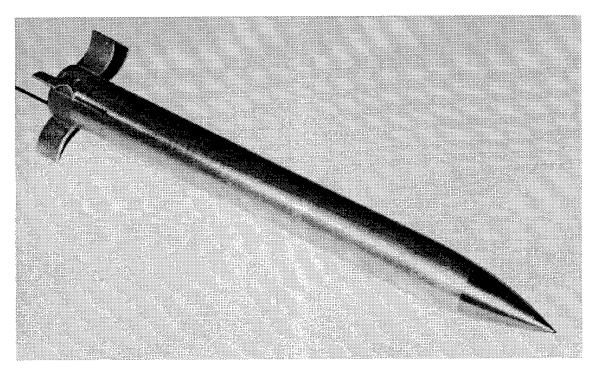
I. Introduction

1.1 Wrap-Around Fins

Wrap-around fins (WAFs) have used by designers for several years on low-speed tube launched missiles and dispenser-launched sub-munitions. The term "wrap-around fin" usually refers to a projectile stabilizing or control surface, which has the same curvature as the missile body, and can be wrapped around the projectile until deployment (see Figure 1.1). Since stealth capability has become a design parameter for many aircraft, WAFs have become even more attractive for their reduced cross-section and stowability. Wrap-around fins can also simplify the design of airframes which integrate the weapon in partial concealment, avoiding complications associated with fin-fuselage contact.

While WAFs enable several design possibilities, several stability anomalies are inherent for missiles employing them ^[1, 6, 52, 113, 119], the most recognized of which is a roll reversal observed near transonic conditions. Also due to the asymmetric fin geometry, missiles with WAFs display a pitch-yaw coupling at all speeds not present on conventional missiles. During recent ballistic range tests ^[1, 113], a possible second rolling moment reversal was observed over a small range of high supersonic speeds (M≈4.5−4.7) on a WAF configuration. In this regime, yawing moment reversals were also detected. Vitale and Abate ^[113] have proposed that this loss of static stability may be related to the complex shock structure in the fin region. Cross-flow induced by missile pitch and spinning may also be a contributing factor. Interaction with the missile bow shock is also plausible at high pitch angles.

The majority of WAF experiments have focused on ascertaining stability characteristics via sub-scale flight tests^[4, 5, 6, 52, 104, 113, 117], most of which emphasized the subsonic and transonic flight regimes^[4, 5, 6, 52, 117]. These experiments provide no detailed flowfield measurements, and do little to promote an understanding of the flowfield.



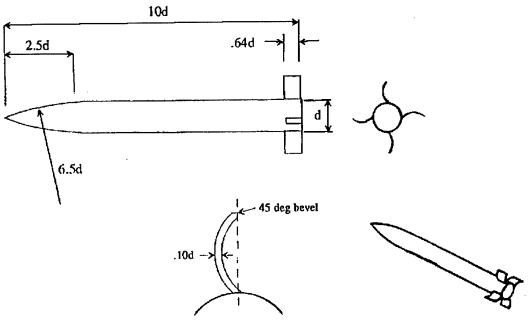


Figure 1.1 Typical WAF missile configuration (Vitale & Abate 1992).

A small number of numerical simulations have been performed on missiles employing wrap-around fins. Some have focused on the design of lift and control surfaces by simulating the fin alone^[58]. However, the majority of these simulations have focused on characterizing the structure of the fin shocks and their interaction. The Euler equations were solved by Vitale, et al.^[113] on a swept WAF configuration with no fin thickness. The Euler equations have also been solved by Abate and Cook^[3] for subsonic, transonic, and supersonic flow conditions on a WAF configuration using unswept 10% bi-convex airfoils. While such inviscid simulations have been able to predict the existence of the sonic rolling moment reversal, they have failed to predict the second rolling moment reversal at high Mach numbers. More recently, Edge^[28] has solved the laminar Navier-Stokes equations over a WAF geometry with a relatively low fin aspect ratio and a round leading edge for Mach numbers ranging from 1.3 to 3.0. To date, no WAF geometry has been simulated using turbulent models.

1.2 Objectives of Present Research

The primary goal of the present research was to characterize the flow structure near WAFs at supersonic speeds ($M\approx3,M\approx5$). This would be accomplished through a systematic numerical and experimental analysis of the mean and turbulent flowfield in the vicinity of a single WAF. An understanding of the flowfield near WAFs is critical to further development of such configurations, given the dependence of stability characteristics on Mach number. Determination of the flow structure near a single non-spinning WAF is an essential first step toward this understanding.

A second objective was to contribute a complete set of mean flow and turbulence data on this shock/boundary-layer interaction flowfield for numerical turbulence model validation. The data gathering criteria of Settles and Dodson^[96] has been used for guidance. Prior to this study, no detailed flowfield measurements (mean flow or turbulence) existed for WAF missile configurations.

Finally, the suitability of a widely used commercial simulation package, the General Aerodynamic Simulation Program (GASP)^[7], with the turbulence model of Baldwin and Lomax^[11] was to be investigated for this flowfield.

1.3 Overview of Present Research

As a first step toward understanding the flow structure near WAFs, a simple model has been investigated which consists of a single wrap-around fin mounted on a partial fuse-lage (Figure 3.1). This simplified model allowed experimental data to be obtained at much higher resolution than would have been possible on a full-body four-finned configuration scaled to fit in the available tunnel space. Also, the single-WAF static model isolates the effects of fin curvature from the effects of upstream cross-flow and interaction of the multiple fin shocks. The flow around this single-WAF configuration has been investigated both numerically and experimentally, with the objective of quantifying the flow structure in the region near the fin/body juncture. Numerical and experimental results are examined and compared to gain an understanding the flow-field in the vicinity of a WAF.

Measured flowfield data was obtained in the AFIT Mach 3 wind tunnel and in the new AFIT Mach 5 wind tunnel on a model composed of a single wrap-around fin on a ceiling-mounted semi-cylindrical fuselage. Shadowgraph and schlieren photographs were also obtained for flow visualization. In the Mach 3 wind tunnel, the flow around the test article was surveyed at several stations along its length, concentrating on the region near the fin. The flowfield was also explored with the model in wall-mounted configurations to enable measurements closer to the fin surface. Detailed mean flow measurements were obtained using conventional cone-static and pitot pressure probes, as well as hot-film cross-wire probes. The flow data measured with the hot-film probes was also used to estimate turbulence quantities using the hot-film anemometry methods outlined by Bowersox and Schetz^[13, 14, 15]. These techniques have been used recently in several experiments^[26, 74, 75, 94] to quantify the effects of pressure gradients on turbulent boundary layers. In the Mach 5 tunnel, mean flow (pressure) measurements, as well as shadowgraph and schlieren photography were obtained.

Experimental data were compared to numerical results obtained with a widely used numerical simulation package (GASP v3.06^[7]) employing the Baldwin-Lomax^[11] algebraic turbulence model. Taken in concert, the experimental and numerical information is examined with a view toward characterizing the net effect of the complex flowfield in the vicinity of the WAF. on aerodynamic loading.

1.4 Outline of Document

This section provides a road map of the chapters which follow. First, Chapter II provides a survey of research that has been directed toward the solution of other shock/boundary-layer interaction flows sharing some characteristics of the flowfield near supersonic wrap-around fins. The experimental methods used in this investigation are outlined in Chapter III. Details relating to the reduction of hot-film anemometry data is presented in Appendix B. The uncertainty of these measurements and an analysis of the effect of these uncertainties on the presented results are provided in Appendix C. Chapter III also details the facility, apparatus, instrumentation, and model used to obtain the experimental results at Mach 3. A more detailed description of the Mach 5 wind tunnel constructed for this research is included in Appendix D. The numerical strategy used is outlined in Chapter IV, and the governing equations and turbulence model which were employed are detailed in Appendix A. The results of the experimental and numerical investigations at Mach 2.8, including an analysis of the flowfield near the fin, is presented in Chapter V, while the results at Mach 4.9 are presented in Chapter VII. A set of conclusions and recommendations for further study are given in Chapter VII.

II. Background

In the mid-1960's research on shock interactions was motivated by a desire to quantify the extreme heating loads imparted on bluff bodies by single and multiple impinging shock waves. Heirs and Loubsky [39] investigated the effects of shock impingement on a cylindrical leading edge in a shock tunnel at supersonic speeds, though the experimental tools of the day limited the accuracy of their heating rate measurements. Meanwhile, Edney [29] was identifying and categorizing the flowfield structures produced by shock/shock interactions for several shock generating geometries. The need for improved high-speed bluff body aerodynamic and heating prediction methods for the *Shuttle* project led to several experimental investigations. Holden [41, 80] provides a historical review of several of these experiments involving single and multiple shock interactions as they effect aerothermal heating loads. This chapter surveys the experimental and numerical investigations on configurations which exhibit similar flowfield characteristics to those observed in the vicinity of supersonic wrap-around fins, beginning with a discussion of blunt unswept fins.

2.1 Blunt Unswept Fins

Over the past three decades, several efforts have been directed toward understanding and accurately predicting flows having shock/boundary-layer interactions. Efforts have included experimental explorations to obtain a detailed knowledge of the flowfield, as well as computational studies aimed at developing and validating numerical methods and turbulence models for such flows.

The present research has been directed toward detailing the flow structure in the vicinity of a curved fin. It was anticipated that this flow structure would be fundamentally different from the oft-studied flow around blunt unswept fins, given the significant cross-flow component of the mean flow induced by the geometric asymmetry. However, the flowfields over the two geometries share several common attributes, and an understanding of the more fundamental flows over straight-fins aids interpretation of the flow characteristics near wrap-around fins.

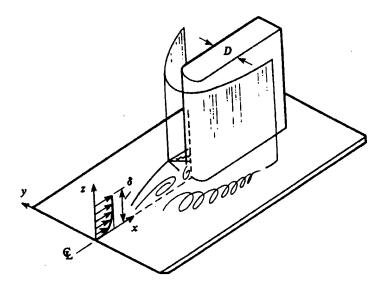


Figure 2.1 Sketch of flow interference near a blunt fin (Hung and Kordulla, 1984).

One commonly studied geometry of particular relevance to the current research is a blunt unswept fin of constant thickness and a rounded leading edge mounted on a flat plate (Figure 2.1). The bow shock produced by the blunt fin forces the incoming plate boundary layer to separate. This separation creates an oblique shock which interacts with the bow shock at a location away from the fin root (Figure 2.2). A supersonic jet forms due to the Edney^[29] Type IV interference associated with the interaction of the separation shock and the bow shock. The entire structure is referred to as the ' λ -shock' pattern. This shock pattern and the associated vortical flowfield are also produced ahead of a cylinder extending from a flat plate in supersonic flow.

2.1.1 Experimental Investigations. As early as 1967, Price and Stallings [87] investigated supersonic turbulent separated flows in the vicinity of fin-type protuberances. In the decade following, several other experimental investigations on blunt fins in supersonic flows were conducted, most notably by Kaufman, et al. [50], Sedney and Kitchens [92, 93], Dolling and Bogdonoff[24], Ozcan [82, 83], Saida and Hattori [91], Fomison [33, 34], and Settles [95].

Sedney and Kitchens^[92, 93] experimentally studied the flow near cylinders mounted on a flat plate. The cylinder height and diameter were varied, as well as Mach number (1.5 < M < 4.5) and unit Reynolds number $(2 \times 10^6 \text{m}^{-1} < \text{Re}/\ell < 19.3 \times 10^6 \text{m}^{-1})$. They found

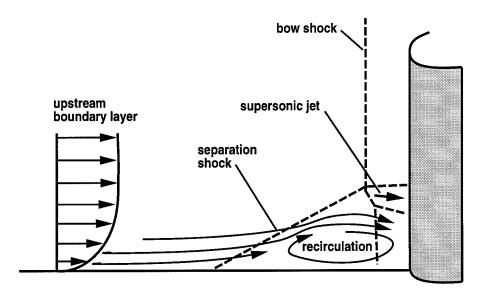


Figure 2.2 The shock structure on symmetry plane ahead of a blunt fin.

that 2, 4, or even 6 vortices could evolve around the juncture at a given Mach number, depending on the unit Reynolds number. The number of vortex pairs generally decreased with increasing Reynolds number. The details of how this structure varies with Re/ℓ is different for each Mach number. However, the unit Reynolds number (and hence number of vortices) was found to have little effect on the location of the primary separation or attachment lines in front of the obstacle.

Dolling and Bogdonoff^[24] demonstrated (using data from several experiments^[50], ^{87, 120]}) that over a large range of Mach number and incoming boundary layer thicknesses (δ/D) , the leading edge diameter (D) was a suitable scaling parameter for the centerline plate pressure ahead of the fin. The upstream influence was always found to be between two and three diameters upstream. They also showed that for a given Mach number $(M=3, Re/\ell=65\times10^6 m^{-1}\pm5\%)$, the entire flat plate surface pressure is scaled by the leading edge diameter.^[24] This corelation was later corroborated by Fomison.^[33] It was found that even the leading edge surface pressure ratios were correlated with y/D for a given Mach number, provided that the shock wave structure was well clear of the boundary layer (i.e., $\delta/D \leq 4$). In essence, Dolling and Bogdonoff showed that the spatial extent of the interaction near a straight unswept fin is dominated by inviscid characteristics of the flow.

Fomison^[33, 34], investigating blunt unswept fins with a semi-cylindrical leading edge extending from a flat plate, detailed the effect of fin thickness and incidence on the flow $(M_{\infty}=2.4, Re/\ell=2.6\times10^6 m^{-1})$. His oil flow visualizations showed that both thick and thin fins produced the same number of vortices (4 at this relatively low Re/ℓ). This was consistent with the hypothesis of Sedney and Kitchens^[92, 93] that the number of vortices was driven by the unit Reynolds number, and not obstacle size. Fomison's oil flow experiments also demonstrated that fin incidence can have a dramatic effect on the flow topology. It was conjectured that at sufficiently high incidence angles, a secondary separation would appear on the wall. This has been shown to occur for sharp swept fins at high incidence angles.^[33] Stollery^[80, 103] has reviewed several experiments which generate flows involving glancing shock/boundary layer interactions, including blunt unswept fins, and has compiled a fairly complete bibliography of the related work.

2.1.2 Numerical Investigations. The flow over a blunt unswept fin appears to have been first solved numerically by Hung, Kordulla, and Bunning^[46, 47] in the mid-1980's $(M=2.95, Re/\ell=63\times10^6 m^{-1})$. They demonstrated good agreement between their Reynolds averaged Navier-Stokes (RANS) solutions and experimental surface pressure distributions obtained by Dolling and Bogdonoff. [24] Small topology differences were probably due to limited grid resolution.

Soon after, McMaster and Shang^[73] numerically simulated this flow by solving the Favré (mass) averaged Navier-Stokes (FANS) equations with an algebraic turbulence model (M=2.95, $Re/\ell=64\times10^6 m^{-1}$). While the primary focus of this effort was to investigate the effect of fin sweep on the flowfield, solutions obtained on the un-swept fin were similar to those of Hung and Bunning^[46], with the separation line on the plate agreeing slightly better with experimental results. Kubendran, et al.^[59] obtained similar results, and designed a leading-edge fillet that eliminated the leading edge flow separation.

In the early 1990's, Knight^[54, 81] reviewed the available numerically-oriented threedimensional shock/turbulent boundary layer interaction literature. He considered five basic interactions, assessing the numerical capability of the simulation methods by comparison with available experimental data. One of these interactions was induced by a blunt unswept fin on a flat plate. At the time of his article, only algebraic turbulence modeling had been employed in any calculations reported over this geometry. Also, while the separation shock wave has been observed to be an unsteady feature^[23, 24, 25], he noted that all computational simulations of the blunt fin problem were steady.^[54] This may be due to inadequate grid resolution or inaccuracies in the turbulence models.

Since Knight's review, Chima and Yokota^[21], Chen and Hung^[20], and Rizzetta^[88] among others have numerically simulated the flow around a cylinder/flat-plate juncture using various methods. While the first two of these studies used algebraic eddy viscosity models with an ad hoc modification to the length scale to account for the multiple intersecting solid surfaces, Rizzetta^[88] employed the two equation k- ϵ turbulence model of Jones and Launder^[48], including low Reynolds number terms (M=2.5, Re/ ℓ =19.3×10⁶m⁻¹). The results agreed very well with experimental results – somewhat better than did the results of Chen and Hung^[20]. This was probably due in part to higher grid resolution and strategic grid clustering. Only one vortex pair was predicted, while three pairs were experimentally observed by Sedney and Kitchens^[92, 93]. Haidinger and Friedrich^[37] were also unable to accurately reproduce the upstream effects of the shock induced separation using Wilcox's k- ω closure model^[118]. However, the downstream predictions of pressure distribution and skin friction were reasonable. In general, recent efforts to assess the viability of numerical methods for the simulation of similar complex flows^[12, 27, 35, 49, 76] have met with varying degrees of success.

2.2 Experimental Turbulence Measurements

Settles and Dodson^[96] recently proposed a set of criteria for experimental data gathering and reporting. Adherence to these criteria is considered necessary in order for the data to be useful for CFD research on supersonic turbulent shock/boundary layer interactions. They advocate inclusion of each experiment satisfying these criteria in a database to be put forth as a standard for CFD code validation and turbulence model development. The primary focus of these criteria is to provide to the CFD community all of the necessary data required to numerically simulate the experiment. These criteria have been adopted as guidance for the current research effort.

As reported by Settles and Dodson, a great number of experiments have been targeted at measuring turbulent quantities in interacting flows. However, most of these experiments do not meet the high standards required for modern code validation. In fact, at the date of publication, they found only 19 experiments which met their criteria, none involving blunt fin-type geometries. Most experiments were rejected because they were not able to provide some kind of data which could would be useful for testing turbulence models. Others failed to report error bounds, the incoming boundary layer profile, or simply did not provide the data in a useful form. Their survey rejuvenated efforts to obtain such critical data.

Seven of the experiments accepted into this database considered the interaction between sharp fin-like geometries and flat plates. [43, 51, 55, 60, 61, 62, 63, 64, 65, 89] However, among these experiments, flowfield data are scarce, and field turbulence data are even more rare. The current study represents a continuance of the experiments accepted to date by introducing surface and shock-generator curvature effects, and thus provides experimental data that does not presently exist.

III. Experimental Methodology

This chapter outlines the tools and methods used to extract meaningful flowfield information. Instruments include pitot pressure probes, cone-static pressure probes, and hot-film cross-wire probes. The pressure probes determine mean flow information such as density, pressure, and velocity magnitude. The hot-film cross-wire probes determine velocity components and turbulence values in a form which, when manipulated, are useful for comparative analysis to results obtained numerically.

3.1 WAF Model

The WAF model (Figure 3.1) is comprised of a cylinder of the fin radius, r=1.59cm, blended to a removable test section wall, and has a maximum height of 0.5r. It is designed to represent a single fin of a typical WAF configuration, and sized to maximize data resolution while avoiding tunnel blockage. The fin has the same proportions as free-flight models which have been tested at the Wright Laboratory Armament Directorate^[1, 113], with a thickness of 0.2r (3.18mm), a span of $\sqrt{2}r$ (22.5mm), and a chord length, c, of 1.28r (20.3mm). The leading edge and tip of the fin are beveled at 45°. The cylinder is 5.12 fin radii in length with the single fin placed at the downstream base. Upstream, the cylinder is blended to the tunnel floor with a polynomial was chosen to ensure second order continuity in the streamwise direction. The blending region is 5r long and starts 21.48r from the throat of the wind tunnel nozzle.

3.2 Mach 3 Wind Tunnel

The AFIT Mach 3 wind tunnel (Figure 3.2) is an intermittent blow-down tunnel with downstream evacuation. The maximum run time for the tunnel was 30 seconds with an evacuation time of 6 to 10 minutes. The nozzle measures 27.3cm from throat to test section entrance. The test section is 33.0cm long with a square 6.35cm cross-section. The settling chamber total pressure and temperature are 2.0-2.14atm and 294K respectively, yielding a freestream Reynolds number of $Re/\ell=17-18\times10^6 m^{-1}$. Figure 3.3 is a photo of the nozzle and removable test sections with the side-walls removed for visibility.

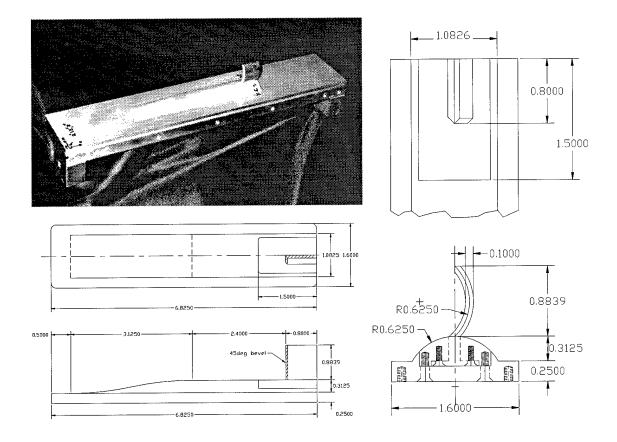


Figure 3.1 Single wrap-around fin model (dimensions in inches).

3.2.1 Operating Conditions. Detailed pitot and cone-static measurements had been previously obtained in an empty test section and used to determine the mean inflow conditions for the test section.^[75] From this survey, the freestream Mach number was determined to be 2.9 (U_e =607m/s). Results from this earlier experiment were used to specify the upstream boundary conditions for the preliminary inviscid numerical simulation.^[110]

During the present research (with the model in the tunnel), the test section entrance conditions were again surveyed. It was determined that at a location just downstream of the test section entrance (8.4c ahead of the fin leading edge) the freestream Mach number was 2.80 (U_e =601m/s), with a measurement uncertainty of 2.8%. The boundary layer on the tunnel ceiling at a location 1.27cm upstream of the model has a measured thickness of 5.3mm at the centerline, defined by the distance from the surface where M=0.95% M_e . A summary of measured freestream mean-flow conditions are presented in Table 3.1.

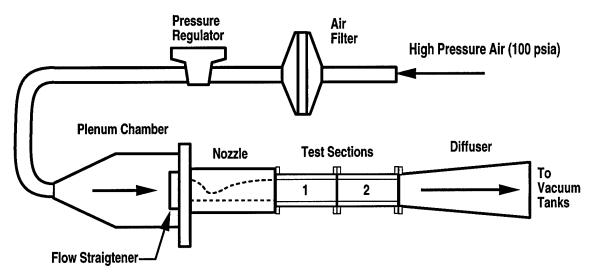


Figure 3.2 Mach 3 wind tunnel schematic.

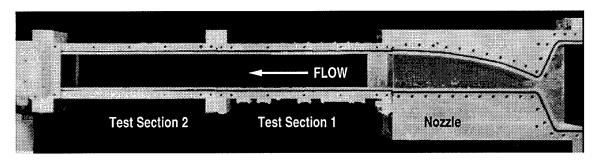


Figure 3.3 AFIT Mach 3 wind tunnel.

- 3.2.2 Tunnel Instrumentation. Instrumentation for the Mach 3 tunnel included an internal pitot tube and thermocouple in the plenum chamber to measure $P_{t\infty}$ and $T_{t\infty}$. The thermocouple (K-type, Omega part no. SEFE-K-5) had an accuracy of $\pm 1 \mathrm{K}^{[32]}$, and the pitot (total) pressure was fitted with a a 6.7atm pressure transducer (Endevco model 8510C-100).
- 3.2.3 Traversing Equipment. The probe traverse system used in the Mach 3 tunnel used a stepper motor with 400 steps per revolution. The slide moves on a shaft of 40 threads per 2.54cm, has a total travel distance of 16.51cm, and a moves at a maximum speed of about 0.254 cm/sec.^[74] A photograph of the traversing assembly is provided in Figure 3.4 (courtesy of Miller^[74]). Traverse control is accomplished via personal computer.

Table 3.1 Mach 3 tunnel freestream inflow conditions.

Condition	Value
M	2.80
P_t	217kPa = 2.14atm
P	7.99kPa = 0.0789 atm
T_t	297K
T	114.5K
u	, $601\frac{\text{m}}{\text{s}}$
ρ	$0.2431 rac{ m kg}{ m m^3}$

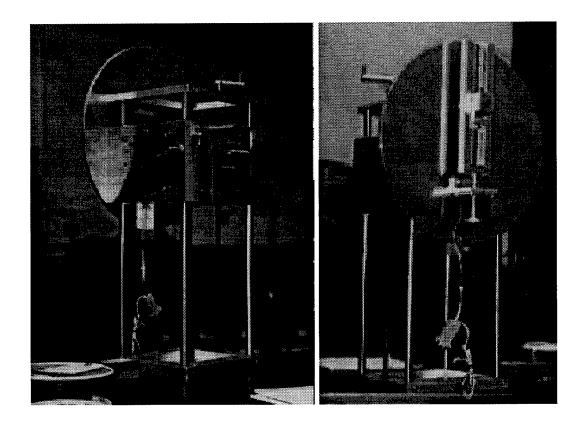


Figure 3.4 Traverse assembly (Miller).

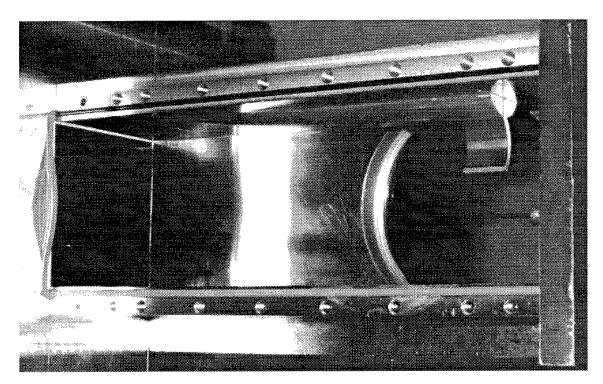


Figure 3.5 AFIT Mach 5 wind tunnel with WAF model.

3.3 Mach 5 Wind Tunnel

Experimental results were also obtained in the new AFIT Mach 5 wind tunnel (Figure D.1). This blow-down wind tunnel has a heated air supply and has been operated over a range of unit Reynolds numbers ($\text{Re}/\ell \approx 32-75\times 10^6\text{m}^{-1}$). Although the tunnel is capable of producing much longer run-times, the current experiments only required total run-times of 10–15 seconds. The design, construction, instrumentation, and initial calibration of this facility comprises a significant portion of this research effort. More detailed information on the AFIT Mach 5 wind tunnel is available in Appendix D.

3.4 Pressure Probes

A pitot probe and a 10° ($\pm .03^{\circ}$) cone-static probe were used to measure pressures throughout the flowfield in the Mach 3 wind tunnel (Figure 3.6). Total and static pressure data is obtained directly from the pitot and cone-static probes through normal and axisymmetric oblique shock relations. This data can be used to calculate mean flow information such as Mach number, density, and the magnitude of the velocity. Through

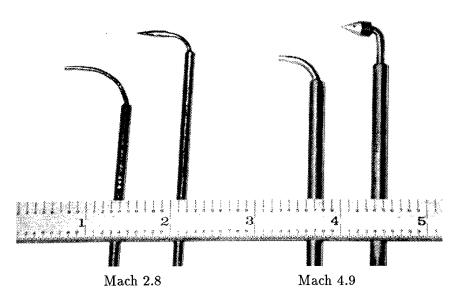


Figure 3.6 Pressure probes.

the manipulation of results from conical^[9, 56] and normal shock relations^[10], the following curve fit was proposed by Bowersox.^[14]

$$\frac{1}{M} = -0.052976 + 4.6840\xi_{10^{\circ}} - 18.6786\xi_{10^{\circ}}^{2} + 50.7006\xi_{10^{\circ}}^{3} - 54.1577\xi_{10^{\circ}}^{4}$$
 (3.1)

where $\xi_{10^{\circ}}$ is defined as the ratio of the pressure measured with the 10° cone-static probe to the pitot pressure ($\xi_{10^{\circ}}=P_c/P_{t2}=fcn[\mathrm{M}]$). It has been found that for flow angles less than 6.0° the errors in Mach number are less than 0.03.^[115] Also note Equation 3.1 is valid for Mach numbers in the range from 1.5 to 4.4 and has a standard deviation of 0.06%.^[14]

Stronger pitot and cone-static probes than those used in the Mach 3 tunnel were fabricated from heavy gauge stainless steel to withstand the higher loads associated with the Mach 5 tunnel. This cone-static probe had a semi-vertex angle of 20°, which produces higher measured pressure levels than the 10° probe, enabling more accurate readings. The higher cone angle also minimized the error due to flow angularity. For this new cone angle, and to envelope the higher Mach number range, a new relationship between Mach number and the measured pressures was needed. Again, conical and normal shock solutions were used to develop a direct relationship between Mach number and the ratio of measured

pressures.

$$\frac{1}{M} = 0.3469176 + 0.908347\xi_{20^{\circ}} - 0.0518062/\xi_{20^{\circ}}$$
 (3.2)

This relationship is valid for Mach numbers between 1.5 and 6.5 with a correlation coefficient of 99.990%. Note that this form provides monotonic behavior at high pressure ratios (low Mach numbers), and is nearly as accurate within the range of validity as a fourth-order polynomial.

With the exception of the Mach 5 pitot pressure, all probes were connected with tubing to a 1atm transducer (Endevco model 8510C-15), which sent its signal to a signal processor (Endevco model 4428A). This unit uses the maximum range of the pressure transducer, is self-zeroing, and connects directly to the data acquisition system (Section 3.6). The Mach 5 pitot pressure was sensed with a 6.7atm transducer (Endevco model 8510C-100). Atmospheric pressure was recorded using a Druck resonant sensor barometer.

3.5 Hot-Film Cross-Wire Probes

Here is presented a brief overview of the hot-film cross-wire probes and the associated data reduction techniques. More details on the hot-film anemometry methods employed to determine both mean and turbulent flow information are provided in Appendix B.

Two hot-film probes (Figure 3.7) were used to determine the velocity and fluctuations of the flow in the Mach 3 tunnel. Both probes were two-component cross-wire hot-film probes, each with two thin films of platinum 1mm long and 51μ m in diameter. One probe had the films oriented in the vertical plane, angled at $\pm 45^{\circ}$ to the horizon (u-v plane). The other probe's films were oriented in the horizontal plane and similarly angled (u-w plane). The transverse separation between the two films was 1mm. During most runs, these probes were traversed about 5cm. Since the traverse was moving slowly relative to the flow, pressure and hot-film measurements were taken while the traverse was in motion. This technique has been validated previously in several experiments in the Mach 3 tunnel. [26, 69, 74, 75, 94] The hot-film probes were connected to a TSI brand Intelligent Flow Analyzer [111]. A Tektronix 2454B oscilloscope was used to view and tune the frequency response shape and response time for each film on the probe.

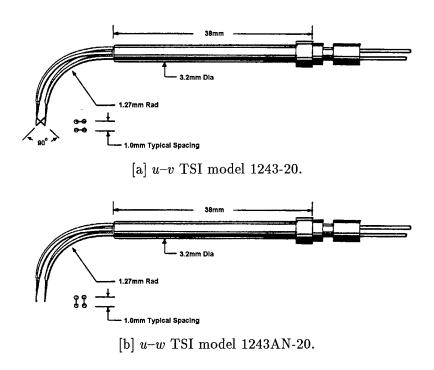


Figure 3.7 Hot film probes.

Cross-film measurements provide a means to resolve the mean mass flux vector into its Cartesian components. When the Mach number normal to the film is greater than 1.2, the Prandtl number may be assumed constant^[57, 98]. When the aspect ratio of the hot-film is also much larger than unity, then the functional form of the Nusselt number may be further simplified. It has been determined experimentally that *King's Law*, the functional relationship between Nusselt number and effective Reynolds number for incompressible flow, is also an acceptable relationship for compressible flow. [13, 14, 15]

$$Nu = a_k \sqrt{Re_e} + b_k \tag{3.3}$$

The unknowns in Equation 3.3 are the calibration coefficients, a_k and b_k , and Re_e which is the effective cooling Reynolds number normal to the film based on film diameter and reference viscosity. The hot-film calibration is performed by placing the probe in the tunnel free stream, varying the plenum pressure (thus changing Re_e), and measuring the hot-film voltage, providing Nu. The calibration constants a_k and b_k are then determined using a

least squares linear regression on the data. Hence, the calibrated hot-film provides values of local Reynolds number, essentially allowing direct measurement of the mass-flux, $\rho \vec{U}$.

A complication faced by modelers is that the apparent mass terms appearing in the compressible turbulence terms of the RANS equations (Appendix A) cannot be directly measured with conventional methods. One of the key features of cross-wire anemometry is how the Reynolds turbulent shear stress can be directly measured as the negative of the mass-flux correlation term combined with the density fluctuation. Bowersox and Schetz^[15] have shown that these apparent mass terms may be approximated by first noting that

$$\rho\phi = \overline{\rho\phi} + (\rho\phi)' \tag{3.4}$$

and also

$$\rho\phi = (\overline{\rho} + \rho')(\overline{\phi} + \phi') = \overline{\rho}\overline{\phi} + \overline{\rho}\phi' + \rho'\overline{\phi} + \rho'\phi'$$
(3.5)

Then, using (3.4) and (3.5) in the Navier-Stokes equations (A.8) and neglecting third order terms allows us to rewrite the Reynolds shear stress (Equation A.11) as

$$\tau_{ij}^{T} = -\frac{\overline{(\rho u_i)'(\rho u_i)'}}{\overline{\rho}} + \overline{\rho} \, \overline{u_i} \, \overline{u_j} \, \overline{\left(\frac{\rho'}{\overline{\rho}}\right)^2}$$
 (3.6)

where the second term has been shown to be much less than the first term for thin layer flows. In the present experiments, the second term was always at least least an order of magnitude smaller than the first term. The first term may be directly measured with cross-film probes.

Multiple overheat ratios are generally required to determine all of the flow information. However, sensitivity to total temperature fluctuation is often negligible for hot-films operating at high overheat ratios ($\frac{R_w}{R_{\rm ref}} \geq 2.0$). In cases where the fluctuation in total temperature is negligible, only a single overheat ratio is necessary to determine flow field information. Since the AFIT Mach 3 wind tunnel has been found to maintain total temperature fluctuation below about 2.0%. [44, 45, 70, 75], a single-overheat data reduction method was used. The single-overheat hot-film analysis and its use in the present research is detailed in Appendix B.

3.6 Data Acquisition

The AFIT Mach 3 tunnel is instrumented with a Multiprol⁷⁹ data acquisition system. The Multipro has four Model 120 data acquisition boards installed with one megabyte of memory per board. The selection of the sampling frequency was based in part on the criteria of Smits and Muck⁹⁷. This sampling frequency was selected such that the character of the flow was captured (as indicated by the sampling energy spectra). Experiments were conducted to insure that data was recorded at a sufficiently high frequency. Data acquisition parameters are summarized in Table 3.2.

Table 3.2 Data acquisition system parameters.

Acquisition Parameter	M=2.8 Experiment	M=4.9 Experiment
Pressure Probe Sampling Frequency	200Hz	500Hz
Traverse Speed	.077in/sec	.20in/sec
Hot-film Response Time	$8-12~\mu\mathrm{s}$	
Hot-film Sampling Frequency	$16.\overline{6}\mathrm{kHz}$	

3.7 Shadowgraph and Schlieren Optics

The shadowgraph and schlieren images were obtained on Polaroid film using a Xenon^[121] arc light source with a spark duration of 10 nanoseconds. For the shadowgraphs, the light is reflected from a 101.6 cm focal length mirror and photographed with series 52 Polaroid film. The schlieren imaging requires an additional mirror and knife edge to polarize the incoming light to the film. The diagrams for the shadowgraph and schlieren layout are provided in Figures 3.8 and 3.9.

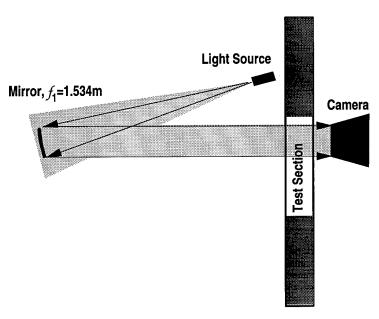


Figure 3.8 Shadowgraph camera and mirror setup.

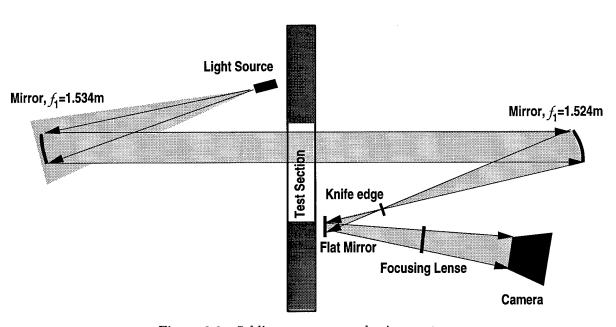


Figure 3.9 Schlieren camera and mirror setup.

IV. Numerical Methodology

In this chapter, the numerical methods which have been applied in the present research are presented, along with the associated boundary conditions. Solutions to the governing equations (Appendix A) were obtained using the General Aerodynamic Simulation Program (GASP). [7, 72] GASP, a fully conservative shock capturing code, has been widely used by the CFD community for the analysis of supersonic and hypersonic flows. [36, 71, 90, 114] GASP Version 2.0 was used for the inviscid calculations, and GASP Version 3.06 was used for the viscous calculations. A sample GASP 3.0 input deck for the viscous simulation at Mach 2.8 in included in Appendix E.

4.1 Inviscid Calculations (M=2.9,5.0)

As a means of establishing the most suitable locations for experimental measurements, pilot numerical simulations were conducted by solving the Euler equations upstream and in the vicinity of the WAF.^[110] These simulations were conducted on grids representing the WAF model as installed in the Mach 3 and Mach 5 tunnel test sections, and will be discussed further here.

4.1.1 Grid Definition. To resolve the features of the shock structure in the vicinity of the fin, the grid was clustered near the fin and cylinder surfaces. For both Mach numbers, the entire computational mesh consists of 11 computational zones connected via 19 zonal boundaries. Flow variable values are passed through the zonal boundaries via a five-point overlap. The entire test section (all four walls) were included in the Mach 2.9 simulation. Since at Mach 5.0 the shock emanating from the body was expected to remain very close to the fin, only two-thirds of the test section was modeled. This simplification provided substantial savings in computational time and memory requirements.

The faces of each zone in the region near the fin were defined with an elliptic grid generator employing Thomas and Middlecoff^[106] control functions. Grid orthogonality was enforced along the edges of each zone, while constraining the grid points to lie on the geometry surface.^[101, 100] The interior points of each zone were then positioned using a standard trans-finite interpolation (TFI) scheme.^[85] Figure 4.1 shows the numerical

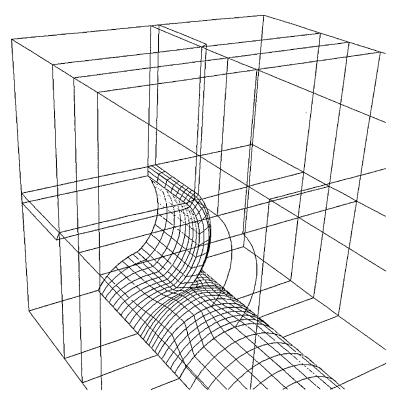


Figure 4.1 Grid boundaries and zonal structure for inviscid Mach 2.9 simulation.

representation of the Mach 3 tunnel test section near the fin. The Mach 5.0 simulation was performed on a grid created by the same methods and defined by the same model geometry. However, the tunnel side walls were moved to represent the wider test section.

4.1.2 Solution Strategy. Since the flow disturbances do not propagate upstream in a fully supersonic flow, the solution was space-marched from an upstream starting plane 0.8r ahead of the blended body to a location approximately 0.4c ahead of the fin (see Figure 5.1). The location at which the space marching was concluded was chosen to be well ahead of the expected bow shock location. Pilot 2-D simulations over a beveled fin provided early estimates of the position of the shock induced by the fin. These simulations also provided an expedient means to ensure that the grid density and clustering near the fin to be used in the 3-D simulation would be sufficient to capture the key feature of the detached fin shock.

Table 4.1 Freestream conditions used for Euler calculations.

Condition	Value	Value
M	2.9	5.0
P_t	2.0atm	20.4atm
P	0.0633atm	0.03858atm
T_t	294K	375K
T	109.6K	62.5K
U	$607\frac{m}{s}$	$792\frac{m}{s}$
ρ	$0.2039 \frac{\text{kg}}{\text{m}^3}$	$0.2179 \frac{\mathrm{kg}}{\mathrm{m}^3}$

The upstream boundary condition (initial marching condition) was simply prescribed to be the nominal Mach 3 wind tunnel freestream condition^[75] summarized in Table 4.1. The upstream boundary condition for the Mach 5.0 simulation was set at the tunnel freestream design conditions (see Appendix D). Flow tangency was prescribed on all solid surfaces, and was enforced explicitly to first-order accuracy with a full flux method. [72] For the Mach 5.0 case, flow conditions were extrapolated (first-order) from the interior at the upper boundary of the computational domain (opposite the model). The two-factor approximately-factorized equations were solved at each streamwise marching plane, with relaxation applied in the marching direction. A third order upwind biasing (full flux) scheme was employed in the marching direction, while a second order up-winding scheme with Roe's flux difference splitting was used in the cross-flow plane.

Beginning at a location 0.4c ahead of the fin, the three-factor approximately-factorized equations were solved globally to first-order spatial accuracy by employing van Leer splitting of the inviscid fluxes^[112]. The upstream boundary condition for this region is specified to be the solution given at that plane by space-marching. Flow conditions were extrapolated to first-order from the interior at the exit boundary of the computational domain, which is at the trailing edge of the WAF model. Again, flow tangency is enforced on all solid surfaces (including the tunnel walls) explicitly to first-order accuracy with a full flux method. For the Mach 2.9 case, this region is comprised of 8 computational zones, containing a total of 825×10^3 cells. For the Mach 5.0 case, this region is also comprised of 8 computational zones, containing a total of 655×10^3 cells.

- 4.1.3 Convergence Issues. The inviscid calculations were not intended to be a rigorous computational study. The primary goal of the inviscid study was to obtain a preliminary estimate of acceptable instrument locations for the experimental study. The inviscid computations were assumed to be converged when the residual of the state vector was reduced by three orders of magnitude. At a CFL number of 1.0^[8], this required 838 iterations for the Mach 2.9 calculation and 643 iterations for the Mach 5.0 calculation.
- 4.1.4 Computational Requirements. The inviscid computations were performed on a Cray C916/161024 supercomputer. The global calculations near the fin required less that 16mWords of memory and 23.5 seconds per iteration to complete. The calculations on the slightly smaller Mach 5.0 grid required 17.5 seconds per iteration.
- 4.1.5 Inviscid Fin Simulations at Other Mach Numbers. The flow near the fin has also been numerically investigated at several Mach numbers other than 2.9 and 5.0 using the same methods discussed above. For these simulations, the effect of the blending region and tunnel were neglected by imposing the freestream boundary condition shortly upstream of the fin. This assumption minimized computational and solution storage requirements. For this study, the computational grid was identical to the 8-zones near the fin from the inviscid Mach 2.9 study (Figure 4.1).

4.2 Viscous Calculations

The Reynolds-averaged Navier-Stokes (RANS) equations were solved over the model geometry using GASP version 3.06^[7], with the algebraic turbulence model of Baldwin and Lomax^[11].

4.2.1 Grid Definition. The numerical representation of the test article used for the viscous calculations is provided in Figure 4.2. A multi-zone approach was again taken, The entire computational mesh consisted of 12 computational zones (the edges of which are shown in Figure 4.2) connected by 21 zonal boundaries and was comprised of 8.2×10^6 cells. The flow variable values were passed through the zonal boundaries via a five-point overlap.

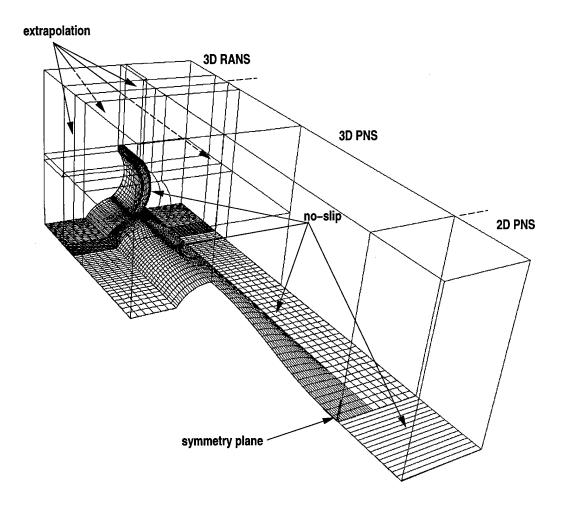


Figure 4.2 Grid boundaries and zonal structure for viscous simulations.

To resolve the features of the flowfield in the vicinity of the fin and to provide the resolution required by turbulence models, the grid was clustered near the fin and cylinder surfaces. At a location 0.4c upstream of the fin leading edge the wall grid spacing corresponded to a y^+ value of roughly 0.15 for both Mach numbers investigated. At this location, approximately half of the points in the normal direction were contained in the boundary layer. Zone faces near the fin were defined using an elliptic grid generator employing Thomas and Middlecoff^[106] control functions. Grid orthogonality was enforced along the edges of each zone, while constraining the grid points to lie on the geometry surface. [101, 100] The interior points of each zone were then positioned using a standard trans-finite interpolation (TFI) scheme. [85]

4.2.2 Solution Strategy. For all calculations the thin layer viscous terms (with Sutherland's viscosity model) were included in the governing equations. The algebraic eddy viscosity model of Baldwin and Lomax^[11] was also used to approximate turbulence. Details of this turbulence model are available in A.5. Since flow disturbances do not propagate upstream in a fully supersonic flow, and since experimental results indicated that the blended body produced no separated flow regions, the parabolized Navier-Stokes (PNS) equations were solved to a location 0.5c ahead of the fin. This location was deemed sufficiently far upstream of the fin interaction region based on previously conducted visualization experiments.^[45, 110]

To allow for the specification of a two-dimensional upstream boundary condition, the PNS equations were solved on a two-dimensional grid for a short distance (0.8r) ahead of the model body. At the inflow boundary, an experimental profile determined using pitot, cone-static, and hot-film probes was prescribed (see Appendix E). Owing to probe volume effects, experimental data could not be obtained sufficiently close to the wall to include the laminar sublayer. However, the two-dimensional PNS region allowed the boundary layer to develop into a fully turbulent profile upstream of the blended body region. The two-dimensionality of the flow in the AFIT Mach 3 wind tunnel has been well documented. [75, 110] For the sumulation of the fin in the Mach 5 wind tunnel, inflow conditions were derived from pitot pressure data. The two-dimensionality of the flow in the AFIT Mach 5 tunnel is documented in Appendix D.

The two-dimensional solution was mapped to the three-dimensional grid at the leading edge of the blended body. As in the inviscid simulations, the two-factor approximately-factorized equations were solved at each marching plane by employing a third order upwind biasing scheme with relaxation in the marching direction and a second order up-winding scheme with Roe's flux difference splitting in the cross-flow plane. The symmetry of the model body was exploited by solving the PNS equations over only half of the blended body region and by employing an x-y symmetry condition at the z=0 plane. GASP was modified to allow the solution at the final symmetric marching plane to be reflected across x-y plane. The solution at this plane was then used as the upstream condition for the downstream asymmetric region. In the vicinity of the fin (behind the plane at 0.5c ahead of

the fin) the RANS equations were solved to third-order spatial accuracy using Jacobi inner iterations^[7]. The inviscid fluxes were split by the method of van Leer^[112], and the min-mod limiter^[40] was used. This region is comprised of 8 computational zones, containing a total of 4.2×10^6 cells.

On the model surfaces, shown as a mesh in Figure 4.2, a no-slip condition on the velocity, an isothermal wall temperature, and vanishing normal pressure gradient were enforced.

$$\rho u_i = 0 T = T_{wall} \frac{\partial P}{\partial n} = 0$$

The wall temperature was 294K for the Mach 2.8 simulation. For the Mach 4.9 simulation, the effect of wall temperature was investigated by enforcing relatively cold (294K) and hot (340K) isothermal boundary conditions at the wall. An adiabatic wall condition was also examined. From these simulations, it was determined that the thermal boundary condition at the wall influences the numerical solution very little. The results presented here were obtained with a 294K isothermal boundary condition, and are indistinguishable from those obtained using the other thermal boundary conditions.

The solid surface boundary conditions were enforced explicitly to second-order accuracy with a full flux method ^[7]. Based on the results of the previously conducted experimental and inviscid numerical investigations ^[45, 110], it was presumed that the side and opposing tunnel walls had a minimal influence on the flowfield near the fin. Thus, although the size of the computational domain represents the test section, flow conditions were extrapolated (first-order) from the interior at these boundaries. This afforded great computational savings by avoiding the need to enforce a no-slip condition on the opposite and side walls. Also, since the side and opposing tunnel walls were not modeled, the same grid was used for both the Mach 2.8 and Mach 4.9 calculations. The flow conditions were also extrapolated at the downstream plane.

A substantial savings of computational resources was realized through the use of a multi-grid sequencing method. This method reduces the mesh resolution by combining every N computational cell edges into one cell edge in a given direction, where N is the sequencing level. Therefore the cellular dimension of the finer grid in the sequenced

direction must be divisible by N. This coarser grid may again be sequenced if it has suitable dimensions. In the present research, the finest grid was dimensioned such that it could be sequenced twice with N=2 in all three grid directions. This simply means that the dimension of every computational block and of every face which defined a geometry had to be evenly divisible by both 2 and 4. Initial iterations were performed on the 'coarse' grid, then that solution interpolated to the 'medium' and the 'fine' grids. This resulted in a huge savings of computational effort, as each iteration on a N=2 sequenced grid requires only about one-eighth the CPU time and memory as an iteration on its parent grid. Comparisons between the solution on the sequenced grids were made to investigate grid consistency and convergence issues.

4.2.3 Convergence Issues.

4.2.3.1 Grid Consistency. Grid sequencing not only accelerates solution convergence in almost all temporally integrated problems, but it also affords an expedient means to evaluate grid consistency. Grid sequencing was also employed in the upstream region which was evaluated by space-marching the PNS equations $(x \le -0.5c)$ as a means to determine grid consistency. Solutions indicate (Figure 4.3) that the boundary layer predicted on the 'medium' grid is unchanged by further grid refinement. Data from the fine-grid solution was used to establish the upstream boundary condition for the adjoining fin region.

Although the grid was defined with sufficient resolution at the solid surfaces to employ the algebraic turbulence model on the finest grid, the wall spacing increases with sequencing, possibly leading to erroneous eddy viscosity values. Since the implementation of algebraic closure models in regions having more than one physical length scale (i.e. near two or more solid surfaces) may cause convergence difficulties, convergence studies were conducted by solving the *laminar* form of the RANS equations in the fin region.

Pitot pressures from converged solutions on each sequence are presented in Figure 4.4 with experimental data obtained at locations aft of the bow shock. The solutions provided by the two finest grids both exhibit the same physical characteristics such the pitot pres-

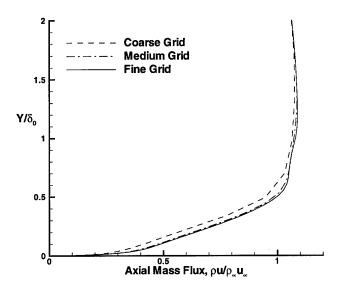


Figure 4.3 Effect of grid refinement on predicted (PNS) boundary layer profile, x=-.5c.

sure increase in the boundary layer on the convex side of the fin $(Y/\delta_0<0.5)$ and a small separation near the body on the concave side of the fin. With the exception of the thickness of this separation region, the predicted pitot pressures become more similar to the experimental data with grid refinement. As will be shown in Chapter V, the extent of the separation region on the concave side of the fin (Figure 4.4[b]) was predicted more accurately with the subsequent addition of an algebraic turbulence model.

Examination of the vortical structures ahead of the fin leading edge (Figure 4.5) indicates that the *structure* of the flowfield obtained on the coarsest grid is different than that predicted on the two finer grids. The first grid refinement provides enough resolution to predict a 4-vortex structure. Further grid refinement moves the predicted locations of these vortices slightly toward the fin. It is important to note that this region is the most difficult area of the flowfield to resolve, since the flow character is changing drastically over short distances. However, previous numerical studies on blunt fins and cylinders have indicated that it may not be necessary to resolve this region of the flow precisely. Indeed, the agreement can be very good between calculated and experimental quantities away from this region such as surface pressure on the fin and on the body near the fin, even when the number of vortices within the structure is incorrectly predicted.^[37, 88] In the present case, while the pressures gradients ahead of the fin on the model surface are slightly elevated by

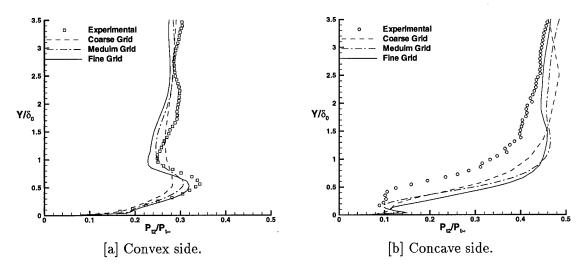


Figure 4.4 Effect of grid refinement on pitot pressure at downstream location.

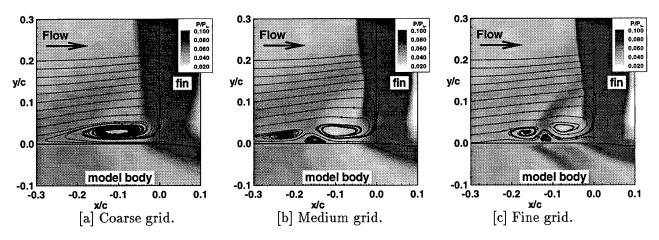


Figure 4.5 Effect of grid resolution on the computed vortical structure ahead of the fin leading edge: M=2.8 laminar RANS simulation.

the last grid refinement, the pressures on the fin surface were virtually identical. Calculated rolling moment coefficients calculated by integrating the surface pressures on the fin sides for the two finest meshes are 0.002412 (medium) and 0.002408 (fine), indicating that grid convergence was achieved in the region of interest. This moment coefficient is about the virtual missile x-axis and based on body diameter and cross-sectional area.

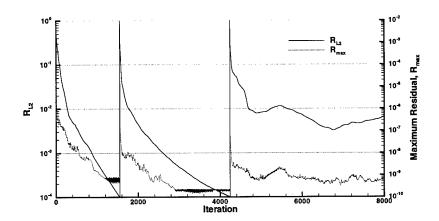


Figure 4.6 Residual history for M=2.8 laminar calculations in global region.

est sequences were time-integrated until $R_{L_2}<10^{-4}$, where R_{L_2} is defined as the Euclidean (L_2) norm of the residual vector, and is normalized its value on the first iteration of the current sequence (Figure 4.6). When approaching convergence on the finest grid, the residual vector was dominated by fluctuations in the vicinity of shock waves. This behavior is exhibited in many problems where the flowfield is comprised of regions in which the fluid motion occurs on greatly disparate time scales. In such simulations, convergence must be based on some physical properties of the flow. For the current problem, the pitot pressure on lines corresponding to the experimental data was chosen to determine temporal convergence. The turbulent calculations were performed on the finest grid only with the laminar solution as the initial condition. Temporal convergence was established in the same fashion as it was for the laminar calculation.

4.2.4 Mach 4.9 Calculations. The Mach 4.9 calculation was conducted following the same strategy used for the Mach 2.8 investigation, except that no laminar computations were performed. The Baldwin-Lomax turbulence model was used throughout the simulation, including the solutions on the sequenced grids. The convergence behavior observed during these calculations was very similar to that observed in the laminar computations at Mach 2.8 (Figure 4.8). Changes in the vortical flow structure ahead of the fin due to grid refinement were also similar to that seen at Mach 2.8 (Figure 4.5).

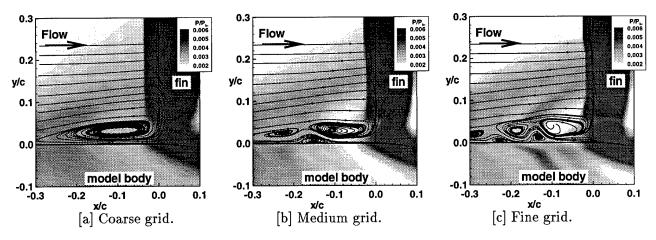


Figure 4.7 Effect of grid resolution on the computed vortical structure ahead of the fin leading edge: M=4.9 RANS simulation with Baldwin-Lomax.

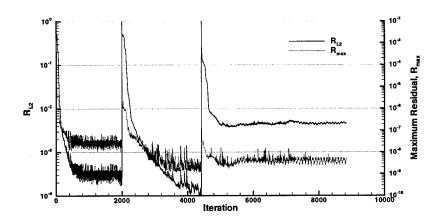


Figure 4.8 Residual history for turbulent M=4.9 calculations in global region.

4.2.5 Computational Requirements. The computational requirements for all of the RANS calculations are provided in Tables 4.2 and 4.3. As expected, the computational requirements, both in terms of memory and CPU, increase by approximately a factor of eight with each grid refinement. The Baldwin-Lomax turbulence model required about 5.5% extra memory, and 34% more time per iteration. All viscous computations were performed on a Cray C916 supercomputer.

Table 4.2 Computational requirements for Mach 2.8 RANS calculations.

Solution	Grid	Number	Required	Time
Method	Sequence	of Cells	Memory	(sec/itn)
Laminar	3	65168	$3.9\mathrm{mW}$	2.45
Laminar	2	521344	$15.3\mathrm{mW}$	14.5
Laminar	1	4170752	$107.\mathrm{mW}$	97.0
B-L turb	1	4170752	$113.\mathrm{mW}$	134.

Table 4.3 Computational requirements for Mach 4.9 RANS calculations.

Solution	Grid	Number	Required	Time
${f Method}$	Sequence	of Cells	Memory	(sec/itn)
B-L turb	3	65168	4.1mW	3.1
B-L turb	2	521344	$16.1 \mathrm{mW}$	19.2
B-L turb	1	4170752	$113.\mathrm{mW}$	133.

V. WAF Flowfield at Mach 2.8

The mean and turbulent structure of the flowfield around a single wrap-around fin mounted on a semi-cylindrical body has been investigated using the experimental and numerical methods outlined in Chapters III and IV. In this chapter, the results of the investigations of the WAF at Mach 2.8, including an analysis of the flowfield near the fin, are presented. Experimental and numerical results are used to describe the flowfield around the single-WAF configuration under consideration. The majority of the results at Mach 2.8 have already been published [45, 108, 110, 109].

First, the results of pilot inviscid calculations and photographic visualization experiments are presented. Then results of the viscous simulation and experimental exploration of the complex flowfield in the vicinity of the fin are then presented, culminating in a discussion of the aerodynamic loading.

5.1 Pilot Inviscid Calculations

The first numerical results in this study were provided by solving the Euler equations over the model geometry in the tunnel's test section (Figure 5.1). These preliminary inviscid results guided the placement of the experimental measurement stations.

5.2 Shadowgraph and Schlieren Photography

To get an initial understanding of the flowfield ahead of the fin, shadowgraph and schlieren images were obtained with the model in the test section. A shadowgraph image of the region near the fin is presented in Figure 5.2. Note how the bow shock remains detached over the full height of the fin at this Mach number. The shock induced by the blended forebody of the model can be seen coalescing and reflecting off of the opposing tunnel wall just above the fin. The bow-shock created by the fin is also visible, although the structure at the fin/body intersection is somewhat obscured by the boundary layer on the model body. The boundary layers on the model and opposing wall are also identifiable.

Composite schlieren images of the test section with the model installed are presented in Figures 5.3 and 5.4. These were made with the horizontal knife edge blocking the

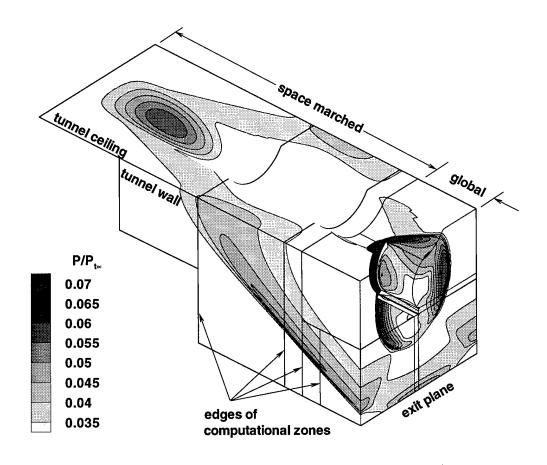


Figure 5.1 Computed inviscid test section surface pressures (at M=2.9).

top and bottom of the light, respectively, thus are theoretically negatives of one another. The turbulent boundary on the model is quite visible in Figure 5.3 whereas the shock structure near the fin/body juncture is most easily seen in Figure 5.4. The blending shock is again visible, as is the bow-shock created by the fin. The other structures in the images which extend from the floor upward are 'seam shocks'. These disturbances are caused by small imperfections in the tunnel floor associated with removable plugs which are inserted into the probe access slots and extend across most of the test section. Although these disturbances appear distinctly, subsequent measurements have shown them to be very small compared to the blending shock and the bow-shock. Their strength is exaggerated in the photographs primarily due to their two-dimensional nature. In contrast, the bow and blending shocks are three-dimensional structures.

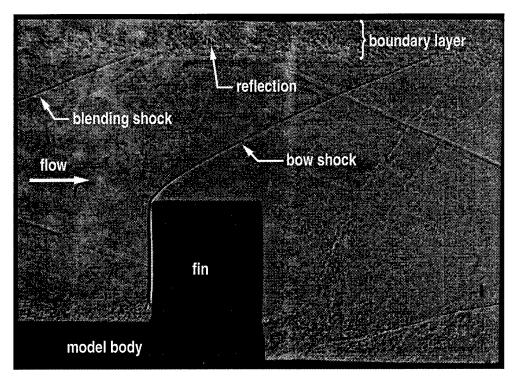


Figure 5.2 Shadowgraph of fin region.

5.3 Lambda Shock

Figures 5.5 and 5.6 are images produced by schlieren and shadowgraph photography which have been enlarged to show the detail of the flow structure in front of the base of the fin. The shock-boundary layer interaction produces the same type of λ -shock typically observed in front of blunt fins and cylinders mounted on flat plates in supersonic flowfields. ^[29, 39] The λ -shock structure was observed to be unsteady, as its position was observed to shift slightly from photograph to photograph.

Configurations possessing blunt leading edges have a stagnation point on the leading edge which corresponds to the end of a 'parting line' in the flowfield, indicating the furthest location from the body at which particles become entrained into the vortical flow ahead of the leading edge. The investigated model has a sharp leading edge, making it difficult to identify any stagnation point in the numerical solutions. However, particle traces of the viscous numerical solutions (Figures, 4.5[c], 5.8[e],& 5.9[e]) indicate that the distance from the body at which streamlines diverge as they encounter the fin leading edge is at $y\approx 0.19c$. This agrees quite well with the λ -shock height indicated by photography of $y\approx 0.20c$.

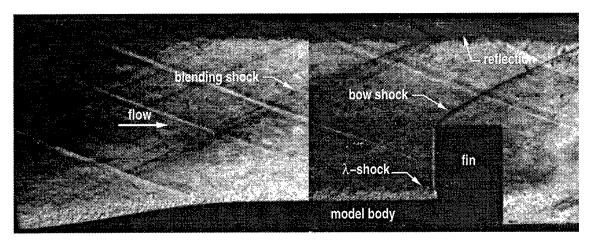


Figure 5.3 Composite schlieren photograph – knife edge on top.

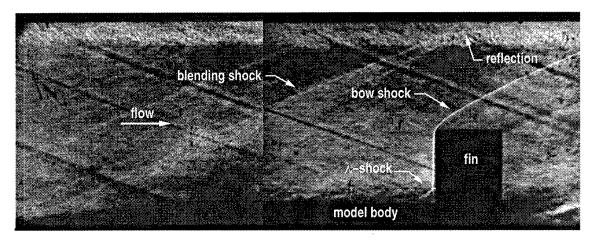


Figure 5.4 Composite schlieren photograph – knife edge on bottom.

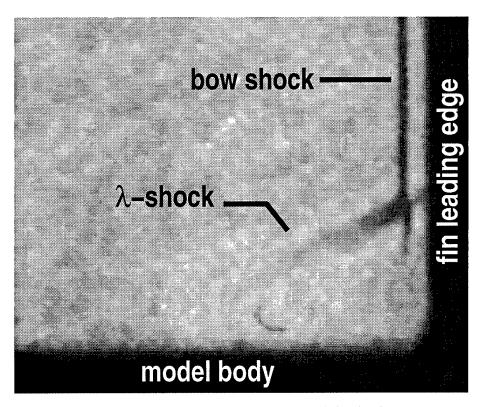


Figure 5.5 Schlieren photograph showing lambda-shock structure.

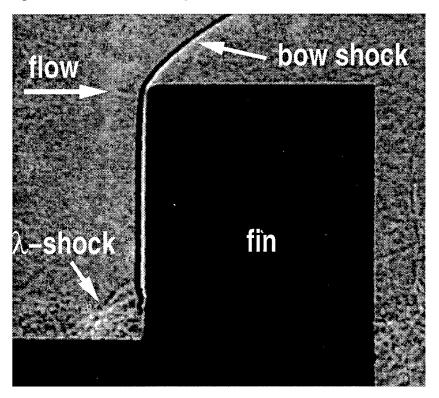


Figure 5.6 Shadowgraph of the lambda-shock region.

5.4 Effect of Fin Curvature on the Flowfield

While 2-D photography indicates flow features similar to those seen on straight fins, conventional pressure probes, hot-film anemometry, and CFD all demonstrate that the flow near the fin is highly asymmetric.^[45, 108, 110, 109]

It is convenient to discuss the flowfield in terms of three regions; an *upstream* region which is ahead of the shock structure, and two *downstream* regions, one on either side of the fin. The present study indicates that the each of the *downstream* regions can be further divided into two regions; an *outer* region which is characterized by inviscid behavior, and an *inner* region near the body in which viscous effects are dominant.

The flowfield near the single-WAF geometry has been experimentally explored[45, 110] by extensively probing the flowfield near the model. In addition to probing the outer flow at several locations near the fin on the ceiling mounted model [110], measurements were obtained nearer to the fin by mounting the model on the tunnel side-walls. The fuselage boundary layer was also surveyed at four locations on the ceiling mounted model as shown in Figure 5.7.^[45] These locations were chosen to represent the upstream and downstream regions on either side of the fin, since two of the stations set the reference for the flow upstream of the fin bow shock (at x=-0.41c) and the other two stations were positioned downstream of the shock (at x=+0.69c). At each of these axial locations, the flow was surveyed on the concave (Cc) side and on the convex (Cv) side of the fin (at $z=\pm 0.47c$) with pressure probes and hot-film cross-wires. Results from the companion numerical study were compared with the experimetal data at these locations, and the combined numerical and experimental information were examined for the purpose of characterizing the flowfield. Note that the pressure and hot-film probes flexed slightly ($\approx 2^{\circ}$) during the experiments under aerodynamic loading. The locations at which the numerical solution was 'probed' were canted to mimic this flexing.

In the data presentation, the probe position (x,y,z) is nondimensionalized by the fin chord, c=20.3mm, where the coordinate origin is located at the intersection of the body surface centerline and leading edge of the fin. Negative x values are upstream of the leading edge, and negative z values are to the concave side of the fin. Boundary layer data

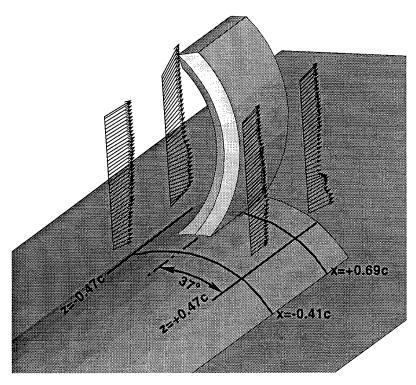
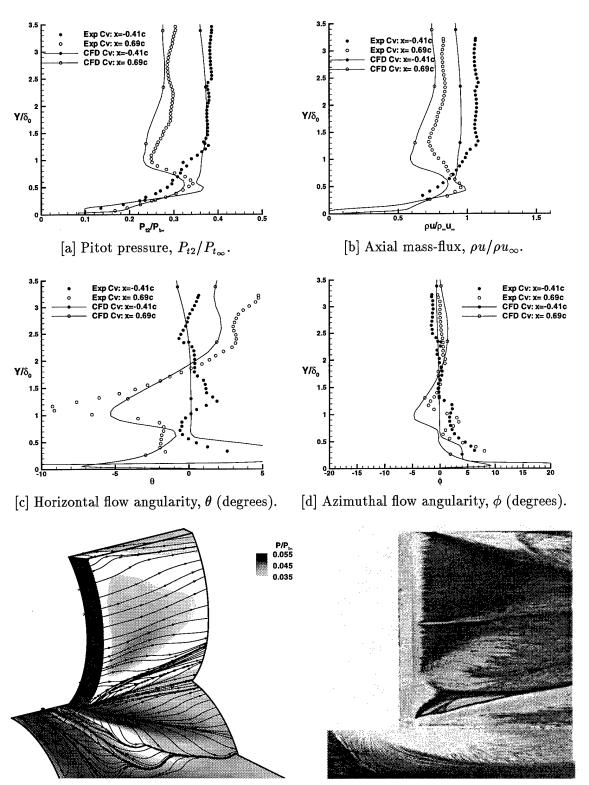


Figure 5.7 Probe locations.

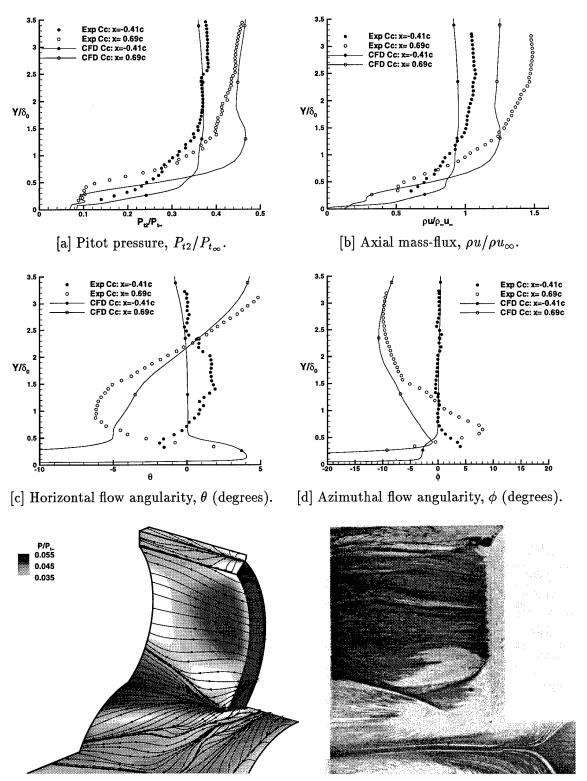
is presented as a function of the distance, from the model body, Y. This relative position from the body is normalized by a reference boundary layer thickness, $\delta_0=6.1$ mm, which was measured on the model centerline 0.41c ahead of the leading edge of the fin.

5.4.1 Flow Ahead of the Bow Shock. At the upstream measurement location, both computed and experimental pitot pressures and mass-flux profiles (see Figures 5.8 and 5.9) correspond to those of a largely "undisturbed" boundary layer. While it appears that the numerical solution predicts a thinner boundary layer than measured experimentally, the agreement is good in the outer flow region. The calculations also suggest a high degree of flow symmetry in the outer flow at the upstream measurement locations, while the degree of measured asymmetry was within the experimental uncertainty (Appendix C). At these upstream locations, the numerical results indicate that the flow in the boundary layer is moving slightly away from the centerline (Figures 5.8[d] and 5.9[d]). The flow very near the body is being swept away from the centerline at a very high angle, indicating this part of the boundary layer feels the presence of the fin.



[e] Calculated limiting surface streamlines. [f] Oil flow at Mach=2.06 (Abate and Berner).

Figure 5.8 Numerical and experimental flow variables; convex side of fin.



[e] Calculated limiting surface streamlines. [f] Oil flow at Mach=2.06 (Abate and Berner).

Figure 5.9 Numerical and experimental flow variables; concave side of fin.

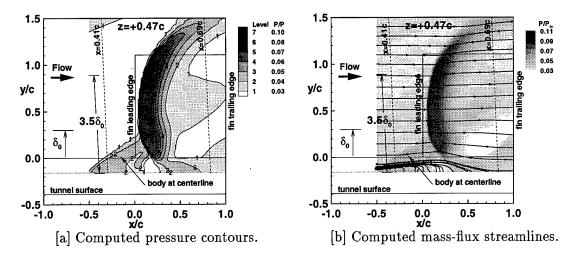
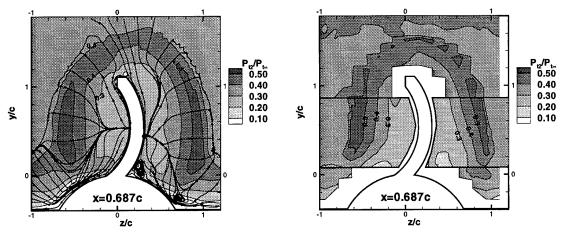


Figure 5.10 Convex measurement plane (z=+0.47c) pressure contours and mass-flux streamlines $(\rho u, \rho v)$ given by numerical simulation. Outline of fin is overlaid. Dashed lines represent survey locations in the Mach 3 tunnel.

5.4.2 Flow on the Convex Side of the Fin. As the flow nears the fin on the convex side, the outer flow $(Y/\delta_0>1.5)$ passes through a strong shock (Figure 5.10). This shock induces a strong compression and deceleration. As the fluid passes the fin it is expanded through a large region of favorable pressure gradient between the shock and the downstream measurement location (seen in Figure 5.10) due primarily to the convex fin curvature.

At the downstream survey location, the pitot pressure and mass-flux in the outer flow has been decreased on the convex side relative to the upstream reference plane. This effect has been captured by both inviscid^[110] and viscous numerical results (Figures 5.8[a]&[b]). At this measurement station the outer flow is directed away from the body, but only mildly away from the fin. This behavior is seen in both the experimental data and the computational results (Figures 5.8[a]&[b]).

Profiles of pressure and momentum in the boundary layer at this location are characterized by a large inflection (Figure 5.8[a]&[b]). The flow near $Y/\delta_0 \approx 1.1$ has passed over the horseshoe vortex system produced by the shock/boundary-layer interaction ahead of the fin (see Figure 5.10). In this process, the flow greatly expands while only slightly accelerating; the net result is a decrease in the mass-flux. Flow in this region is directed strongly toward the body as indicated by the inflection in the horizontal flow angularity



- [a] Numerical pitot pressure and streamlines.
- [b] Experimental pitot pressure.

Figure 5.11 Flow at x=0.69c measurement plane given by numerical simulation and experiment.

(Figure 5.8[c]). Agreement with experimental data is considered excellent, although the flow turning angle is somewhat underpredicted. Examination of the numerical results indicate that this turning effect is due to a vortex embedded in the fin/fuselage juncture which entrains fluid, pulling it toward the body (seen in Figure 5.11[a]). This vortex creates the pressure minimum seen both numerically and experimentally in Figure 5.8[a]. At roughly the same location, a mild secondary flow component toward the fin $(\phi < 0^{\circ})$ is observed in the numerical solution; while a corresponding inflection is observed in the experimental results (Figure 5.8[d]). Although the numerical and experimental ϕ profiles are somewhat different, the discrepancies may be attributed to probe volume effects and probe location errors (see Section C.4). Notably, if the location at which the numerical solution is examined is shifted by the probe volume (1mm) closer to the fin, the predicted inflection in ϕ very closely resembles the experimentally obtained data (Figure 5.12[b]). Also, the flattening of the θ profile in the experimental data over the range $0.3 < Y/\delta_0 < 0.8$ is closely duplicated (Figure 5.12[a]). It is notable that the juncture vortex and the associated acceleration toward the body are viscous phenomena and thus have not been captured by inviscid methods.^[110] The significance of this finding is addressed in Section 5.5.

Slightly closer to the body $(Y/\delta_0\epsilon[0.3,1.0])$, the flow experiences a compression from above while is at the same time aligned with the x-axis near the body. The net effect is

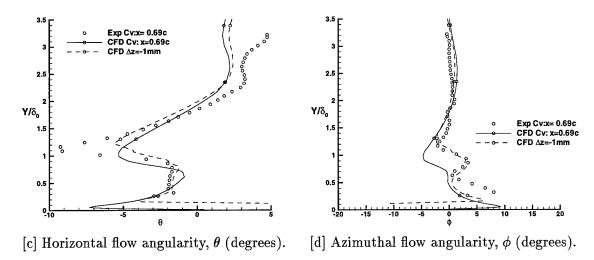


Figure 5.12 Effect of $\Delta z = -1$ mm on flow angularity; convex side of fin.

a sharp increase in mass-flux. Below $Y/\delta_0\approx 0.3$, wall effects force a decrease in mass-flux and pitot pressure. The flow is directed downward and away from the fin over a very small region $(Y/\delta_0<0.2)$, following the contour of the body. The numerical results and oil flow patterns at Mach 2.06^[2] (discussed below) suggest that the azimuthal flow angularity, ϕ , at this location tends toward zero at the wall.

Given its proximity to the fin, and hence its effects on the aerodynamic loading, more discussion on the 'juncture' vortex is warranted. The juncture vortex (Figure 5.13) originates near the leading edge of the fin/body juncture and remains tucked into the fin/body junction, growing in strength and size as it progresses along the fin. The size and orientation of this vortex is clearly evident in limiting surface streamlines calculated from the numerical solution (Figure 5.8[e]) and in the surface oil flow patterns obtained by Abate and Berner^[2] at Mach 2.06 (Figure 5.8[f]). Surface streamlines starting at the leading edge travel downward along the beveled edge and join with streamlines flowing up from the root to form an accumulation of oil film (or convergence of streamlines) on the surface. This convergence line marks the separation line formed by the juncture vortex, and moves away from the juncture as it travels toward the trailing edge. The complicated flow structure observed in the oil flow patterns closely resembles that predicted by the numerical solution, suggesting that the flow structure near the juncture changes little within this Mach number range. On the body, a weak attachment line (surface streamline

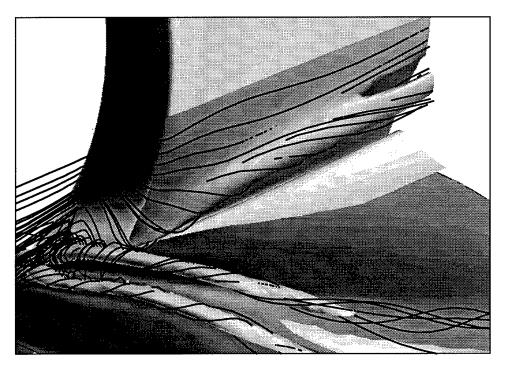


Figure 5.13 Stagnation pressure iso-surfaces and streamlines in juncture vortex region on convex side of the fin.

divergence) moving outward from the leading edge is clearly evident in both the numerical solution (Figure 5.8[e]) and the oil flow (Figure 5.8[f]).

Evidence of such a vortex has also been observed in oil flow patterns on straight blunt fins mounted on flat plates.^[24, 34] Such vortices have been observed to change rotational direction on straight fins depending on incidence angle.^[34] The viscous numerical results indicate that the rotation of the juncture is of the same sense as that seen on the compression side of a straight fin at incidence. Thus, with respect to the juncture vortex, fin curvature and attachment angle can induce similar effects to those produced by cross-flow.

5.4.3 Flow on the Concave Side of the Fin. In contrast to the flow on the convex side of the fin, the flow on the concave side passes through a somewhat weaker shock (Figure 5.14). Thus, the flow undergoes a much more modest deceleration. Also, the post-shock expansion is partially offset by the compressive effects of fin curvature. The net effect is a dramatic increase in the mass-flux (up to 30%) at the downstream measurement

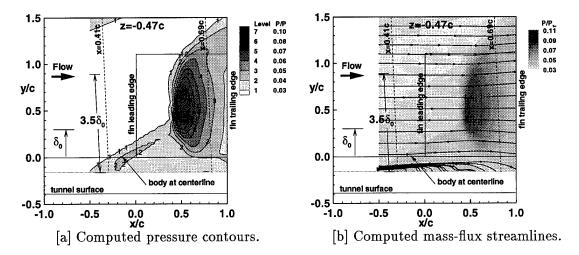


Figure 5.14 Concave measurement plane (z=-0.47c) pressure contours and mass-flux streamlines $(\rho u, \rho v)$ given by numerical simulation. Outline of fin is overlaid. Dashed lines represent survey locations in the Mach 3 tunnel.

location as compared to the upstream location; This is evident in both the numerical and experimental data. On this side of the fin, the outer flow is strongly directed away from the fin (Figure 5.9[d]) at flow angles, ϕ , up to 10° at the mid-span $(Y/\delta_0\approx 2.5)$. Here, numerical and experimental results indicate that $\theta=0^{\circ}$, meaning that the flow is directed toward the center of fin curvature (Figures 5.9[c] and 5.11[a]).

Approaching the body, the fluid momentum decreases (Figure 5.9[a]&[b]). Over a small region inside the boundary layer $(Y/\delta_0\epsilon[0.5, 1.1])$, the numerical solution suggests that there is a large inflection in the azimuthal angularity (Figure 5.9[d]) where the flow is almost aligned with the vertical plane $(\phi\approx0^\circ)$. This inflection is more pronounced in the experiment data, but occurs at the same location. This effect is likely to be a combination of the flow wrapping around the fin and an expansion which reflects off of the bow shock as a compression. Inviscid numerical results[45, 110, 109] only faintly hinted at this trend. Over this same range, the experimental data (Figure 5.9[c]) suggests that the magnitude of the horizontal flow angularity is greatly reduced (i.e. $\theta\to0$ at $Y/\delta_0\approx0.3$). However, this change in flow angularity was not present in the numerical solution at the nominal measurement location. This discrepancy can be attributed to probe volume effects and probe location errors (see Section C.4). Notably, this trend is clearly present in the numerical solution at a probe width (1mm) further from the fin (Figure 5.15[a]).

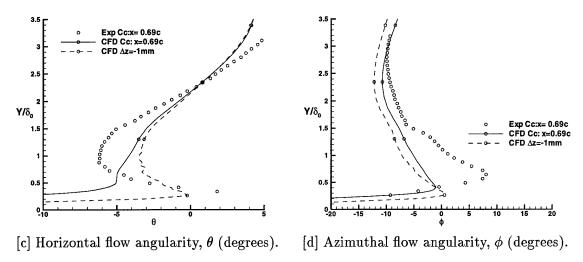


Figure 5.15 Effect of $\Delta z = +1$ mm on flow angularity; concave side of fin.

Closer to the body $(Y/\delta_0<0.5)$ there is a small region in which measured and computed pitot pressures do not change. The numerical results suggest that the flow is moving downward and away from the fin $(\theta\approx-30^{\circ},\phi\approx-39^{\circ})$, lending to the flattening of pitot pressure. Cross-wire volume effects precluded experimental examination of this region.^[45]

On this side of the fin, surface streamlines starting at the leading edge also travel downward along the beveled edge and join with streamlines flowing up from the root. However the streamline convergence is 'incomplete' from below, and no juncture vortex is indicated. As on the convex side, the similarities between the predicted surface streamlines and the observed oil flow patterns of Abate and Berner at Mach $2.06^{[2]}$ suggest that the flow structure near the juncture on this side of the fin changes little within this Mach number range. The downstream measurement station on this side of the fin is located just behind a separation line on the body, which is seen in the computational results and oil flow pattern. Due to the oblique attachment angle ($\approx 135^{\circ}$), no juncture vortex was observed on the concave side of the fin in either the numerical or experimental studies, nor is one indicated by the oil flow visualizations at Mach 2.06 (Figures 5.9[e]&[f]).

In comparing the numerical results to the oil flow patterns of Abate and Berner^[2], is is notable that the latter was obtained on a four-finned missile. Thus the similarity between fin surface streamline patterns suggests that the single-fin model produces the relevant flow features present on configurations with multiple wrap-around fins.

5.5 Aerodynamic Loading on the Fin

The diverse flow topologies on either side of the WAF produce an axisymmetric load distribution on the fin surface. While previous inviscid calculations have captured many of the essential flow features, the juncture vortex on the convex side of the fin is dominated by viscous effects and its position and growth near the fin root may provide a significant aerodynamic load, particularly at higher Mach numbers.

The fin surface pressures computed in the inviscid and viscous simulations are shown in Figures 5.16 and 5.17, respectively. On the concave side of the fin, the bow shock is "focused", producing a high pressure region between the fin and its center of curvature (Figure 5.11) where mass flux levels are increased to 50% over the free-stream value. This produces large region of relatively high surface pressures near the half-span of the fin that contributes to a negative rolling moment (Figures 5.16[b] and 5.17[b]). Here, rolling moment will be defined in the vehicle stability sense, thus a negative value indicates a moment acting in the direction of negative curvature. The inviscid calculations predicted that the convex side of the fin also had a region near the fin root over which high pressure levels nearly reach the magnitudes seen on the concave side. This compression had been attributed to the fin being canted in the convex direction (≈45°) at the fin/body intersection.[110] However, the viscous numerical results show that this high pressure region is displaced by the boundary layer, and weakened greatly (Figure 5.17[a]). Instead of high pressure, the root region is dominated by low pressures induced by the juncture vortex. Using inviscid numerical methods, Abate and Cook^[3] have shown that the rolling moment is a function of both the fin curvature and fin attachment angle. However, it is now clear that the effect of fin attachment angle is not fully captured by an inviscid analysis. While the Euler analysis predicted a rolling moment coefficient of -0.0102, the viscous simulation predicted a value of -0.0112, a 10% increase.

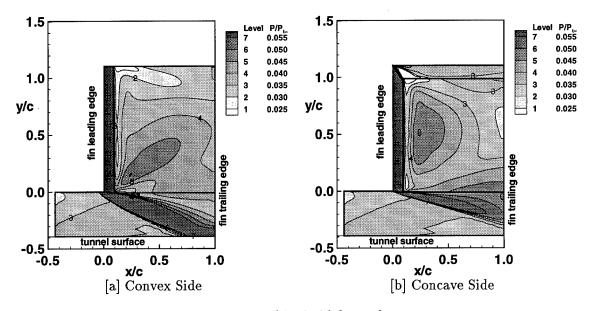


Figure 5.16 Computed inviscid fin surface pressures.

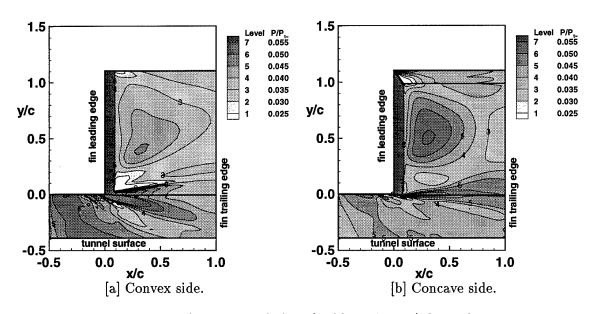


Figure 5.17 Computed viscous turbulent (Baldwin-Lomax) fin surface pressures.

5.6 Effect of the Fin on Fuselage Boundary Layer Turbulence

Turbulence quantities were also measured at the same locations discussed in Section 5.4 (see Figure 5.7).^[45] Although the downstream probe location on the concave side of the fin is in a region of mild favorable pressure gradient, it is also very close to the bow shock. Examination of the turbulence intensity in this region indicates that the shock induces an increase in the axial (Figure 5.18[a]) and transverse (Figures 5.18[b] and 5.18[c]) turbulence intensity, which is consistent with the destabilizing effects of adverse pressure gradients on turbulent boundary layers.^[99]

On the convex side, the turbulence intensities at the same streamwise location are far lower, since the flow has experienced a favorable pressure gradient over an extended streamwise distance (Figure 5.10). Expansions have been reported to *stabilize*, or reduce, the turbulence levels. [99] Also contributing to this dramatic recovery is the rapid flow acceleration induced by the convex curvature of the fin. Both of the secondary massflux turbulence intensities experience a sharp rise near $Y/\delta_0=1.1$, but not so the axial component. The rise in cross-flow turbulence intensity occurs at the same location where the mean flow is being turned sharply toward the body by the juncture vortex.

The net effect of the bow shock and fin curvature are illustrated in Figures 5.19 and 5.20 via the nondimensional turbulent kinetic energy (TKE), K_c , defined by

$$K_c = rac{1}{2} \left[\overline{\left(rac{\left(
ho u
ight)'}{\overline{
ho u}}
ight)^2} + \overline{\left(rac{\left(
ho v
ight)'}{\overline{
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ight)^2} + \overline{\left(rac{\left(
ho w
ight)'}{\overline{
ho u}}
ight)^2}
ight]$$

The TKE is significantly elevated on the concave side of the fin and reduced on the convex side relative to values upstream of the shock (Figure 5.19).

Figure 5.20 shows the nondimensional TKE at two streamwise stations; one at the same location as the boundary layer measurements (x=+0.69c), and one further upstream at x=+0.38c. These surveys, which included the upper portion of the boundary layer, indicate that TKE levels on the convex side are markedly greater than those on the concave side at both stations. Also, TKE is dissipating in the axial direction on both sides of the fin, as the flow passes through regions of favorable pressure gradient. Thus, as the flow

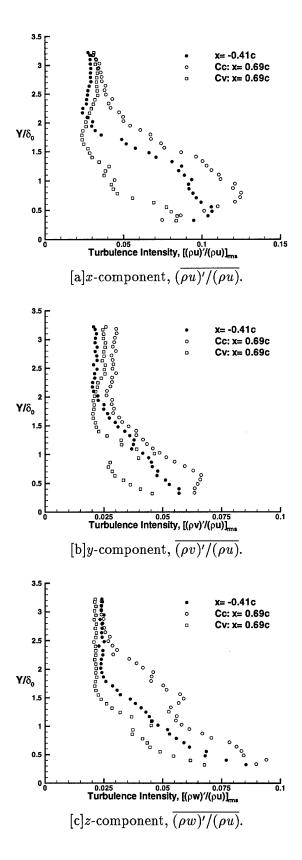


Figure 5.18 Turbulence intensity profiles. 5-19

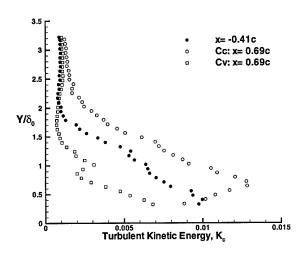


Figure 5.19 Turbulent kinetic energy, K_c .

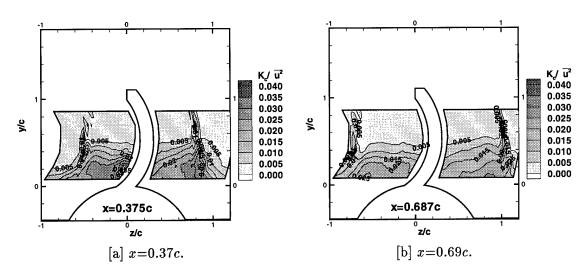


Figure 5.20 Turbulent kinetic energy, K_c .

continues to recover, the TKE levels on the concave side of the fin are likely to continue decreasing in the downstream direction, possibly to the levels seen on the convex side.

The stabilizing and destabilizing effects on turbulence to either side of the fin are also revealed in the Reynolds shear stress estimates measured with the cross-wire (Equation 3.6, Chapter III) presented in Figure 5.21. Upstream of the fin, the shear stress profile corresponds to that of an undisturbed boundary layer, with levels comparable to those upstream of the model. This indicates that the effects of the compression caused by the blended region of the model have been damped to levels comparable to an equilibrium

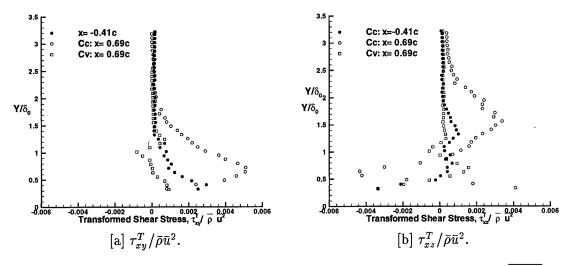


Figure 5.21 Measured turbulent shear stresses, $\tau_{ij}^T = -\frac{\overline{(\rho u_i)'(\rho u_i)'}}{\overline{\rho}} + \overline{\rho} \ \overline{u_i} \ \overline{u_j} \ \overline{\left(\frac{\rho'}{\overline{\rho}}\right)^2}$.

turbulent boundary layer. Note that the second term of the total turbulent shear stress in Equation 3.6 has been determined to be at least an order of magnitude smaller than the first term for all surveyed regions, even in those having large flow angularity. Therefore, only the total turbulent shear stress is presented.

On the convex side of the fin, a reduction of turbulent shear stress with downstream position is indicative of the strong stabilizing effect of favorable pressure gradient. Indeed, as observed by other researchers investigating correlations between streamline distortion and turbulence^[16], the expansion associated with a favorable pressure gradient can result in reduced (or even negative) turbulent shear stress. Conversely, the shear stress on the concave side is increased by roughly 100–200%, commensurate with the previously noted increases in turbulence intensity and turbulent kinetic energy. This pattern is consistent with other measurements obtained in regions of large compression.^[16] Note too that the boundary layer thickness has dramatically increased (by about 60–70%) on the concave side, while it was reduced slightly on the convex side. The large increase in turbulent shear stress on the concave side of the fin may the primary reason that measured pitot pressure and mass flux levels were less than those predicted by the numerical simulation in the outer boundary layer (Figure 5.9[a]&[b]), since the Baldwin-Lomax turbulence model was not designed to simulate the effects of pressure gradient on turbulence.

VI. WAF Flowfield at Mach 4.9

The single-WAF model has also been investigated experimentally and numerically at Mach 4.9 and a unit Reynolds number of $\text{Re}/\ell \approx 65-75\times 10^6 \text{m}^{-1}$. These investigations were aimed at determining the structure of the mean flowfield at a high-speed condition.

In the experiment, the mean flow around the ceiling-mounted WAF configuration was surveyed using pitot and cone-static probes and was visualized using shadowgraph and schlieren photography in the AFIT Mach 5 wind tunnel (Appendix D). Fuselage boundary layer surveys were obtained upstream and downstream of the bow shock. The fuselage boundary layer flow was explored near the fin on the ceiling mounted model, as it was in the Mach 3 tunnel. Placement of the measurement stations for the experiment was guided by the inviscid computations (Figure 6.1) and by experience gained from the experiment in the Mach 3 tunnel. The probe locations were the same in the span-wise direction $(z=\pm 0.47c)$ as they were in the Mach 2.8 experiment, and the stations that set the reference for the flow were again placed just upstream of the flow interaction at x=-0.41c. However, the probes were positioned further aft at the downstream locations (x=+0.84c) so as to remain well behind the bow shock.

In the viscous numerical simulation, the Navier-Stokes equations were solved using the same computational grid and numerical strategy used for the Mach 2.8 simulation. The algebraic turbulence model of Baldwin and Lomax^[11] was again employed. Experimental pressure data was used to define the upstream boundary condition for this calculation. The resulting numerical solution is compared with the experimental data and the combined sets of information are examined to characterize the flowfield.

In the presentation of the results, the probe position (x,y,z) is nondimensionalized by the fin chord as it was for the Mach 2.8 results. Boundary layer data is presented as a function of the distance from the model body, Y. This relative position from the body is normalized by a reference boundary layer thickness, $\delta_{\infty}=10.2$ mm, which was measured on the tunnel centerline 0.8r ahead of the blended body. Note that this is larger than the dimension ($\delta_0=6.2$ mm) by which the Mach 2.8 results were normalized. Although the pressure probes used in the Mach 5 wind tunnel experienced higher loadings than

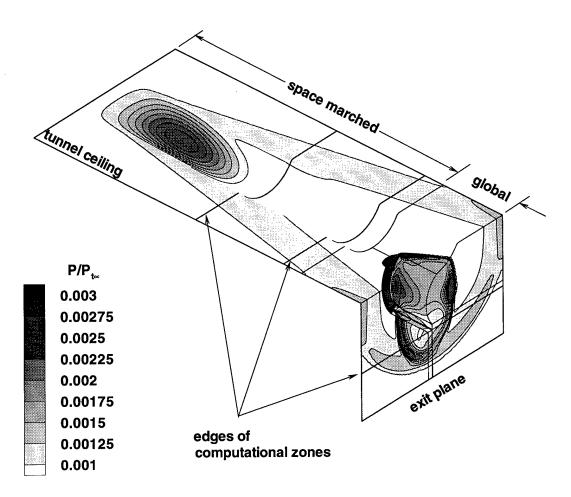


Figure 6.1 Computed inviscid test section surface pressures (at M=5.0).

the probes used in the Mach 3 tunnel, they were much stiffer and experienced less flexing (≈1.1°). The locations at which the numerical solution is compared to experimental results are canted to mimic this flexing.

6.1 Shadowgraph and Schlieren Photography

Shadowgraphs and schlieren images of the fin region (Figures 6.2 and 6.3) again indicate that fin shock remained detached over the full span of the fin as it did at Mach 2.8, although stand-off distance was reduced. The same principal features observed at the lower Mach number were again visible, including the shock caused by the blended forebody and the bow shock, both of which were more highly swept than at Mach 2.8. The λ -shock

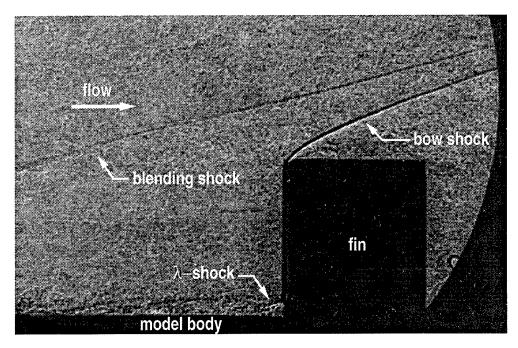


Figure 6.2 Shadowgraph of fin region (M=4.9).

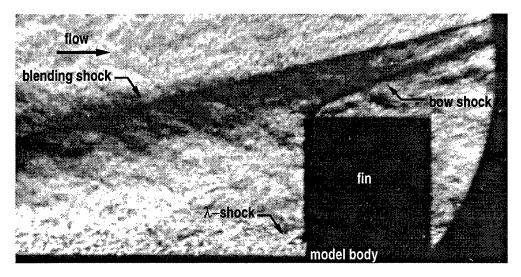


Figure 6.3 Schlieren photograph (M=4.9).

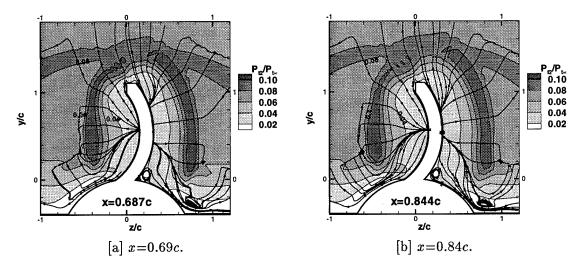


Figure 6.4 Computed pitot pressure and secondary streamlines at M=2.8 measurement plane, and at present measurement plane (x=0.84c).

was also distinct, though somewhat unsteady, and positioned slightly closer to the body and at a shallower angle than observed in the Mach 2.8 experiment (cf Figures 5.2 and 6.2). This trend was also captured in the viscous numerical solutions (cf Figures 4.5 and 4.7).

6.2 Effect of Fin Curvature on the Mean Flowfield

The experimental and numerical results suggest that the flow near the fin is highly asymmetric as it was at Mach 2.8. In fact, most of the qualitative discussion on the flowfield structure at Mach 2.8 (Chapter V) applies at Mach 4.9 as well. As expected, the fin's domain of influence in the outer flow was reduced from that at Mach 2.8 (Figure 6.4).

The measured flow asymmetry at the upstream measurement plane was minimal (Figure 6.5), and well within the experimental uncertainty (especially considering that the data were acquired on different days). At this upstream location, there is a much larger pressure gradient in the direction away from the body than was observed at Mach 2.8 due to the relative proximity of the blending shock.

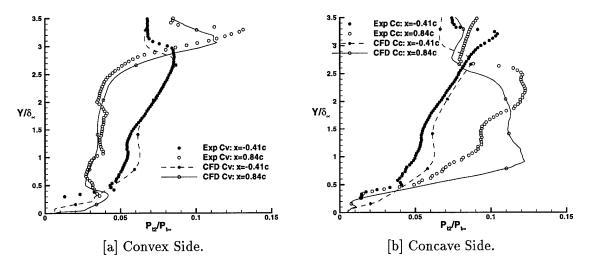


Figure 6.5 Experimental and numerical pitot pressure.

6.2.1 Flow on the Convex Side of the Fin. As seen at Mach 2.8, the flow on the convex side of the fin passes through a strong shock (Figure 6.6[a]), and then expands through a large region of favorable pressure gradient between the shock and the downstream measurement location due to the convex fin curvature. Relative to its upstream value, the pitot pressure in the outer flow at the downstream measurement station has been decreased by about 40% (Figure 6.5[a]). Agreement between experimental and computed pitot pressures is considered excellent.

The calculated pitot pressure profile features a large inflection in the inner region (Figure 6.5[a]). This inflection is more difficult to identify in the experimental results than it was at Mach 2.8. While volume of the pitot probe used at Mach 5 precluded a definitive assessment of this feature, it appears that the inflection may be closer to the body and not as large as that predicted by the numerical simulation. The computed pressure peak is at the approximately the same physical distance from the wall at both Mach numbers $(0.3\delta_{\infty}\approx 0.5\delta_{0})$.

Recall from the Mach 2.8 discussion that this inflection in pitot pressure was associated with the existence of a juncture vortex. This vortex is also present in the solution at Mach 4.9 (Figure 6.7), and is probably present in the experimental flowfield, although the pressure data does not provide conclusive evidence. The predicted rotational direction at Mach 4.9 is the same as it was at Mach 2.8, but the predicted location of the junc-

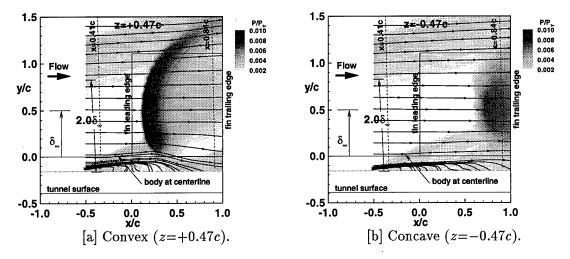


Figure 6.6 Computed pressure and mass-flux streamlines $(\rho u, \rho v)$ on measurement planes (M=4.9). Outline of fin is overlaid. Dashed lines represent survey locations.

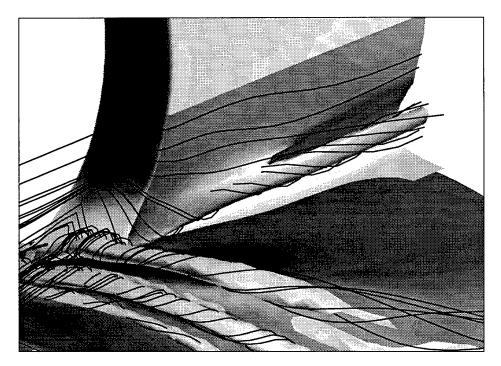


Figure 6.7 Stagnation pressure iso-surfaces and streamlines in juncture vortex region on convex side of the fin.

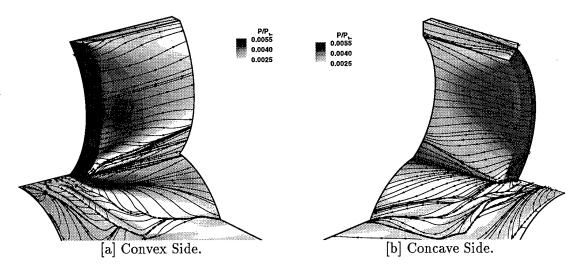


Figure 6.8 Computed limiting surface streamlines at M=4.9.

ture vortex is slightly closer to the fuselage (cf Figures 5.11[a] and 6.4[a]). The size and orientation of this vortex is also indicated by the calculated limiting surface streamlines (Figure 6.8[a]). While the structure of the surface streamlines on the fin are very similar to those calculated at Mach 2.8, the separation line formed by the juncture vortex is slightly closer to the body. Also, the weak attachment line on the body moving outward from the leading edge is slightly closer to the fin than predicted at Mach 2.8.

6.2.2 Flow on the Concave Side of the Fin. As was the case at Mach 2.8, the outer flow $(Y/\delta_{\infty}>1.0)$ on the concave-side measurement plane passes through a somewhat weaker shock than on the convex side (Figure 6.6[b]). Again, the post-shock expansion is partially offset by the compressive effects of fin curvature. The net effect is a very large increase in the pitot pressure (up to 90%) and momentum by the time the flow reaches the downstream measurement location. This increase is observed in both the numerical and experimental data (Figure 6.5[b]), and is even more dramatic than at Mach 2.8. The overprediction of the pitot pressure in the outer boundary layer on this side of the fin is probably again the result of the lack of pressure gradient effects in the turbulence model.

Close to the body $(Y/\delta_{\infty}<0.4)$ there is a small region over which measured and numerical pitot pressures do not change. The viscous simulations suggest that the flow in this region is moving down and away from the fin at angles comparable to those predicted

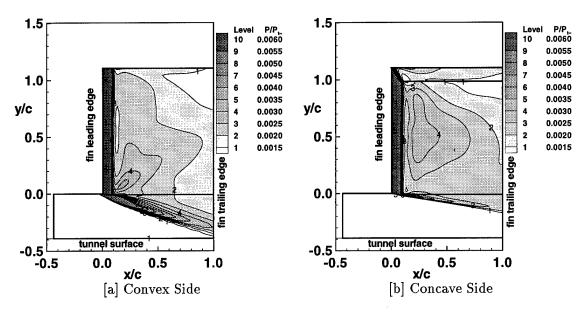


Figure 6.9 Computed inviscid fin surface pressures.

at Mach 2.8, leading again to a 'flattening' of pitot pressure. The similarities between the calculated flowfields the two Mach numbers (M=2.8,4.9), as well as the similarity of calculated surface streamline patterns to the oil flow patterns of Abate and Berner at Mach 2.06^[2], suggest that the flow structure on the concave side of the fin changes little with Mach number. The exception is the trajectory of the incomplete surface streamline convergence on the fin, which becomes more obtuse with decreasing Mach number. The downstream measurement station on this side of the fin is again located just behind a separation line on the body which is at approximately the same location as it was at Mach 2.8. On this side of the fin, the calculated secondary flow structure is also very similar to that predicted at Mach 2.8 (cf Figure 6.4[a] and 5.11[a]). The outer flow is strongly directed away from the fin toward the center of fin curvature at the mid-span, and again, no juncture vortex is observed on this side of the fin.

6.3 Aerodynamic Loading on the Fin

As was true at Mach 2.8, diverse flow topology on either side of the WAF produce a dramatically different load distributions on the opposing fin surfaces. The fin surface pressures predicted by the inviscid and viscous simulations are shown in Figures 6.9 and 6.10, respectively. The computed rolling moment from this simulation at Mach 4.9 is about

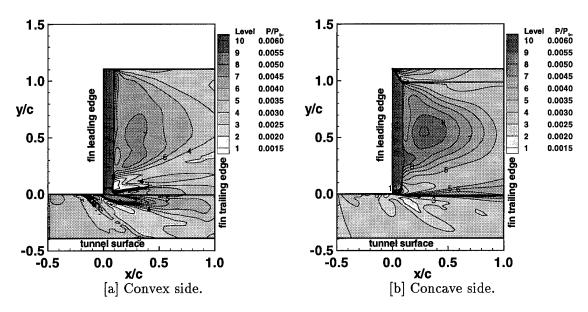


Figure 6.10 Computed viscous turbulent (Baldwin-Lomax) fin surface pressures.

one-third of that predicted at Mach 2.8, and is about 60% of that predicted by inviscid simulation. As shown in Figure 6.11, the viscous simulations suggest that Mach number has a stronger influence on rolling moment that inviscid simulations would imply.

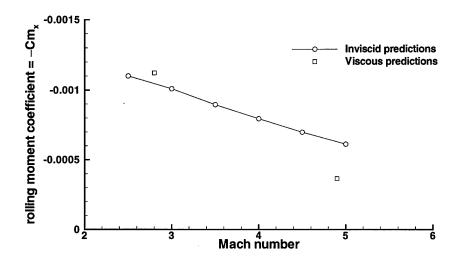


Figure 6.11 Computed rolling moments.

VII. Conclusions and Recommendations

7.1 Conclusions

The structure of the flowfield near a single wrap-around fin (WAF) mounted on a semi-cylindrical body has been characterized using both experimental and numerical methods at Mach numbers of 2.8 and 4.9. A single-finned model was first extensively tested in the AFIT Mach 3 wind tunnel. In this experiment, the flow around the test article was surveyed at several stations along its length, concentrating on the region near the fin. While the boundary layer on the fin was determined to be too thin to survey with pressure or hot-film cross-wire probes, the boundary layer on the missile fuselage was easily explored using these devices. The result was a mapping of the pressure, velocity, and turbulent properties near the fin. The mean flow near the model was also obtained in the AFIT Mach 5 wind tunnel. Taken together, these experimental studies comprise a set of mean flow and turbulence data not previously available for curved fins.

Companion numerical studies were also performed wherein the Reynolds averaged Navier-Stokes equations were solved with the algebraic turbulence model of Baldwin and Lomax^[11] in the vicinity of the single-WAF model. The excellent agreement with experimental data suggests that the calculations have captured the relevant flow physics involved in this complicated flowfield. It is notable that the oil flow pattern of Abate and Berner^[2] to which these results compared so favorably was obtained on a four-finned missile. Thus the resemblance of computed and observed surface streamline patterns on the fin suggests that the present study, which uses a simplified single-fin model, captures the relevant flow features in the fin region for an non-spinning missile with multiple wrap-around fins. Taken in concert, the experimental and numerical results have been interpreted to characterize the flowfield in the vicinity of a wrap-around fin. Based on the results of this research, several conclusions may be made regarding the nature of the flowfield near wrap-around fins.

One of the more significant findings of the present study is that both inviscid and viscous properties play significant roles in determining the structure of the flowfield near WAFs. The outer flowfield exhibits asymmetries brought about by the effects of pressure

gradient, streamline curvature, and differing shock/expansion structures — while viscous phenomena induce asymmetries near the fuselage. Regarding the latter, the Navier-Stokes simulations predicted a vortex in the fin/body juncture on the convex side of the fin. This vortex, not present on the concave side presumably due to the oblique fin attachment angle, increases the pressure loading near the fin root. The net result is a pressure differential across the fin which alters the rolling moment. Both hot-film anemometry and surface flow visualizations corroborate the existence of this viscous-induced vortical structure. Inviscid simulations cannot capture this vortex and thus may not be expected to reasonably predict the stability behavior of missiles having WAFs.

That said, many aspects of the flowfield were accurately captured by solving the Euler equations. The bow shock created by the wrap-around fin is an inviscid phenomenon. Except in the immediate vicinity of the fin/body intersection where the bow shock interacts with the missile body boundary layer, the pressure field is dominated by inviscid effects. This has been demonstrated through the excellent agreement between measured quantities and those predicted by inviscid (as well as viscous) numerical methods in the outer region of the flow. The shock remains detached over the full span of the fin at Mach 2.8 and at Mach 4.9, and its interaction with the fuselage boundary layer creates the same type of λ -shock associated with blunt fins in supersonic flowfields.

The reduction of data from the pitot, cone-static and hot-film probes at Mach 2.8 produced a significant amount of turbulence data. Prior to this study, no detailed mean flow or turbulence measurements existed for WAF missile configurations. These data yielded some interesting insights. As expected, the bow shock causes a dramatic increase in turbulent kinetic energy and Reynolds shear stress on both sides of the fin. The flow experiences an expansion as it passes the fin which reduces the turbulence intensity. However, for a fixed streamwise location, the reduction is far greater on the convex side of the fin, where the flow experiences a stronger favorable pressure gradient over a longer distance. This results in lower turbulence intensities, producing lower, though still significant, shear stresses. It is notable that the turbulence model used was not designed to account for the effects of pressure gradient and streamline curvature. This may be largely responsible for the overprediction of momentum levels in the outer boundary layer on the concave side of the fin

in the present numerical simulations. It is expected that this turbulence data will be useful for validation of turbulence closure models intended to predict flows having large pressure gradients.

At Mach 4.9, both the numerical and experimental results qualitatively resemble those obtained at Mach 2.8. Examination of the computed surface streamline patterns suggests that the flow structure in the inner viscous region is somewhat invariant over this range of Mach number. However, the juncture vortex is observed to shift slightly toward the body with increasing Mach number, causing a dramatic reduction in computed rolling moment compared to that predicted by inviscid theory. Again, this would seem to underscore the importance of viscous effects on the rolling moment.

7.2 Recommendations

Although the present study has provided clearer picture of the flowfield near a WAF in the given environment, it was by necessity limited in scope, and thus represents a first step toward understanding the flowfield dynamics of deployed missiles employing WAFs. What follows are suggested research areas that could expand the understanding of WAF aerodynamics. Unquestionably, this problem should continue to be addressed using both experimental and numerical means.

- 7.2.1 General. As a means of addressing the problems induced by the variation in rolling moment with Mach number, the current research suggests than remedies which act to alter, or perhaps even eliminate, the juncture vortex may provide fruitful. Techniques which act to reduce or eliminate much of the loading asymmetry near the root by altering the effective fin attachment angles should be explored.
- 7.2.2 Experimental. It is recommended that the experiment at Mach 4.9 be extended to include a hot-film exploration of the flowfield near the WAF model. The data from such experiments would provide the same type of detailed flow angularity and turbulence data that was obtained at Mach 2.8. The AFIT Mach 5 wind tunnel is currently being modified to enable such measurements.

It is also suggested that surface flow visualization (oil film and/or pressure-sensitive paint) be obtained at several Mach numbers on both spinning and non-spinning WAF configurations to identify significant changes or bifurcations in the flow structure near the juncture. Such flow visualizations may also provide insight as to the effects of unit Reynolds number on the flow structure.

7.2.3 Numerical. From a numerical prospective, a reasonable next-step would be to study the effects of cross-flow on the flowfield near the fin. WAFs most certainly encounter cross-flow due to missile spinning and yaw (among other factors), which are likely to have significant effects on fin loading. Experiments on sharp-fin/flat-plate geometries have demonstrated a considerable dependency of juncture vortex structure on cross-flow.^[33, 34] The effect of cross-flow could be numerically investigated for the current geometry by solving the governing equations subject to periodic boundary conditions.

Clearly numerical simulations which address fin interaction issues as well as the effects of Mach number and Reynolds number should be conducted. Further, simulations which employ turbulence models capable of resolving flowfields which are characterized by regions of large pressure gradient should be evaluated against the current body of experimental data.

Appendix A. Turbulent Navier-Stokes Equations

A.1 Overview

It has become clear that computational fluid dynamics (CFD) will play an increasing role in the design of future high speed vehicles and weapons. In fact, due to the difficulties and large expense associated with ground testing such configurations, CFD is becoming a necessity in the design process. The flow over such vehicles is characterized by turbulent structures that are not well understood. This lack of understanding has remained the major obstruction to accurately simulating complicated high-speed flows, and turbulence modeling has remained the controlling factor in the accuracy of predicting such flows. Recently, Settles and Dodson^[96] pointed out that the modeling community is sorely lacking adequate experimental data that meets the high standards required by modern code validation. One of the objectives of the experimental portion of the research was to help fill that void.

There is every reason to believe that turbulence is contained in the Navier-Stokes equations. However, since turbulent flows are characterized by temporal and spatial scales that range over several orders of magnitude, direct numerical solutions of the unsteady Navier-Stokes equations for turbulent problems of practical interest are highly unlikely in the foreseeable future. Thus, researchers are restricted to considering time averages of turbulent motion, and to rely on approximation methods to provide solutions to high Reynolds number problems.

The two most prevalent forms of the governing equations are the Reynolds (time) averaged and Favré (mass-weighted-time) averaged forms of the N-S equations (RANS and FANS, respectively). In either case, additional fluctuation cross-correlation terms appear in the averaged form of the equations, resulting in a mathematical system having more unknowns than equations (details follow this section). Reducing the number of unknowns to the number of equations is known as the "closure" problem. [68] Thus, the function of turbulence modeling is to accurately represent for these terms, either by expressing them as functions of mean flow properties, or by expressing them in terms of additional transport equations. The form of the closure model depends on the type of averaging,

Favré (FANS) or Reynolds (RANS). In the past, researchers have often made use of ad hoc assumptions to achieve closure of the N-S equations. The assumptions result in turbulence models which are rigorously incorrect. While these simplified turbulence models do serve a purpose and have had some degree of success, they are inadequate for predictions of compressible viscous/inviscid interactions such as shock/boundary-layer interaction. [66, 96]

The Reynolds averaged equations are obtained by un-coupling the instantaneous flow properties into a time-average mean value plus a fluctuating turbulent contribution, e.g.,

$$\phi = \overline{\phi} + \phi'$$

where $\overline{\phi}$ is the time-averaged quantity, and ϕ' is the instantaneous turbulent fluctuating component. The Favré-averaged quantity and the Favré turbulent fluctuation of the quantity is are given by

$$ilde{\phi} = rac{\overline{
ho\phi}}{\overline{
ho}} \qquad ext{and} \qquad \phi'' = \phi - ilde{\phi}$$

respectively. Note that, by definition, the time average Reynolds fluctuation $\overline{\phi'}$, is zero, however, the time average of the Favré fluctuation, $\overline{\phi''}$, is non-zero. The form of the compressible FANS cross-correlation terms are very similar in appearance to those of the incompressible RANS. This coupled with Morkovin's hypothesis^[77] which states that "the turbulence structure is unaffected by compressibility as long as the fluctuation Mach number is less that unity" has led to the current virtually universal trend of adopting the FANS equations for high speed compressible flows. As a result, practically all compressible turbulence models represent direct extensions of incompressible formulations, where the constants are adjusted and the density is allowed to vary. Such corrections do little more than correlate the data upon which the models are based. [75] In fact, Morkovin's own Mach 1.77 expansion fan/boundary layer interaction data [78] suggests that the compressible $\overline{u}\overline{\rho'}\overline{v'}$ term in the Reynolds shear stress is of the same order as the typical incompressible $\overline{\nu}\overline{v'}$ term.

A.2 Navier-Stokes Equations

In Cartesian coordinates the Navier-Stokes equations may be written^[66]:

Conservation of Mass

$$\rho_{,t} + (\rho u_i)_{,i} = 0 \tag{A.1}$$

Conservation of Momentum

$$(\rho u_i)_{,t} + (\rho u_i u_j)_{,j} = \sigma_{ij,j} \tag{A.2}$$

Conservation of Energy

$$(\rho E)_{,t} + (\rho E u_i)_{,i} = (\sigma_{ij} u_j)_{,i} - q_{i,i}$$
(A.3)

or

$$(\rho H)_{,t} + (\rho H u_i)_{,i} = p_{,t} + (\tau_{ij} u_j)_{,i} - q_{i,i}$$
(A.4)

where

$$E = e + \frac{1}{2}u_{i}u_{i} , \quad H = e + \frac{p}{\rho} + \frac{1}{2}u_{i}u_{i} , \quad e = C_{v}T$$

$$\sigma_{ij} = -p\delta_{ij} + \tau_{ij} , \quad \tau_{ij} = 2\mu s_{ij} - \mu^{*}u_{k,k}\delta_{ij} , \quad s_{ij} = \frac{1}{2}(u_{i,j} + u_{j,i})$$

$$\mu^{*} = \frac{2}{3}\mu - \mu_{bulk} , \quad q_{i} = -\kappa T_{,i}$$
(A.5)

A.3 Reynolds (Time) Averaged Navier-Stokes Equations

When using Reynolds averaging, any given primitive flow quantity, ϕ , is expressed as the sum of a time-averaged component, $\overline{\phi}$ and a fluctuating component, ϕ' , as follows^[66]:

$$\begin{split} \rho &= \overline{\rho} + \rho' \qquad u_i = \overline{u}_i + u'_i \qquad p = \overline{p} + p' \qquad T = \overline{T} + T' \qquad E = \overline{E} + E' \\ H &= \overline{H} + H' \qquad \mu = \overline{\mu} + \mu' \qquad \mu^* = \overline{\mu^*} + \mu^{*'} \qquad C_v = \overline{C_v} + C'_v \qquad C_p = \overline{C_p} + C'_p \end{split}$$

The time average is defined by

$$\overline{\phi} = \frac{1}{T} \int_{t_0}^{t_0 + T} \phi \, dt \tag{A.6}$$

where the characteristic time T is long in comparison to the cycle times of the fluctuating component, but still permits gradual time-dependent fluid motion for non-stationary flows.

To obtain the mean flow equations, these expressions for the decomposed variables are substituted into the governing equations. These instantaneous equations are then time

averaged, expanded, and simplified.^[105, 116] The results are the time averaged (or Reynolds averaged) Navier-Stokes equations given below in conservative form.^[38, 66, 14]

Mean Continuity

$$\overline{\rho}_{,t} + (\overline{\rho}\,\overline{u_j} + \overline{\rho'u_j'})_{,j} = 0 \tag{A.7}$$

Mean Momentum

$$(\overline{\rho}\,\overline{u_i} + \overline{\rho'u_i'})_{,t} + (\overline{\rho}\,\overline{u_i}\,\overline{u_j})_{,j} = -\overline{p}_{,i} + (\tau_{ij} + \tau_{ij}^T)_{,j}$$
(A.8)

Mean Energy

$$(\overline{\rho}\,\overline{e_0} + \overline{\rho'h_0'})_{,t} + (\overline{\rho}\,\overline{h_0}\,\overline{u_j})_{,j} = (\overline{u_i}\,\overline{\tau_{ij}} + \overline{u'\tau_{ij}'} - q_j - q_j^T)_{,j}$$
(A.9)

with the Equation of State

$$\overline{p} = \overline{\rho}R\overline{T} + R\overline{\rho'T'} \tag{A.10}$$

where the compressible RANS turbulence terms have been defined to be

$$m_{i}^{T} = -\overline{\rho' u'_{i}}$$

$$\tau_{ij}^{T} = -\overline{\rho} \ \overline{u'_{i} u'_{j}} - \overline{u_{i}} \ \overline{\rho' u'_{j}} - \overline{u_{j}} \ \overline{\rho' u'_{i}} - \overline{\rho' u'_{i} u'_{j}}$$

$$q_{i}^{T} = +\overline{\rho} \ \overline{h'_{0} u'_{i}} + \overline{h_{0}} \ \overline{\rho' u'_{i}} + \overline{u_{i}} \ \overline{\rho' h'_{0}} + \overline{\rho' h'_{0} u'_{i}}$$
(A.11)

However, this process introduces an additional 6 unknowns. In these equations e_o and h_o are stagnation conditions (i.e., $e_o = e + \frac{1}{2}u_iu_i$). The terms which are due to Reynolds averaging are the turbulent apparent mass, m_i^T , compressible turbulent shear stress, τ_{ij}^T , and compressible turbulent heat flux, q_i^T . For thin layer flows, these reduce to:

$$m_y^T = -\overline{\rho'v'} \qquad \tau_{xy}^T = -\overline{\rho} \ \overline{u'v'} - \overline{u} \ m_y^T \qquad q_y^T = +\overline{\rho} \ \overline{h_0'v'} - \overline{h_0} \ m_y^T \qquad (A.12)$$

and for incompressible flows:

A.4 Favré Averaged Navier-Stokes Equations

When employing Favré averaging, any given primitive flow quantity, ϕ , is expressed as the sum of a mass-weighted-averaged mean value (Favré averaged), $\tilde{\phi}$, and a fluctuating component, ϕ'' . The Favré averaged quantity and the Favré turbulent fluctuation of the quantity are defined as^[66]:

$$\tilde{\phi} = \frac{\overline{\rho\phi}}{\overline{\rho}}$$
 and $\phi'' = \phi - \tilde{\phi}$ (A.14)

It should be noted that although $\overline{\phi''} \neq 0$, it is also true that

$$\overline{\rho\phi} = \overline{\rho(\tilde{\phi} + \phi'')} = \overline{\rho\tilde{\phi}} + \overline{\rho\phi''} = \overline{\rho}\tilde{\phi} + \overline{\rho\phi''} = \overline{\rho}\frac{\overline{\rho\phi}}{\overline{\rho}} + \overline{\rho\phi''} = \overline{\rho\phi} + \overline{\rho\phi''}$$

so, it must be true that $\overline{\rho \phi''} = 0$. Also, the following relationships can be derived

$$\overline{\phi} - \widetilde{\phi} = \phi'' - \phi' = \overline{\phi''} = -\frac{\overline{\rho'\phi''}}{\overline{\rho}} = -\frac{\overline{\rho'\phi'}}{\overline{\rho}}$$

The Favré averaged equations, as presented by Marvin^[68] (and corrected here), are Continuity:

$$\frac{\partial \overline{\rho}}{\partial t} + \frac{\partial (\overline{\rho}\tilde{u}_i)}{\partial x_i} = 0 \tag{A.15}$$

Momentum:

$$\frac{\partial(\overline{\rho}\tilde{u}_i)}{\partial t} + \frac{\partial(\overline{\rho}\tilde{u}_i\tilde{u}_j)}{\partial x_j} = -\frac{\partial\tilde{p}}{\partial x_i} + \frac{\partial(\overline{\tau}_{ij} - \overline{\rho}u_i''u_j'')}{\partial x_j}$$
(A.16)

Energy:

$$\frac{\partial \overline{\rho}\tilde{h}}{\partial t} + \frac{\partial (\overline{\rho}\tilde{h}\tilde{u}_{j})}{\partial x_{j}} = \frac{\partial \tilde{p}}{\partial t} + \tilde{u}_{j}\frac{\partial \tilde{p}}{\partial x_{j}} + \overline{u_{j}''\frac{\partial p}{\partial x_{j}}} + \frac{\partial (-\overline{q}_{j} - \overline{\rho}h''u_{j}'')}{\partial x_{j}} + \overline{\tau_{ij}\frac{\partial u_{i}''}{\partial x_{j}}}$$
(A.17)

These equations have the same form as the *incompressible* Reynolds averaged equations, except that the Reynolds stresses $\overline{\rho u_i'' u_j''}$ include the density fluctuations, which must be accounted for in some way. Compressibility is generally included by replacing the density with the mean density neglecting the terms which involve additional correlations arising from compressibility. Researchers using the Favré forms of the governing equations

cite that avoiding some of the fluctuating density-generated terms simplifies closure of the system. However since much of the experimental data provides RANS-type information, modeling the effects of compressibility is problematic. The lack of an explicit fluctuating density component in the turbulent shear stresses is one of the specific shortcomings of this model.

The compressible FANS turbulence terms may be expressed as

$$m_i^T = 0$$
 $\tau_{ij}^T = -\overline{\rho u_i'' u_j''}$ $q_i^T = \overline{\rho h_o'' u_i''}$ (A.18)

Note that these *compressible* Favré averaged terms are similar in appearance to their *incompressible* Reynolds averaged counterparts (Equation A.13). Bowersox and Schetz^[15] have shown that cross-wire anemometry is well suited for measurement of RANS turbulent terms. In particular, they have shown that the total shear stress can be directly measured for thin layer type flows. Furthermore, if the effects of the pressure fluctuations on the hotwire response are small, then the multiple overheat cross-wire results can be decomposed into all of the terms in Equation A.11. This assumption has been verified by Bowersox and Schetz^[15] for a Mach 4.0 free mixing layer, and Kistler^[53] suggests that is valid for supersonic boundary layers up to Mach 4.7.

There are also forms of the Navier-Stokes equations in which both Reynolds- and Favré averaging are used.^[66] In these equations, the Reynolds average is often used for the density, pressure, transport coefficients, and specific heats, and Favré averaging is used for the other quantities.

A.5 Zero-Equation Turbulence Models (Baldwin-Lomax)

Both the RANS and FANS equations have additional fluctuation cross-correlation terms appear in the averaged form of the equations, causing them to have more unknowns than equations. Thus, turbulence modeling must be used to reduce the number of unknowns (or increase the number of equations) to close the system. This can be accomplished by expressing the cross-correlation terms as functions of mean flow properties, or by expressing them in terms of additional transport equations.

The following discussion is in no way intended to be a thorough review of turbulence modeling, but only a brief overview of the type of turbulence model used in the the current research.

The simplest, and most widely used turbulence models are derivatives of the method of Cebeci and Smith [18, 19, 17]. The main drawback of this method is that the boundary layer thickness has to be known. In zero-equation (algebraic) models, the concept of a turbulent or eddy viscosity, μ_t , is used. This eddy viscosity is simply added to the molecular viscosity in the governing equations, i.e.,

$$\mu \rightarrow \mu + \mu_t$$

Also, a turbulent Prandtl number, Pr_t , is defined such that

$$\frac{\kappa}{C_p} \to \frac{\mu}{Pr} + \frac{\mu_t}{Pr_t}$$

in the energy equation. Baldwin and Lomax^[11] modified the model to eliminate the need for finding the edge of the boundary layer, δ .

$$\mu_t = \left\{ egin{array}{ll} (\mu_t)_{ ext{inner}} & y \leq y_c \ (\mu_t)_{ ext{outer}} & y_c < y \end{array}
ight.$$

where y is the normal distance from the wall, and y_c is the smallest value of y at which the outer formulation is to be used.

The inner region is based on the em Prandtl-van Driest formulation

$$(\mu_t)_{\mathrm{inner}} =
ho \ell^2 |\omega|$$

where the mixing length and scaled coordinate are

$$\ell = ky \left[1 - e^{-y^+/A^+} \right]$$
 and $y^+ = \frac{\rho_w u_\tau y}{\mu_w} = \frac{\sqrt{\rho_w \tau_w} y}{\mu_w}$

where $u_{\tau} = \sqrt{\frac{\tau_{w}}{\rho_{w}}}$ is the friction velocity, and $|\omega|$ is the magnitude of the vorticity. The outer layer model is a modification of the Clauser formulation.

$$(\mu_t)_{ ext{outer}} = K C_{ ext{cp}} \, \rho \, F_{ ext{wake}} \, F_{ ext{kleb}}(y)$$

in which K is the Clauser constant, C_{cp} is a constant, and the wake function is given by

$$F_{
m wake} = min \left\{ egin{array}{l} y_{
m max} F_{
m max} \ \\ C_{
m wk} \ y_{
m max} \ u_{
m diff}^2 / F_{
m max} \end{array}
ight\}$$

where F_{\max} is the maximum value of the function

$$F(y) = y|\omega| \left[1 - e^{-y^+/A^+} \right]$$

and y_{max} is the value of y at which F_{max} occurs. The Klebanoff intermittency factor is given by

$$F_{\text{kleb}}(y) = \left[1 + 5.5 \left(\frac{C_{\text{kleb}}y}{y_{\text{max}}}\right)^{6}\right]^{-1}$$

The constants specified to agree with Cebeci-Smith formulation for constant pressure boundary layers at transonic speeds, and are given as

$$A^{+} = 26$$
 $C_{cp} = 1.6$ $C_{kleb} = 0.3$ $C_{wk} = 0.25$ $k = 0.4$ $K = 0.0168$ $Pr = 0.72$ $Pr_{t} = 0.9$

While simulating the flow about supersonic pointed bodies at large incidence, Degani and Schiff modified the method to properly account for the associated large regions of cross-flow separation.^[22] This allowed the method to more accurately predict these turbulent 3-D vortical flows using the thin layer parabolized Navier-Stokes (PNS) equations.

Appendix B. Hot-Film Methods for Turbulence

Care must be taken when comparisons between numerical and experimental results are made. However, it is clear that hot-film anemometry responds to time-averaged mass fluxes and total temperatures [13]. The present research uses single-overheat thermal anemometry to measure the compressible Reynolds turbulence data in a Mach 2.8 $(\text{Re}/\ell=18\times10^6\text{m}^{-1})$ flow involving a shock/boundary-layer interaction. Detailed three-dimensional surveys of pressure and mass fluxes have been obtained, enabeling the calculation of turbulant quantities such as the turbulence intensities and Reynolds turbulent shear stresses.

The constant temperature hot-film anemometer $^{[84, 67]}$ records the voltage required to maintain the film at a constant known temperature. The power required to maintain this temperature is equivalent to the heat transfer, q_f , between the hot-film and the surrounding flow. The Nusselt number can be related to the heat transfer from the film by

$$Nu = \frac{q_f}{\pi k L (T_f - T_e)}$$
 (B.1)

Where T_e is the temperature the unheated film would approach under these specific flow conditions (equilibrium temperature).

The basic shape of a hot film probe used in this research is a cylinder and the form of the Nusselt number for compressible flow in dimensionless heat transfer is [57]:

$$Nu = fcn(L/d, M, Pr, Re_e, \tau)$$
(B.2)

L/d is the film aspect ratio; M is the Mach number; Pr is the Prandtl Number; Re_e is the effective cooling Reynolds number base on film diameter; and τ is the temperature loading factor. The temperature loading factor can be expressed as

$$\tau = \frac{T_f - T_e}{T_t}$$

where T_f is the film temperature and T_e is the equilibrium temperature, or the temperature that the unheated film would attain if placed in the flow. For Reynolds numbers greater

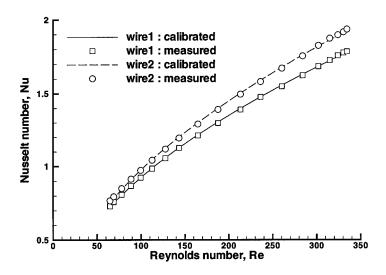


Figure B.1 Sample two-film calibration using King's Law.

than about 20, T_e is about 97% of T_t . When the Mach number normal to the film is greater than 1.2, or $Msin\varphi \ge 1$, Pr is assumed constant, and the aspect ratio $L/d \gg 1$, the function for the Nusselt number simplifies to

$$Nu = fcn(Re_e, \tau)$$
 (B.3)

It has been determined experimentally by Bowersox and Schetz^[15] that *King's Law*, the functional relationship between Nusselt number and Reynolds number for incompressible flow, is also an acceptable relationship for compressible flows.

$$Nu = a_k \sqrt{Re_e} + b_k \tag{B.4}$$

where the constants a_k and b_k must be experimentally determined for each value of T_f . Sample data from a two-film cross-wire calibration along with the corresponding King's Law curve fits are presented in Figure B.1. By definition, the Nusselt number is also proportional to the film power

$$Nu = \frac{q_f}{\pi k_t L(T_f - T_t)}$$
(B.5)

where

$$q_f = {i_f}^2 R_f$$
 and $i_f = \frac{E_f}{R_f + R_s + R_L}$

Here R_f is the film resistance, R_s is the resistance of the resistor in series with the film, and R_L is the probe lead resistance. Assuming that $T_e=T_t$ (which results in minimal error if done in both the calibration and the data reduction), the Nusselt number can be written as

$$Nu = \frac{E_f^2 R_f}{(R_f + R_s + R_L)^2} \frac{1}{\pi k_t L (T_f - T_e)}$$
(B.6)

The turbulent power laws for viscosity and thermal conductivity are used to determine Nusselt and Reynolds numbers.

$$k_t = k_0 \left(\frac{T_t}{T_0}\right)^{n_k} \qquad n_k = 0.89$$

$$\mu_t = \mu_0 \left(\frac{T_t}{T_0}\right)^{n_\mu} \qquad n_\mu = 0.77$$
(B.7)

Combining (B.4), (B.6), and (B.7), gives the hot film response equation

$$\frac{E_f^2}{C_0} = \left(\frac{T_t}{T_0}\right)^{n_k} \left[a_k \sqrt{\text{Re}_{0_e}} \left(\frac{T_t}{T_0}\right)^{-n_{\mu}/2} + b_k \right] (T_f - T_t)$$
 (B.8)

where Re_{0_e} is the effective Reynolds number with $\mu = \mu_0$, and

$$C_0 = \frac{(R_f + R_s + R_L)^2}{R_f} \pi L k_0 \tag{B.9}$$

B.1 Turbulence Fluctuations

Replacing E_f , Re_{0_e} , and T_t by their mean and fluctuating components in the *hot* film response equation (B.10), using the Binomial Theorem, retaining only the first order terms, and noting that

$$\frac{\overline{E_f}^2}{C_0} = \left(\frac{\overline{T_t}}{T_0}\right)^{n_k} \left[a_k \sqrt{\overline{\mathrm{Re}_{0_e}}} + b_k\right] (T_f - \overline{T_t})$$
(B.10)

then solving for $E'_f/\overline{E_f}$, the hot film fluctuation equation is derived in the form

$$\frac{E_f'}{\overline{E_f}} = f\left(\frac{\operatorname{Re}_{0_e}'}{\overline{\operatorname{Re}_{0_e}}}\right) + g\left(\frac{T_t'}{\overline{T_t}}\right) \tag{B.11}$$

where the hot film sensitivities are given by

$$f = \frac{1}{4} \left[1 + \frac{b_k}{a_k \sqrt{\overline{Re}_e}} \right]^{-1} \quad \text{and} \quad g = \frac{-\overline{T_t}}{2(T_f - \overline{T_t})} + \frac{n_k}{2} - f \, n_\mu$$
 (B.12)

For the single-overheat technique [13], the sensitivity to total temperature fluctuation is minimized by operating the hot-film at large overheat ratios $(\frac{R_f}{R_{ref}} \approx 2)$; hence g is small. For flows where the total temperature fluctuations, T_t' , is also small, the second term in Equation B.11 can be neglected. For Mach 3 boundary layers, the total temperature fluctuation has been found to be small $(\frac{T_t'}{T_t} \approx 2-3\%)$, thus neglecting that term is reasonable. Specifically, the AFIT Mach 3 wind tunnel has been found to maintain total temperature fluctuations below about 2.0%. [44, 45, 70, 75] To evaluate f, \overline{Re}_e is found from Equation B.10, where $\overline{T_t}$ is assumed equal to the plenum total temperature, $T_{t_{\infty}}$.

B.1.0.1 Decomposition into Cartesian Coordinates. To derive the formulas for analysis, the effective Reynolds number given by the previous section must be related to the x-y coordinate system. Since φ did not vary substantially from the calibration values, the cosine law was assumed valid, i.e.,

$$\left\{
\begin{array}{c}
\operatorname{Re}_{n} \\
\operatorname{Re}_{t}
\end{array}
\right\} = \left[
\begin{array}{c}
\cos \varphi & \sin \varphi \\
-\sin \varphi & \cos \varphi
\end{array}
\right] \left\{
\begin{array}{c}
\operatorname{Re}_{x} \\
\operatorname{Re}_{y}
\end{array}
\right\}$$
(B.13)

Thus the effective cooling Reynolds number becomes

$$\operatorname{Re}_{e}^{2} = A_{1} \operatorname{Re}_{x}^{2} + 2A_{2} \operatorname{Re}_{x} \operatorname{Re}_{y} + A_{3} \operatorname{Re}_{y}^{2}$$
 (B.14)

where A_i are given by

$$A_{1} = \cos^{2} \varphi$$

$$A_{2} = \cos \varphi \sin \varphi$$

$$A_{3} = \sin^{2} \varphi$$
(B.15)

and φ is the incidence angle of the hot film to the flow.

Replacing Re_{0_x} , Re_{0_x} and Re_{0_y} by their mean and fluctuating components and applying the binomial theorem, with $R_0 \ll 1$, one can show that

$$\overline{\operatorname{Re}_{0_{ej}}} \equiv \overline{\operatorname{Re}_{0_x}} \sqrt{B_{3j}} \tag{B.16}$$

and write the fluctuation equation as

$$\left(\frac{\operatorname{Re}_{0_{e}}'}{\overline{\operatorname{Re}_{0_{e}}}}\right)_{j} \equiv B_{1j} \left(\frac{\operatorname{Re}_{0_{x}}'}{\overline{\operatorname{Re}_{0_{x}}}}\right) + B_{2j} \left(\frac{\operatorname{Re}_{0_{y}}'}{\overline{\operatorname{Re}_{0_{x}}}}\right)$$
(B.17)

where the index j sums over the two films on the cross-film probe, and

$$R_{0} \equiv \frac{\overline{Re_{0}_{y}}}{\overline{Re_{0}_{x}}} = \overline{\rho v}/\overline{\rho u}$$

$$B_{1} \equiv \frac{A_{1}}{B_{3}}$$

$$B_{2} \equiv \frac{A_{2}}{B_{3}}$$

$$B_{3} \equiv A_{1} + 2A_{2}R_{0}$$
(B.18)

Solving this set of equations and decomposing into x and y components

$$\overline{\operatorname{Re}_{0_x}}^2 = \frac{\overline{\operatorname{Re}_{0_{e1}}}^2 / A_{21} - \overline{\operatorname{Re}_{0_{e2}}}^2 / A_{22}}{A_{11} / A_{21} - A_{12} / A_{22}}$$
(B.19)

$$\overline{\mathrm{Re}_{0_{y}}} = \frac{1}{2\overline{\mathrm{Re}_{0_{x}}}} \frac{\overline{\mathrm{Re}_{0_{e_{1}}}}^{2} / A_{11} - \overline{\mathrm{Re}_{0_{e_{2}}}}^{2} / A_{12}}{A_{21} / A_{11} - A_{22} / A_{12}}$$

The turbulence variables can be decomposed into x and y components via (B.17) as

$$\frac{\left(\frac{\operatorname{Re}_{0_{x}}'}{\overline{\operatorname{Re}_{0_{x}}}'}\right)^{2}}{\left(\frac{\operatorname{Re}_{0_{e}}'}{\overline{\operatorname{Re}_{0_{e}}}'}\right)^{2}} = \frac{1}{D_{2}^{2}} \left[\frac{1}{B_{21}^{2}} \overline{\left(\frac{\operatorname{Re}_{0_{e}}'}{\overline{\operatorname{Re}_{0_{e}}}}\right)^{2}} - \frac{2}{B_{21}B_{22}} \overline{\left(\frac{\operatorname{Re}_{0_{e}}'}{\overline{\operatorname{Re}_{0_{e}}}}\right)^{2}} + \frac{1}{B_{22}^{2}} \overline{\left(\frac{\operatorname{Re}_{0_{e}}'}{\overline{\operatorname{Re}_{0_{e}}}}\right)^{2}}\right] \\
\frac{\left(B.20\right)}{\left(\frac{\operatorname{Re}_{0_{y}}'}{\overline{\operatorname{Re}_{0_{x}}}}\right)^{2}} = \frac{1}{D_{1}^{2}} \left[\frac{1}{B_{11}^{2}} \overline{\left(\frac{\operatorname{Re}_{0_{e}}'}{\overline{\operatorname{Re}_{0_{e}}}}\right)^{2}} - \frac{2}{B_{11}B_{12}} \overline{\left(\frac{\operatorname{Re}_{0_{e}}'}{\overline{\operatorname{Re}_{0_{e}}}}\right)^{2}} + \frac{1}{B_{12}^{2}} \overline{\left(\frac{\operatorname{Re}_{0_{e}}'}{\overline{\operatorname{Re}_{0_{e}}}}\right)^{2}}\right] \\
\frac{\left(B.20\right)}{\left(\frac{\operatorname{Re}_{0_{x}}'}{\overline{\operatorname{Re}_{0_{y}}'}} \overline{\operatorname{Re}_{0_{y}}'}\right)} = \frac{1}{2B_{11}B_{21}} \left[\overline{\left(\frac{\operatorname{Re}_{0_{e}}'}{\overline{\operatorname{Re}_{0_{e}}}}\right)^{2}} - B_{11}^{2} \overline{\left(\frac{\operatorname{Re}_{0_{x}}'}{\overline{\operatorname{Re}_{0_{x}}}}\right)^{2}} + B_{21}^{2} \overline{\left(\frac{\operatorname{Re}_{0_{y}}'}{\overline{\operatorname{Re}_{0_{x}}}}\right)^{2}}\right]}$$

$$(B.22)$$

where $D_1 = (B_{21}/B_{11} - B_{22}/B_{12})$ and $D_2 = (B_{11}/B_{21} - B_{12}/B_{22})$. The covariance of the two films can be expressed as

$$\overline{\left(\frac{E_f'}{\overline{E_f}}\right)_1 \left(\frac{E_f'}{\overline{E_f}}\right)_2} = f_1 f_2 \overline{\left(\frac{\operatorname{Re}_{0_e}'}{\overline{\operatorname{Re}_{0_e}}}\right)_1 \left(\frac{\operatorname{Re}_{0_e}'}{\overline{\operatorname{Re}_{0_e}}}\right)_2}$$
(B.23)

For the x-z plane, the above equations are used with w replacing v, and z replacing y. In this case, the cross-film is rotated 90 degrees (i.e. an x-z cross-film is used).

B.2 Turbulence Transformation - Reynolds Shear Stress

Bowersox and Schetz^[15] have shown that the Reynolds shear stress can be expressed in terms of the conservative cross-film variables as

$$\tau_{ij}^{T} = -\frac{\overline{(\rho u_{i})' (\rho u_{j})'}}{\overline{\rho}} + \overline{\rho} \ \overline{u_{i}} \ \overline{u_{j}} \overline{\left(\frac{\rho'}{\overline{\rho}}\right)^{2}}$$

where the second term on the right hand side has been shown to be much less than the first term for thin layer type flows. For the present flowfield, the flow angle was usually less than 5–10°, hence neglecting the second term would have probably been acceptable. In fact, the second term was calculated using the methods of Bowersox^[13] and was determined to be at least least an order of magnitude smaller than the first term for all of the data presented.

Appendix C. Experimental Uncertainty Analysis

Error and uncertainty are inherent to experimental research. This section attempts to identify the possible sources of measurement error in the experiments, and then quantify the effects of these errors on the presented data. Based on the analysis presented by Bowersox in^[14] the Euclidean (L_2) norm is utilized to assess the cumulative effects of error sources. The L_1 norm (a summation of the absolute error values) has been found to be too conservative an estimate when compared to a perturbation analysis of the data reduction equations. The L_2 norm of a set data, x_i , is defined by^[102]

$$||x_i||_2 = ||x_1, x_2, ..., x_n||_2 \equiv \left[\sum_{i=1}^n x_i^2\right]^{\frac{1}{2}}$$
 (C.1)

Thus, the total dimensional error is defined to be^[42]

$$\mathcal{E}_R \equiv \|\mathcal{E}_{x_i}\|_2 = \left[\sum_{i=1}^n \left(\frac{\partial R}{\partial x_1} \mathcal{E}_{x_i}\right)^2\right]^{\frac{1}{2}} \tag{C.2}$$

where the index *i* runs over the various measurement errors, \mathcal{E}_{x_i} , associated with determination of the result, R. The dimensional errors can be normalized by reference values to obtain nondimensional errors (i.e. $\varepsilon_R = \mathcal{E}_R/R$). The effects of measurement errors were propagated through the data reduction process, where the equations were linearized to provide approximate error bounds on the processed data for the experiments.

C.1 Measurement Errors

Every measurement has an associated error. It is assumed all measurement errors are random, with a Gaussian distribution. The assumption of random errors precludes the existence of biased errors or blunders.

C.1.1 Conventional Probes. Pressure was measured by transducers which measure gauge pressure. An error of ± 0.0034 atm was assumed in measurement of ambient pressure, determined by the smallest increment on the barometer.

The pressure transducers used to measure pitot, cone-static and plenum pressure are advertised to have accuracies of 0.5%, 0.5% and 0.4%, respectively. [30] Calibration and digital conversion of the pressure data for storage and processing also adds error. All pressure readings were conditioned the same style of indicator (Endevco 4428A) with a maximum gain error of $\pm 0.5\%$ and gain stability of $\pm 0.2\%$. [31] The probe pressure units were re-zeroed daily, and never deviated more than 0.01psi or 0.1psi for the probe and plenum pressures, respectively. Finally, Volluz [115] reports that turbulence induces about ± 0.0068 atm error for both pitot and cone static probe types.

Using multiple overheat (MOH) hot-film anemometry, the AFIT Mach 3 wind tunnel has been found to have boundary layer total temperature root mean square (RMS) fluctuations of $2.0\%.^{[74, 69]}$ The RMS fluctuations are included as errors in this analysis as they provide a definitive bound of measurement uncertainty from large data samples. The plenum total temperature was observed to vary no more than ± 2.36 K during tunnel runs. The plenum thermocouple and display unit were accurate to within ± 1 K.

The degree of flexing experienced by each type of probe during tunnel operation was determined by aligning two grids onto the Plexiglas plates to measure x and y position. The flex angle and position were then determined as a function of initial measured position, and accurate to within 1° (1.1mm). The measurement of x and y position was accurate to ± 0.5 mm. Without Plexiglas windows on the top and bottom of the tunnel, it was more difficult to determine the z position of each probe. The error in z position was assumed to be twice the measurement error in x or y (1.0mm). An additional error from digitization occurred in the measurement of y position - as y position was recorded using a linear displacement voltage transducer, LDVT. Since the LDVT was sampled with a 12.0V range, the above error in digitization voltage was multiplied by the calibration slope. This manipulation resulted in an error in y position from digitization of ± 0.015 mm. Errors in position were also incurred due to the flexing of the probes during tunnel operation.

C.1.2 Hot-Film Probes. The possibility of measurement error is greatest in the angular rotation of the probe. Since the probes are calibrated at an upstream location then moved to the downstream measurement locations, great efforts were taken to ensure

that the probe remained aligned with the tunnel axis. Probe alignment was "spot checked" where possible by examining the measured flow angularity in the freestream.

Hot-wire measurements have shown 1.0% root mean square fluctuation in voltage for freestream flow. Additionally, a digitization error of ± 0.003 V was accounted for in the 12.0V sampling range. The errors in pressure, temperature, position and voltage have been summarized in Table C.1.

Measured Property, x	Error	
	Mach 2.8	Mach 4.9
\boldsymbol{x}	1.2mm	1.2mm
\overline{y}	0.5mm	0.5mm
z	1.0mm	1.0mm
T_{t1}	2.3%	2.2%
P_{t1}	0.8%	0.7%
P_{t2}	0.9%	0.8%
P_{cs}	3.5%	1.3%
E_{ϵ}	1.0%	

Table C.1 Measurement error bounds.

C.2 Error Propagation

The errors listed in Table C.1 have an influence on all subsequent data reduction. To determine the influence on calculations, the equations used are linearized about freestream conditions.^[44] Tables C.2 and C.3 list the freestream conditions and typical freestream hot-film calibration parameters used in the analysis, as well as to normalize the uncertainty estimates.

C.2.1 Properties Determined with Pressure Probes. The majority of mean flow calculations are based on the local Mach number, where the Mach number is calculated from a curve fit to experimental data (Equations 3.1 and 3.2). As an example of error propagation, the analysis is applied to Equation 3.1 which is of the form

$$\frac{1}{M} = C_0 + C_1 \xi + C_2 \xi^2 + C_3 \xi^3 + C_4 \xi^4 \Rightarrow M = M^2 [C_0 + C_1 \xi + C_2 \xi^2 + C_3 \xi^3 + C_4 \xi^4]$$

Table C.2 Freestream conditions.

Condition	M=2.8 Value	M=4.9 Value
T_{t1}	297K	354K
P_{t1}	$2.085 \mathrm{atm}$	32.0atm
P_{t2}	$0.7175 \mathrm{atm}$	1.86atm
P_{cs}	0.1017	$0.3388 \mathrm{atm}$
ξ	0.1417	0.1725
M	2.80	4.90
γ	1.4	1.4
R_{air}	$287.1 \frac{\text{m}^2}{\text{s}^2 \text{K}}$	$287.1 \frac{\text{m}^2}{\text{s}^2 \text{K}}$
T	114.5K	61.5K
a_{∞}	$214.48\frac{\text{m}}{\text{s}}$	$157.19\frac{\text{m}}{\text{s}}$
P_1	$0.065 \mathrm{atm}$	$0.070 \mathrm{atm}$
$ ho_1$	$0.2432rac{\mathrm{kg}}{\mathrm{m}^3}$	$0.3977 \frac{\text{kg}}{\text{m}^3}$
u	$600.1 \frac{m}{s}$	$766\frac{m}{s}$
$ ho_1 u$	$140.6 rac{ m kg}{ m m^2 s}$	$304.7 \frac{\text{kg}}{\text{m}^2\text{s}}$
Re_{∞}	$1.8 \times 10^6 / \text{m}$	$75 \times 10^6 / \text{m}$

Table C.3 Typical freestream hot-film parameters (M=2.8).

Condition	Value
E_f	5.0V
T_f	700.0K
T_e	$297.0 \mathrm{K}$
R_f	10.0Ω
R_s	50.0Ω
R_L	$\Omega 0.0$
a_k	0.11
b_k	-0.10
d	$5.1 \cdot 10^{-5} \text{m}$
L	$0.001\mathrm{m}$
Re_e	300
Nu(wire)	1.8

Application of Equation C.2 results in the normalized error at Mach 2.8 of

$$\varepsilon_{M} = \frac{\mathcal{E}_{M}}{M} = \|M(C_{1}\xi + 2C_{2}\xi^{2} + 3C_{3}\xi^{3} + 4C_{4}\xi^{4}) \cdot \varepsilon_{\xi}\|_{2} = 0.725\varepsilon_{\xi}$$
 (C.3)

Similarly, Equation 3.2 at Mach 4.9 gives

$$\varepsilon_{\mathbf{M}} = \|\mathbf{M}(C_1 \xi + C_2 \xi) \cdot \varepsilon_{\xi}\|_2 = 0.855 \varepsilon_{\xi} \tag{C.4}$$

The pressure ratio, ξ is the ratio of pressures measured with a 10° or 20° cone-static probe and a pitot probe.

$$\xi = \frac{P_{cs}}{P_{t1}} \Big|_{cs} \cdot \frac{P_{t1}}{P_{t2}} \Big|_{t2} \tag{C.5}$$

Two different plenum pressures $(P_{t1}|_{t2} \text{ and } P_{t1}|_{cs})$ are used to minimize errors caused by differences between the two separate tunnel runs (one for each probe). Since ξ was a combination of pressure measurements, the errors combine with the Euclidean norm

$$\varepsilon_{\xi} = \|2\varepsilon_{P_{t1}}, \varepsilon_{P_{t2}}, \varepsilon_{P_{cs}}\|_{2} \tag{C.6}$$

The Mach number and plenum temperature were used to derive the local tunnel temperature, T_1 , assuming isentropic flow. Although isentropic flow was violated by shocks, no method for measuring local temperature was available. The equation of state and ideal gas laws were then used to calculate density and speed. Table C.4 summarizes the propagation errors of the pressure probe measurements.

C.2.2 Properties Determined with Hot-film Measurements. Single overheat (SOH) hot-film anemometry was used to measure mass-flux mean flow and RMS fluctuations. SOH analysis assumes negligible total temperature fluctuations and has proved to be valid for this experimental facility. [74, 26] Additionally, cross-wire measurements provided flow direction information. A detailed explanation of the hot-film data reduction techniques which were used is presented in Appendix B. Due to the complicated nature of the hot-film data reduction, a logarithmic/derivative technique [44] was applied to the hot-film data reduction equations to estimate the propagation of errors throughout the hot-film analysis.

Table C.4 Pressure probe related error bounds.

Calculated	Derivation		Error	
Property	M=2.8	M=4.9	M = 2.8	M = 4.9
ξ	$ 2\varepsilon_{P_{t1}}, \varepsilon_{P_{t2}}, \varepsilon_{P_{cs}} _2$	$\ 2\varepsilon_{P_{t1}}, \varepsilon_{P_{t2}}, \varepsilon_{P_{cs}}\ _2$	3.9%	2.0%
M	$0.725arepsilon_{\xi}$	$0.855arepsilon_{m{\xi}}$	2.8%	1.7%
T_1	$\ \varepsilon_{T_{t1}}, 1.221\varepsilon_{\mathrm{M}}\ _{2}$	$\ arepsilon_{T_{t1}}, 1.655arepsilon_{\mathbf{M}}\ _{2}$	4.1%	3.6%
a	$0.5arepsilon_{T_1}$	$0.5arepsilon_{T_1}$	2.1%	1.8%
P_1	$\ \varepsilon_{P_12}, 1.907\varepsilon_{\mathbf{M}}\ _2$	$\ arepsilon_{P_12}, 1.970arepsilon_{\mathbf{M}}\ _2$	5.5%	3.5%
$ ho_1$	$\ arepsilon_{P_1},arepsilon_{T_1}\ _2$	$\ arepsilon_{P_1},arepsilon_{T_1}\ _2$	6.9%	5.0%
u	$ arepsilon_{ m M},arepsilon_{lpha} _{2}$	$\ arepsilon_{ ext{M}}, arepsilon_{lpha}\ _{2}$	3.5%	2.5%

The Nusselt number (of the hot-film), Nu, was determined from the power consumption required to maintain a constant wire temperature (Equation B.6). The error in Nu was a function of the measured voltage error and total temperature error. The effective Reynolds number, Re_e , was determined by a curve fit of Nu (King's Law, Equation 3.3). Additionally, the fluctuation in Re_e was a function of measured voltage error. These errors were combined under the L_2 norm. The error in mass-flux is equivalent to the error in Reynolds number, and it is assumes that the transverse mass-fluxes suffer the same error as the axial component. Table C.5 summarizes the propagation errors of the hot-film probe measurements.

C.2.3 Separation of Primitive Fluctuations. The separation equations for the primitive fluctuations were linearized about the reference conditions of Table C.2. The results of variable separation error analysis are summarized in Table C.6.

C.3 Comparison of u-v and u-w Hot-film Probes

The agreement between the axial mean and fluctuating quantities obtained by the two probes was considered excellent (Figure C.1). The small differences were attributed primarily to the high flow angles ($\phi \approx \pm 10^{\circ}$) experienced by the probes which have finite (1mm) wire separations.

Table C.5 Hot-film related error bounds (M=2.8).

Calculated Property	Derivation	Error
Nu	$\ 2.0arepsilon_{E_f},arepsilon_{T_{t1}}\ _2$	3.0%
Re_e	$\ 2.0arepsilon_{\mathrm{Nu}},arepsilon_{E_f}\ _2$	6.1%
f	$0.5arepsilon_{\mathrm{Re_e}}$	3.1%
g	$\ arepsilon_{T_{t1}},arepsilon_f\ _2$	3.8%
$\frac{\operatorname{Re}_e^2}{\operatorname{Re}_x^2}$	$2.0arepsilon_{\mathrm{Re}_{e}}$	12.2%
Re_x^2	$\ arepsilon_{\mathrm{Re}_{oldsymbol{e}_1}^2}, arepsilon_{\mathrm{Re}_{oldsymbol{e}_1}^2, \mathrm{Re}_{oldsymbol{e}_2}^2}, arepsilon_{\mathrm{Re}_{oldsymbol{e}_2}^2}\ _2$	21.2%
$\mathrm{Re}_x\mathrm{Re}_y$	$arepsilon_{\mathrm{Re}_x^2}$	21.2%
$\mathrm{Re}_x\mathrm{Re}_z$	$arepsilon_{\mathrm{Re}_x^2}$	21.2%
Re_x	$0.5arepsilon_{\mathrm{Re}_x^2}$.	10.6%
Re_y	$arepsilon_{\mathrm{Re}_x}$	10.6%
Re_z	$arepsilon_{\mathrm{Re}_{m{x}}}$	10.6%
ho u	$arepsilon_{\mathrm{Re}_x}$	10.6%
ho v	$arepsilon_{\mathrm{Re}_{oldsymbol{y}}}$	10.6%
ho w	$arepsilon_{\mathrm{Re}_z}$	10.6%

Table C.6 Turbulent fluctuation error bounds (M=2.8).

Calculated Property	Derivation	Error
$(\rho u)'$	$arepsilon_{\mathrm{Re}_x}$	$\boxed{10.6\%}$
$(\rho v)'$	$arepsilon_{\mathrm{Re}_{m{y}}}$	10.6%
$(\rho w)'$	$arepsilon_{\mathrm{Re}_z}$	10.6%
$(\rho u)'(\rho v)'$	$arepsilon_{\mathrm{Re_xRe_y}}$	21.2%
$(\rho u)'(\rho w)'$	$arepsilon_{\mathrm{Re_xRe_z}}$	21.2%
ho'	$\ 0.458arepsilon_{ ext{M}}, 0.771arepsilon_{(ho u)'}\ _{2}$	8.3%
u'	$\ arepsilon_{ ho'},arepsilon_{(ho u)'}\ _2$	13.4%
v'	$arepsilon_{u'}$	13.4%
w'	$arepsilon_{u'}$	13.4%

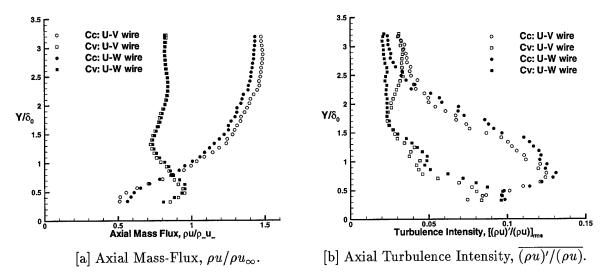


Figure C.1 Comparison of hot-wire probe orientation at x=0.69c (M=2.8).

C.4 Assessment of Probe Location Error Using Numerical Solutions

The effects of probe location error were also assessed by 'probing' the computational results. By assuming a location error, then examining the CFD results at the extremes of that error band, an estimate of the sensitivity of measured flowfield variables to probe location error may be ascertained. Figure C.2 shows the effect that a ± 1 mm probe location error in the x and z directions (in the numerical solution) has on the measured pitot pressure. Due to the high transverse pressure gradients, the measured data is more sensitive to variations in z (with measurement errors of up to 8.5%). than it is to x (up to 5.5% on the concave side). In reality, it is likely that the probe experiences less flexing as it is moved away from the model wall. If this is true, Δx becomes less positive as Y/δ increases, and a profile more closely resembling the experimentally observed data (without the acceleration peak over $Y/\delta \epsilon [0.8,1.8]$) could result on the concave side of the fin. The measured data on the convex side would be relatively unaffected as it is comparatively invariant with Δx .

Many of the differences between measured and predicted flow angularity may also be attributed to probe location errors. Figures C.3 through C.6 show the effects of a ± 1 mm probe location error in the x and z directions on the calculated flow angularities. For example, at a location only 1mm closer to the fin than estimated on the convex side, the numerical simulation almost exactly reproduces the experimentally observed flattening of the

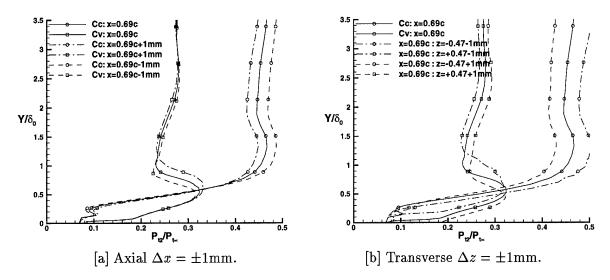


Figure C.2 Effect of a variation in probe position on computed pitot pressure (M=2.8).

horizontal angularity, θ , near the body (0.3<Y/ $\delta_0<$ 0.8) (cf Figures 5.8[c] and C.3[b]). At this same location, the experimentally observed inflection seen in the azimuthal flow angle, ϕ , is also very closely reproduced in the numerical solution (cf Figures 5.8[d] and C.4[b]).

On the concave side of the fin, moving the probe location 1mm further away from the fin (in the numerical solution) yields the drastic reduction in the horizontal flow angularity, θ , near the body $(Y/\delta_0<0.7)$ similar to that observed in the experiment (cf Figures 5.9[c] and C.5[b]). The sensitivity of θ to probe location error in the z direction in this region $(z/c\approx-.47)$ can also be Figure 5.11[a]. Near the body, the flow can be directed either toward or away from the body with a small variation in z.

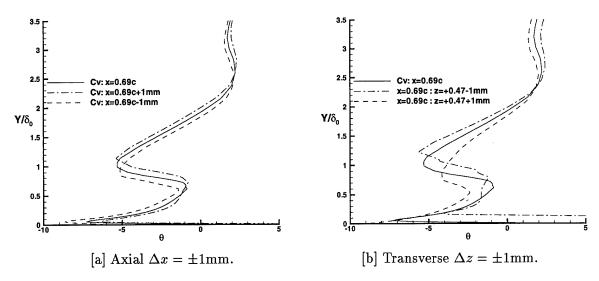


Figure C.3 Effect of a variation in probe position on θ ; convex side (M=2.8).

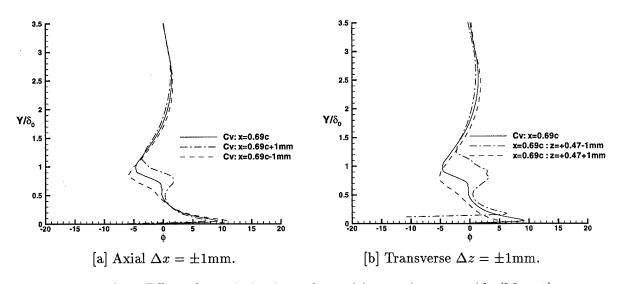


Figure C.4 Effect of a variation in probe position on ϕ ; convex side (M=2.8).

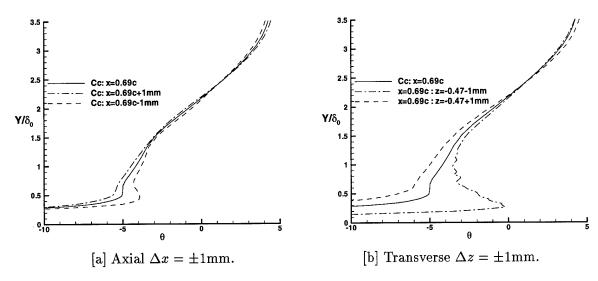


Figure C.5 Effect of a variation in probe position on θ ; concave side (M=2.8).

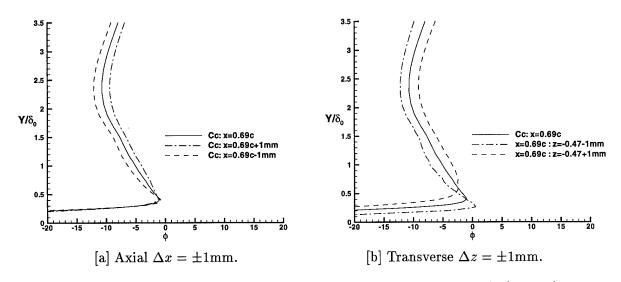


Figure C.6 Effect of a variation in probe position on ϕ ; concave side (M=2.8).

Appendix D. Mach 5 Wind Tunnel

D.1 Overview

The AFIT Mach 5 wind tunnel is a blow-down design (as illustrated in Figure D.1) which operates over a range of Reynolds numbers. Since the static temperature for Mach 5 air at standard day total temperature is below the liquefaction temperature of oxygen, the air is heated by a refractive pebble-bed heating system. The nominal chamber total pressure and temperature are 20-32 atm and 350-375K respectively, yielding a freestream Reynolds number $Re/\ell \approx 32-75 \times 10^6 m^{-1}$. The nominal tunnel conditions experienced in the tunnel for the present research are shown in Table D.1. Although the tunnel is capable of sustaining higher run times, it is typically run for only 10-15 seconds. The design, construction, and instrumentation of this facility comprised a significant portion of this research effort.

D.2 Air Supply

High pressure air is stored in a 175atm tank (Figure D.2) having a capacity of 1.25 cubic meters, and is controlled with a high volume dome regulated control valve (Figure D.3). The tank is recharged with a four-stage compressor and dryer system (Figure D.4). This system provides enough air to run the tunnel at a plenum pressure of 20atm for over 2 minutes, and requires about 5 hours to re-charge, although actual run-times are never expected to exceed 30 seconds so as to allow several runs during a day.

Table D.1 Typical Mach 5 tunnel freestream conditions (used for viscous CFD).

Condition	Value
M	4.87
P_t	$3.23 \times 10^6 \text{Pa} = 32.0 \text{atm}$
P	7.017 kPa = 0.070 atm
T_t	354K
T	61.5K
u	$766\frac{m}{s}$
ρ	$0.3977 \frac{\text{kg}}{\text{m}^3}$

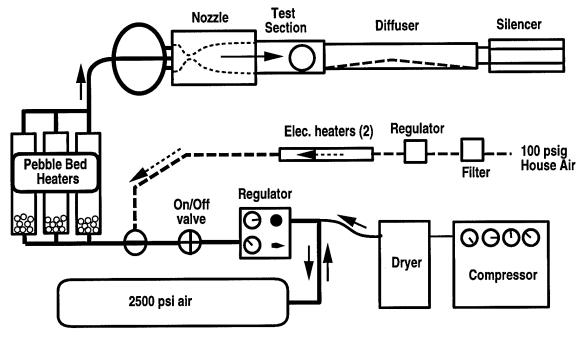


Figure D.1 Mach 5 wind tunnel schematic.

In the present configuration, both the run time and down time are are determined by the heating system. The system passes the high-pressure air through a bank of refractory pebble-bed heaters (Figure D.5) before it enters the tunnel. To accomplish the heater design, computer programs (both FORTRAN and Mathcad) were developed which implement the heater design method of Pope and Goin. [86] Each of the pebble beds are designed to heat the air to 375K before entering the tunnel, which keeps the static temperature in the tunnel well above the liquefaction temperature. This temperature can be maintained or exceeded for several seconds, and is monitored by a thermocouple in the settling chamber. The air can easily be heated to higher or lower temperatures by heating the pebble beds to other initial temperatures. The heater system is designed to be very flexible, allowing the use of single or multiple heaters during a run. This is accomplished by channeling the air from the heaters through a manifold before entering the tunnel, which allows them to be run independently or in parallel. In practice, two heaters are usually run in parallel, providing enough heat for three runs, each sustaining acceptable temperatures for 8-12 seconds of 10-15 second runs.

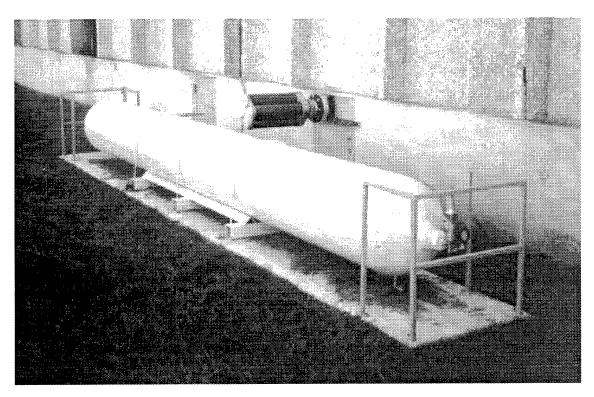
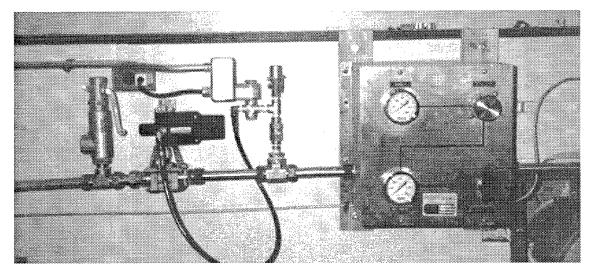
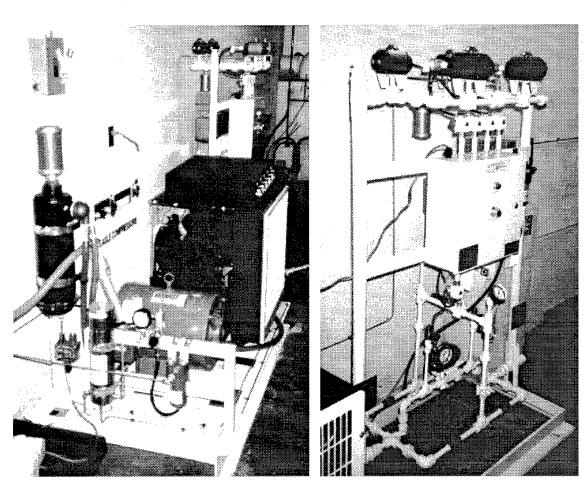


Figure D.2 High pressure air tank.



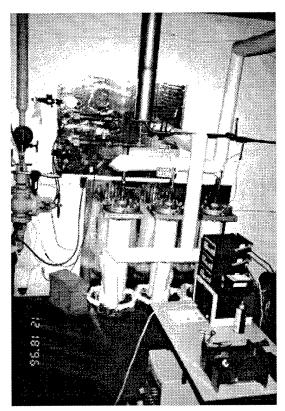
Style:	High Volume / Dome Regulated 204atm
Regulator:	Grove Powreactor Dome Regulator #200/300
Manufacturer:	Eagle Compressors Inc.,
	Pleasant Garden, NC
Model:	A.C.P. Custom Air Control Panel #G07C0177

Figure D.3 Air control panel.



Style:	air cooled four stage compressor
Power:	30kW
Separator:	mechanical
Dryer:	regenerative
Delivery:	1m ³ /min @ 41atm (free air delivery)
Manufacturer:	Eagle Compressors Inc.,
	Pleasant Garden, NC
Model:	HORIZONTAL 4S50 MKII #HW40HH3

Figure D.4 Compressor and dryer.



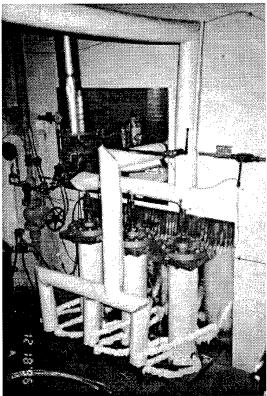


Figure D.5 Mach 5 wind tunnel pebble bed heating system.

The heaters are re-heated by convection with two heavy-duty electric air heaters (Reheat Co. Inc. Model HDA-2-12-2). These heaters each produce a minimum 1.5kW when powered by standard 240 Volt outlets. With both electric heaters in operation, it takes approximately one hour to re-heat each pebble-bed heater from an end-of-run temperature back to operating temperature.

D.3 Nozzle & Test Section

The nozzle profile was designed using the method of characteristics with modifications for viscous effects. The test section of the wind tunnel has cross-sectional dimensions of 7.62cm \times 7.62cm and a length of 26.67cm. The test section and nozzle (Figures D.6 and D.7) are milled from 347 stainless steel. The test section side walls are fitted with optical grade glass windows to allow for photographic visualization of the flow (Figure D.8). The tunnel ceiling (Figure D.9) is designed to accept the WAF model, and the floor (Figure D.10) is fitted with slots for probe insertion.

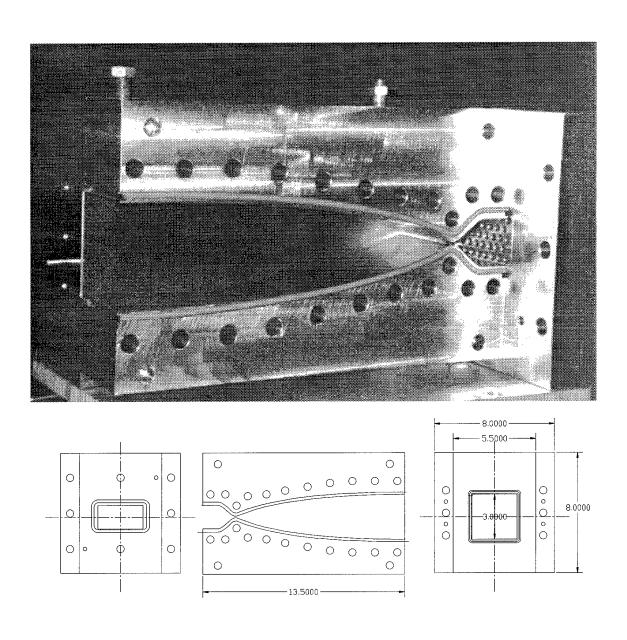


Figure D.6 Wind tunnel nozzle (dimensions in inches).

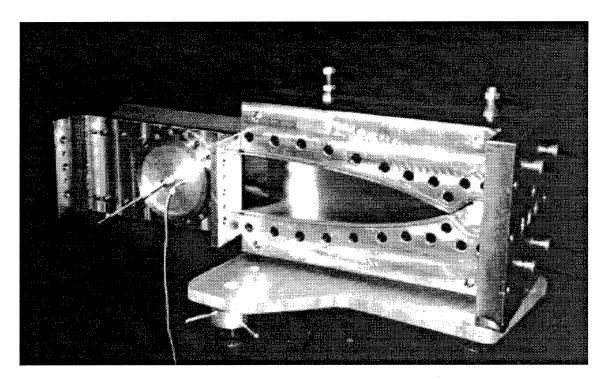


Figure D.7 Wind tunnel nozzle and test section. Shown with nozzle wall removed for visibility and window replaced by aluminum plug for initial tunnel calibration.

D.4 Diffuser & Silencer

An adjustable throat-area diffuser was employed, allowing it to be tuned for optimal performance after the tunnel was assembled. A sound muffler (seen in Figure D.2) which is attached directly to the the diffuser exit directs the air back outside the building.

D.5 Plenum Chamber Instrumentation

Instrumentation for the tunnel conditions include an upstream pitot tube and thermocouple well ahead of the throat to measure $P_{t\infty}$ and $T_{t\infty}$. A 34atm Endevco pressure transducer was used to sense plenum pressure, which is displayed and digitized by an Endevco (model 4428A) signal conditioner. Plenum temperature is sensed with an Omega K-type (model KAIN-18-U-12) lance thermocouple, then displayed on an Omega model DP41-TC-A temperature display. This temperature data was used in the data reduction as well as to ensure that the air had been adequately heated. Pressure and temperature is sent to the data acquisition unit (Section 3.6).

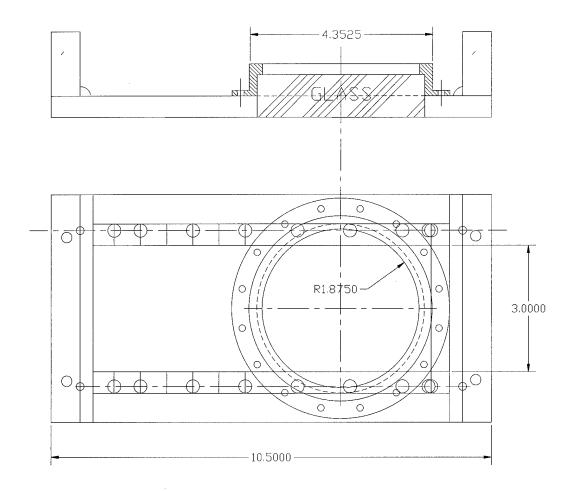
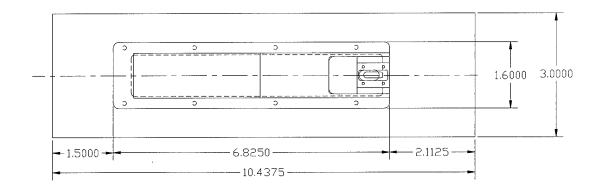


Figure D.8 Wind tunnel test section wall with windows (dimensions in inches).

D.6 TSI 3-DOF Traverse System

A TSI 3-DOF traverse system was used for the Mach 5 experiments. Although this traverse was equipped with its own manual control center, safety concerns dictated that the traverse be controlled from a remote location during tunnel operation. The control software also provides the ability to move specific distances at prescribed speeds.



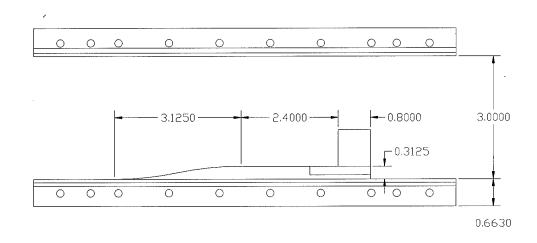


Figure D.9 Wind tunnel ceiling with model insert (dimensions in inches).

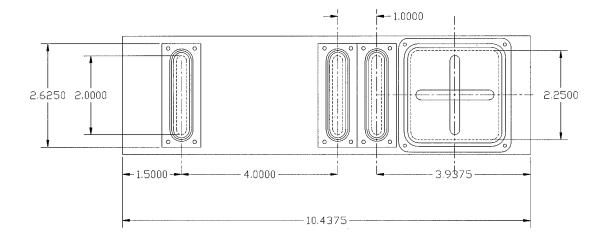


Figure D.10 Wind tunnel floor with probe access (dimensions in inches).

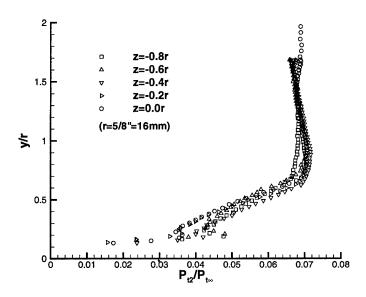


Figure D.11 Measured pitot pressure at upstream location.

D.7 Tunnel Calibration

When operated near the conditions given in Table D.1, the tunnel flow is very twodimensional over a significant portion of the tunnel width. This is demonstrated in Figure D.11 which shows pitot pressures measured at an upstream (x=-9.64r=-7.53c) location over a range of span-wise locations.

D.8 Numerical Validation

The AFIT Mach 5 wind tunnel was simulated numerically to provide some reassurance of the tunnel design, as well as to gain some early experience with the methods used for the wrap-around fin simulations. The simulations were conducted using the General Aerodynamic Simulation Program (GASP) Version 2.0^[72]. The computational requirements of these simulations were also used to estimate the computational requirements of the WAF simulations presented in this document. Several 2-D and 3-D solutions were obtained, the details of which were reported in the Prospectus for this research.^[107]

Appendix E. GASP Input Deck for M=2.8 Viscous Simulation

The GASP input deck (version 3.0) for the viscous simulation at Mach 2.8 discussed in Chapter IV is presented below. As discussed in Chapter IV, a 2-Dimensional inflow boundary condition (shown in Figure E.1) is specified on the upstream edge of the first zone. Parallel flow and constant pressure through the boundary layer was assumed. This two-dimensional PNS region allowed the boundary layer to develop into a fully turbulent profile (also shown in Figure E.1) upstream of the blended body region.

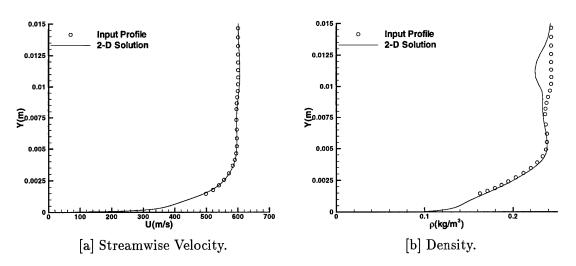


Figure E.1 Space marched zone inflow boundary condition for and exit.

GASP Input Deck: Mach 3 WAF Simulation with Experimental Upstream BC FILE INFO chemModPath gridDir solutionDir bcDir '../../database/db1.bin' '.' gridFileMode solnFileMode bcFileMode **GENERAL INFO** iunits rhoNDim vNDim tNDim **lNDim** pGauge 1 2.039000e-01 6.070000e+02 1.096000e+02 1.000000e+00 0.000000e+00 residmode irest initByZone memoryMode cpumode 1 2 1 nZone nZonalBoun nPartStyle nPhysMod nBlock iBlkStt iBlkEnd 12 3 8 ZONE INFO

```
ZONE #1: 2D -- Rectangular Part of Test Section (half)
  Initial Conditions
  initPhysMod
      1
  Boundary Conditions
  nSurfTypes i0 id j0 jd k0 kd
             -2 -3 10 -3 -19 -3
   twall
             pback
  294.00
              1.431
Mesh Sequencing
  nSeqLevel
     3
   seqNum
            initSolFile intrpQ ilev jlev klev
               0
                          0
                                       1
                                            1
     1
                                 1
     2
                0
                           0
                0
                           0
     3
                                 1
                                       1
                                             1
ZONE #2: Blend from Flat Plate to Cyl Body (half)
  Initial Conditions
  initPhysMod
      1
  Boundary Conditions
  nSurfTypes i0 id j0 jd k0 kd
             -20 -3 10 -3 -19 -3
     6
            pback
   twall
  294.00
              1.431
Mesh Sequencing
  nSeqLevel
     3
   seqNum
            initSolFile
                         intrpQ ilev jlev klev
                           0
     1
                0
                                 1
                                      1
                                              1
     2
                0
                           0
                                  1
                                       1
     3
                           0
                                  1
                                        1
ZONE #3: Cylinderical Body
  Initial Conditions
  initPhysMod
      1
  Boundary Conditions
  nSurfTypes i0 id j0 jd k0 kd
             -20 -3 10 -3 -3 -3
     6
             pback
   twall
  294.00
              1.431
Mesh Sequencing
  nSeqLevel
     3
   seqNum
            initSolFile
                         intrpQ ilev
                                       jlev klev
                                     1 1
     1
                0
                          0
                                 1
                                 1
     2
                0
                           0
                                       1
     3
                0
```

1

1

0

```
ZONE #4: Blend to fin
  Initial Conditions
  initPhysMod
       1
  Boundary Conditions
  nSurfTypes i0 id j0 jd k0 kd
              -20 -3 10 -3 -3 -3
      6
   twall
              pback
  294.00
               1.431
Mesh Sequencing
  nSeqLevel
     3
   seqNum
             initSolFile intrpQ ilev
                                         jlev klev
                 0
                          0
                                  1
                                         1
                                                 1
                 0
                             0
                                    1
                                                 1
      2
                                          1
      3
                 0
                             0
                                    1
ZONE #5: Quadrant I -- ahead of fin
  Initial Conditions
  initPhysMod
       3
  Boundary Conditions
  nSurfTypes i0 id j0 jd k0 kd
              -20 -20 -20 -3 -20 -3
   twall
             pback
               1.431
  294.00
Mesh Sequencing
  nSeqLevel
      3
   seqNum
             initSolFile
                          intrpQ ilev
                                         jlev klev
      1
                 1
                             0
                                   1
                                         1
                                                 1
                                    2
                                                 2
      2
                 1
                             0
                                          2
      3
                 1
                             0
                                                 4
ZONE #6: Quadrant II -- ahead of fin
  Initial Conditions
  initPhysMod
       3
  Boundary Conditions
  nSurfTypes i0 id j0 jd k0 kd
      6
              -20 -20 -20 -3 -3 -20
   twall
              pback
  294.00
               1.431
Mesh Sequencing
  nSeqLevel
      3
   seqNum
             initSolFile
                          intrpQ
                                  ilev
                                         jlev
                                              klev
     1
                 1
                           0
                                   1
                                         1
                                                 1
      2
                 1
                             0
                                   2
                                          2
                                                 2
```

3

0

```
ZONE #7: Fin region - Quadrant I
  Initial Conditions
  initPhysMod
  Boundary Conditions
  nSurfTypes i0 id j0 jd k0 kd
              -20 -3 -20 -3 -20 -3
   twall
              pback
  294.00
               1.431
Mesh Sequencing
  nSeqLevel
      3
   seqNum
             initSolFile intrpQ ilev
                                        jlev klev
                                                 1
                1
                           0
                                  1
      1
                                                 2
                             0
                                    2
                                          2
      2
                 1
      3
                 1
                             0
                                    4
ZONE #8: Fin region - Quadrant II
  Initial Conditions
  initPhysMod
       3
  Boundary Conditions
  nSurfTypes i0 id j0 jd k0 kd
      6
              -20 -3 -20 -3 -3 -20
             pback
   twall
               1.431
  294.00
Mesh Sequencing
  nSeqLevel
      3
   seqNum
             initSolFile
                          intrpQ
                                  ilev
                                         jlev klev
                             0
                                  1
                                         1
                                                 1
                 1
      1
                                    2
                             0
                                          2
      2
                 1
                             0
                                    4
                                                 4
      3
                  1
ZONE #9: Fin region - Quadrant III
  Initial Conditions
   initPhysMod
       3
  Boundary Conditions
  nSurfTypes i0 id j0 jd k0 kd
              -20 -3 10 -20 -3 0
      6
              pback
   twall
                1.431
   294.00
Mesh Sequencing
  nSeqLevel
      3
   seqNum
             initSolFile
                           intrpQ
                                   ilev
                                         jlev
                                               klev
      1
                 1
                             0
                                    1
                                         1
                                                1
                             0
                                    2
                                          2
                                                 2
      2
                  1
                 1
                             0
      3
```

```
ZONE #10: Fin region - Quadrant IV
  Initial Conditions
  initPhysMod
  Boundary Conditions
  nSurfTypes i0 id j0 jd k0 kd
             -20 -3 10 -20 0 -3
   twall
             pback
  294.00
               1.431
Mesh Sequencing
  nSeqLevel
     3
   seqNum
            initSolFile intrpQ ilev jlev klev
                          0
                                  1
     1
                 1
                                   2
                                               2
      2
                 1
                            0
                                         2
      3
                 1
                            0
                                   4
ZONE #11: fin tip to top wall
  Initial Conditions
  initPhysMod
      3
  Boundary Conditions
  nSurfTypes i0 id j0 jd k0 kd
             -20 -3 10 -3 -20 -20
      6
             pback
   twall
  294.00
              1.431
Mesh Sequencing
  nSeqLevel
     3
   seqNum
            initSolFile
                          intrpQ ilev
                                       jlev klev
                            0
                                  1
                                        1
                                               1
     1
               1
                                   2
                                               2
      2
                 1
                            0
                                         2
                 1
                            0
                                   4
                                               4
      3
ZONE #12: fin tip to side wall
  Initial Conditions
  initPhysMod
      3
  Boundary Conditions
  nSurfTypes i0 id j0 jd k0 kd
             -20 -3 -3 10 -20 -20
      6
             pback
   twall
               1.431
  294.00
Mesh Sequencing
  nSeqLevel
      3
                                  ilev
   seqNum
             initSolFile
                          intrpQ
                                        jlev klev
      1
                 1
                            0
                                   1
                                        1
                                              1
                                  2
                                        2
                                               2
      2
                            0
                 1
                            0
                                  4
      3
```

ZONAL BOUN INFO

```
ZONAL BOUNDARY #1: -- straight test sect to body blend
izbpass zbType zbFluxCrct 2 1 0
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
1 2 2 1 136 3 1 1
neqn zbmap(1:neqn)
       1 2 3 4 5
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
2 1
         2 1 136 3 1 96
neqn zbmap(1:neqn)
5 1 2 3 4 5
ZONAL BOUNDARY #2: -- body blend to cyl body -- Quad I & IV
izbpass zbType zbFluxCrct
               0
2
       0
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
        2 1 136 3 1 96
neqn zbmap(1:neqn) 5 1 2 3 4 5
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
3 1 2
              1 136 3 97
neqn zbmap(1:neqn)
       1 2 3 4 5
ZONAL BOUNDARY #3: -- body blend to cyl body -- Quad II & III
izbpass zbType zbFluxCrct 2 0 0
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
2 2 2 1 136 3 1 96
neqn zbmap(1:neqn)
       1 2 3 4 5
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
3 1
        2 1 136 3 96 1
neqn zbmap(1:neqn)
       1 2 3 -4 5 (NOTE: zbmab2 -4 requires GASP mod.)
ZONAL BOUNDARY #4: -- cyl body to body-to-fin transition zone
izbpass zbType zbFluxCrct
       0
               0
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
3 2
        2 1 136 3 1 192
neqn zbmap(1:neqn)
5 1 2 3 4 5
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
4 1 2 1 136 3 1 192
neqn zbmap(1:neqn)
       1 2 3 4 5
```

```
ZONAL BOUNDARY #5: -- Quadrant I of Zone 4 to Zone 5
izbpass zbType zbFluxCrct
      1
              0
 2
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
4 2 2 97 136 3 97 192
neqn zbmap(1:neqn)
    1 2 3 4 5
5
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
5 1 2 1 40 3 1 96
neqn zbmap(1:neqn)
      1 2 3 4 5
5
ZONAL BOUNDARY #6: -- Quadrant II of Zone 4 to Zone 6
izbpass zbType zbFluxCrct
2 1 0
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
4 2 2 97 136 3 1 96
neqn zbmap(1:neqn)
      1 2 3 4 5
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
6 1 2 1 40 3 1 96
neqn zbmap(1:neqn) 5 1 2 3 4 5
ZONAL BOUNDARY #7: -- Quadrant III of Zone 4 to Zone 9
izbpass zbType zbFluxCrct
2
      1
              0
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
4 2 2 1 96 3 1 96
neqn zbmap(1:neqn)
5 1 2 3 4 5
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
9 1 2 1 96 3 1 96
neqn zbmap(1:neqn)
       1 2 3 4 5
ZONAL BOUNDARY #8: -- Quadrant IV of Zone 4 to Zone 10
izbpass zbType zbFluxCrct 2 1 0
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
4 2 2 1 96 3 97 192
neqn zbmap(1:neqn)
      1 2 3 4 5
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
10 1 2 1 96 3 1 96
neqn zbmap(1:neqn) 5 1 2 3 4 5
_____
ZONAL BOUNDARY #9: -- Zone 5 to Zone 6
izbpass zbType zbFluxCrct 0 0 0
```

```
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
5 \qquad 5 \qquad \qquad 1 \qquad \qquad 1 \qquad \qquad 72 \qquad \qquad 2 \qquad \qquad 1 \qquad \qquad 40
neqn zbmap(1:neqn)
5 1 2 3 4 5
        1 2 3 4 5
5
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
6 6 1 1 72 2 1 40
neqn zbmap(1:neqn)
5
        1 2 3 4 5
ZONAL BOUNDARY #10: -- Zone 6 to top of front of Zone 9
izbpass zbType zbFluxCrct
        0
                 0
0
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
6 3 1 1 72 3 1 96
neqn zbmap(1:neqn) 5 1 2 3 4 5
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
9 4 1 1 72 3 1 96
neqn zbmap(1:neqn) 5 1 2 3 4 5
ZONAL BOUNDARY #11: -- Zone 9 to Zone 10 (extends forward from 1.e.)
izbpass zbType zbFluxCrct 0 0 0
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
10 5 1 1 72 2 1 96
neqn zbmap(1:neqn) 5 1 2 3 4 5
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
9 6 1 1 72 2 1 96
neqn zbmap(1:neqn) 5 1 2 3 4 5
ZONAL BOUNDARY #12: -- Zone 5 to top of front of Zone 10
izbpass zbType zbFluxCrct 0 0 0
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
5 3 1 1 72 3 1 96
neqn zbmap(1:neqn)
5 1 2 3 4 5
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
10 4 1 1 72 3 1 96
neqn zbmap(1:neqn)
5 1 2 3 4 5
        1 2 3 4 5
ZONAL BOUNDARY #13: -- Zone 5 to Zone 7
izbpass zbType zbFluxCrct 0 0 0
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
5 2 2 1 40 3 1 96
neqn
     zbmap(1:neqn)
```

```
1 2 3 4 5
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
7 1 2 1 40 3 1 96
neqn zbmap(1:neqn)
5 1 2 3 4 5
ZONAL BOUNDARY #14: -- Zone 6 to Zone 8
izbpass zbType zbFluxCrct 0 0 0
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
6 2 2 1 40 3 1 96
neqn zbmap(1:neqn)
5 1 2 3 4 5
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
8 1 2 1 40 3 1 96
neqn zbmap(1:neqn)
       1 2 3 4 5
             _____
ZONAL BOUNDARY #15: -- Zone 7 to back of Zone 10
izbpass zbType zbFluxCrct
    0     0     0
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
7 3 1 1 84 3 1 96
neqn zbmap(1:neqn)
5 1 2 3 4 5
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
10 4 1 73 156 3 1 96
neqn zbmap(1:neqn)
5 1 2 3 4 5
       1 2 3 4 5
ZONAL BOUNDARY #16: -- (Q1) to Fin-to-Top Zone -- LE
izbpass zbType zbFluxCrct 0 0 0
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
7 5 1 1 20 2 1 40
neqn zbmap(1:neqn)
5 1 2 3 4 5
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
11 1 3 1 20 2 1 40
neqn zbmap(1:neqn)
       1 2 3 4 5
5
______
ZONAL BOUNDARY #17: -- (Q1) to Fin-to-Top Zone -- Side
izbpass zbType zbFluxCrct
    0     0     0
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
7 5 1 21 84 2 1 40
neqn zbmap(1:neqn)
5 1 2 3 4 5
       1 2 3 4 5
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
11 6 1 1 64 2 1 40
```

```
neqn zbmap(1:neqn) 5 1 2 3 4 5
_____
ZONAL BOUNDARY #18: -- (Q2) to Fin-to-Top Zone
izbpass zbType zbFluxCrct 0 0 0
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
8 6 1 1 64 2 1 40
neqn zbmap(1:neqn) 5 1 2 3 4 5
       1 2 3 4 5
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
11 5 1 1 64 2 1 40 neqn zbmap(1:neqn)
5 1 2 3 4 5
ZONAL BOUNDARY #19: -- (Q3) to Fin-to-Side Zone -- LE
izbpass zbType zbFluxCrct 0 0 0
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
        1 73 92 3 1 96
neqn zbmap(1:neqn) 5 1 2 3 4 5
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
12 1 3 1 20 2 1 96
neqn zbmap(1:neqn)
        1 2 3 4 5
5
              _____
ZONAL BOUNDARY #20: -- (Q3) to Fin-to-Side Zone -- Side
izbpass zbType zbFluxCrct 0 0 0
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
9 4 1 93 156 3 1 96
neqn zbmap(1:neqn)
5 1 2 3 4 5
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
12 6 1 1 64 2 1 96
neqn zbmap(1:neqn)
5 1 2 3 4 5
ZONAL BOUNDARY #21: -- (Q2) to Fin-to-Side Zone
izbpass zbType zbFluxCrct
0 0 0
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
8 3 1 1 64 3 1 96
neqn zbmap(1:neqn)
5 1 2 3 4 5
nz zbface zbdir1 zbstt1 zbend1 zbdir2 zbstt2 zbend2
12 5 1 1 64 2 1 96
neqn zbmap(1:neqn)
5 1 2 3 4 5
 5
       1 2 3 4 5
```

PARTITION STYLES

```
PARTITION STYLE #1:
nDir
dir numPart
1
******************
              PHYSICAL MODELING INFO
********************
PHYSICAL MODEL #1: PNS x-marching, Viscous - B-L
            CHEMISTRY & THERMODYNAMICS
nspec nnev prefDiss vibRelax itherm
                                 chemmod
 1 0 0 0 4 'Perfect Gas' 1
                INVISCID FLUXES
imarch
 1
invflxi invflxj invflxk
      3
             3
4
rkapi rkapj rkapk
                   sdm2 sdm4
-1.0000 0.3333 0.3333 0.0000 0.0000
limi limj limk rk_ven
 2 2
         2 1.000
                VISCOUS FLUXES
isViscous
 2
visflxi visflxj visflxk
0 -1 -1
modlmu modlk imodld ivac
     2 1 2
prt scl sct
prl
0.72 0.90 1.00 0.50
ikeps kemin wallfunc igb
     0
           0
                  0
             INITIAL CONDITIONS
icond
 2
Vel/Mach cx cy cz temp/press turbi tkelref
2.9 1 0 0 109.6 0.01 0.001
rho_spec
0.2039
```

REFERENCE STATE FOR B.C.'s

```
icond
 2
Vel/Mach cx cy cz temp/press turbi tkelref 2.9 1 0 0 109.6 0.01 0.001
rho_spec
0.2039
********************
PHYSICAL MODEL #2: RANS, Viscous - Laminar, 3rd order
_____
            CHEMISTRY & THERMODYNAMICS
nspec nnev prefDiss vibRelax itherm chemmod
                                            ieq
 1 0 0 0 4 'Perfect Gas' 1
                INVISCID FLUXES
imarch
 0
invflxi invflxj invflxk
             2
 2
       2
rkapi rkapj rkapk sdm2 sdm4
0.3333  0.3333  0.0000  0.0000
limi limj limk rk_ven
 2 2 2 1.000
                VISCOUS FLUXES
isViscous
visflxi visflxj visflxk
 -1 -1 -1
modlmu modlk imodld ivac
2 2 1 2
prl
     prt scl
                 sct
0.72 0.90 1.00 0.50
ikeps kemin wallfunc igb
 0 0 0 0
             INITIAL CONDITIONS
icond
 2
Vel/Mach cx cy cz temp/press turbi tkelref
2.9 1 0 0 109.6 0.01 0.001
rho_spec
0.2039
            REFERENCE STATE FOR B.C.'s
```

icond

```
Vel/Mach cx cy cz temp/press turbi tkelref
               0 0 109.6 0.01 0.001
   2.9
         1
rho_spec
0.2039
********************
PHYSICAL MODEL #3: RANS, Viscous - B-L, 3rd order
             CHEMISTRY & THERMODYNAMICS
nspec nnev prefDiss vibRelax itherm chemmod
    0 0 0 4 'Perfect Gas' 1
                 INVISCID FLUXES
imarch
 0
invflxi invflxj invflxk
         2
                2

        rkapi
        rkapj
        rkapk
        sdm2
        sdm4

        0.3333
        0.3333
        0.0000
        0.0000

limi limj limk rk_ven
 2 2 2 1.000
                  VISCOUS FLUXES
isViscous
visflxi visflxj visflxk
 -1 -1 -1
modlmu modlk imodld ivac
2 2 1 2
prl prt scl sct
prl
0.72 0.90 1.00 0.50
ikeps kemin wallfunc igb
                     0
 0 0
             0
               INITIAL CONDITIONS
icond
 2 .
Vel/Mach cx cy cz temp/press turbi tkelref
                     0 109.6 0.01 0.001
   2.9
          1
               0
rho_spec
0.2039
             REFERENCE STATE FOR B.C.'s
icond
 2
Vel/Mach cx cy cz temp/press turbi tkelref
```

```
rho_spec
0.2039
                BLOCK INFO
BLOCK #1: march through zone 1 -- (starting at experimental zb) (1-60)
 imcont nswp ncycle nwres mstage rtolr rtola
   1 1 250 50 1 1.00e-03 1.00e-10
 mgstyle nitfine nitcrct nitsmth smthfac dtfac
   0 1 1 0 3.00e-01 1.00e+00
   SWEEP #1: march through zone 3
   nz iseq npm partStyle iswpdir iplstt iplend
   1 3 1 1 1 1 60
   impl itmstep keslv ichemslv nplane inner mxin
   2 1 1 1 1 0 5
                                                0.01
  dtmin dtmax irelu nremax tolreu
-1.00e+00 -1.00e+00 1 10 1.00e-01
BLOCK #2: march through zone 2 (1-100)
 imcont nswp ncycle nwres mstage rtolr rtola
  1 1 250 50 1 1.00e-03 1.00e-10
 mgstyle nitfine nitcrct nitsmth smthfac dtfac
   0 1 1 0 3.00e-01 1.00e+00
   SWEEP #1: march through zone 4
   nz iseq npm partStyle iswpdir iplstt iplend
   2 3 1 1 1 1 100
   impl itmstep keslv ichemslv nplane inner mxin
                                                tolin
   2 1 1 1 1 0 5
                                                 0.01
  dtmin dtmax irelu nremax tolreu
-1.00e+00 -1.00e+00 1 10 1.00e-01
BLOCK #3: march through zone 3 (1-80)
 imcont nswp ncycle nwres mstage rtolr rtola
   1 1 250 50 1 1.00e-03 1.00e-10
 mgstyle nitfine nitcrct nitsmth smthfac dtfac

0 1 1 0 3.00e-01 1.00e+00

SWEEP #1: march through zone 5
   SWEEP #1: march through zone 5
   nz iseq npm partStyle iswpdir iplstt iplend
   3 3 1 1 1 1 80
   impl itmstep keslv ichemslv nplane inner mxin
                                                 tolin
           1 1 1 1 dtmax irelu nremax tolreu 10 1.00e-01
   2 1 1 1 1 0 5
                                                0.01
   dtmin
  -1.00e+00 -1.00e+00 1 10 1.00e-01
BLOCK #4: march through zone 4
 imcont nswp ncycle nwres mstage rtolr rtola
 1 1 250 50 1 1.00e-03 1.00e-10 mgstyle nitfine nitcrct nitsmth smthfac dtfac
   0 1 1 0 3.00e-01 1.00e+00
   SWEEP #1: march through zone 6
```

2.9 1 0 0 109.6 0.01 0.001

```
nz iseq npm partStyle iswpdir iplstt iplend
   4 3 1 1 1 1 24
                                            tolin
   impl itmstep keslv ichemslv nplane inner mxin
   2 1 1 1 1 0 5 0.01
  dtmin dtmax irelu nremax tolreu
-5.00e-01 -5.00e-01 1 10 1.00e-01
 _____
BLOCK #5: global by fin - Laminar - sequence 3
 imcont nswp ncycle nwres mstage rtolr rtola
 0 8 2000 100 1 1.00e-04 1.00e-10
 mgstyle nitfine nitcrct nitsmth smthfac dtfac
                    0 3.00e-01 1.00e+00
  0. 1 1
   SWEEP #1:
   nz iseq npm partStyle iswpdir iplstt iplend
   10 3 2 1 2 1 96
   impl itmstep keslv ichemslv nplane inner mxin
                                            tolin
 4 1 1 1 1 1 5 0.01

dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
   SWEEP #2:
   nz iseq npm partStyle iswpdir iplstt iplend
   9 3 2 1 2 1 96
   impl itmstep keslv ichemslv nplane inner mxin
  4 1 1 1 1 1 5 0.01
dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
   SWEEP #3:
   nz iseq npm partStyle iswpdir iplstt iplend
   5 3 2 1 2 1 40
   impl itmstep keslv ichemslv nplane inner mxin
                                            tolin
  4 1 1 1 1 1 5 0.01
dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
   SWEEP #4:
   nz iseq npm partStyle iswpdir iplstt iplend
   6 3 2 1 2 1 40
   impl itmstep keslv ichemslv nplane inner mxin
                                             tolin
                                             0.01
   4 1 1 1 1 5
  dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
   SWEEP #5:
   nz iseq npm partStyle iswpdir iplstt iplend
               1 2 1 40
   7 3 2
   impl itmstep keslv ichemslv nplane inner mxin
                                              tolin
   4 1 1 1 1 5
                                              0.01
  dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
   SWEEP #6:
   nz iseq npm partStyle iswpdir iplstt iplend
   8 3 2 1 2 1 40
   impl itmstep keslv ichemslv nplane inner mxin tolin
```

```
4 1 1 1 1 1 1 5 0.01 dtmin dtmax irelu nremax tolreu -1.00e-00 -1.00e-00 0 10 1.00e-01
   SWEEP #7:
   nz iseq npm partStyle iswpdir iplstt iplend
   11 3 2 1 3 1 20
   impl itmstep keslv ichemslv nplane inner mxin tolin
   4 1 1 1 1 1 5 0.01 dtmin dtmax irelu nremax tolreu
 dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
   SWEEP #8:
   nz iseq npm partStyle iswpdir iplstt iplend
   12 3 2 1 3 1 20
   impl itmstep keslv ichemslv nplane inner mxin
                                               tolin
  4 1 1 1 1 1 5 0.01
dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
BLOCK #6: global by fin - Laminar - sequence 2
 imcont nswp ncycle nwres mstage rtolr rtola
   0 8 3000 100 1 1.00e-04 1.00e-10
 mgstyle nitfine nitcrct nitsmth smthfac dtfac
   0 1 1 0 3.00e-01 1.00e+00 SWEEP #1:
   SWEEP #1:
   nz iseq npm partStyle iswpdir iplstt iplend
                1 2 1 96
   10 2 2
   impl itmstep keslv ichemslv nplane inner mxin tolin
  4 1 1 1 1 1 5

dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
                                                0.01
   SWEEP #2:
   nz iseq npm partStyle iswpdir iplstt iplend
                1 2 1 96
   9 2 2
   impl itmstep keslv ichemslv nplane inner mxin
                                               tolin
   4 1 1 1 1 5
                                                0.01
  dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
   SWEEP #3:
   nz iseq npm partStyle iswpdir iplstt iplend
   5 2 2 1 2 1 40
   impl itmstep keslv ichemslv nplane inner mxin
   4 1 1 1 1 5
                                                0.01
  dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
   SWEEP #4:
   nz iseq npm partStyle iswpdir iplstt iplend
   6 2 2 1 2 1 40
   impl itmstep keslv ichemslv nplane inner mxin
                                               tolin
   4 1 1 1 1 5 0.01
  dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
```

```
SWEEP #5:
   nz iseq npm partStyle iswpdir iplstt iplend
                1 2 1 40
   7 2 2
   impl itmstep keslv ichemslv nplane inner mxin
                                             tolin
  4 1 1 1 1 1 5 0.01

dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
   SWEEP #6:
   nz iseq npm partStyle iswpdir iplstt iplend
                1 2 1 40
   8 2 2
   impl itmstep keslv ichemslv nplane inner mxin
                                              tolin
   4 1 1 1 1 5 0.01
  dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
   SWEEP #7:
   nz iseq npm partStyle iswpdir iplstt iplend
   11 2 2 1 3 1 20
                                              tolin
   impl itmstep keslv ichemslv nplane inner mxin
   4 1 1 1 1 5 0.01
  dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
   SWEEP #8:
   nz iseq npm partStyle iswpdir iplstt iplend
   12 2 2 1 3 1 20
   impl itmstep keslv ichemslv nplane inner mxin
                                              tolin
   4 1 1 1 1 5 0.01
  dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
 _____
BLOCK #7: global by fin - Laminar - sequence 1
 imcont nswp ncycle nwres mstage rtolr rtola
 0 8 4000 100 1 1.00e-03 1.00e-10
mgstyle nitfine nitcrct nitsmth smthfac dtfac
0 1 1 0 3.00e-01 1.00e+00
   SWEEP #1:
   nz iseq npm partStyle iswpdir iplstt iplend
   10 1 2 1 2 1 96 impl itmstep keslv ichemslv nplane inner mxin
   4 1 1 1 1 5 0.01
  dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
   SWEEP #2:
   nz iseq npm partStyle iswpdir iplstt iplend
   9 1 2
                1 2 1 96
   impl itmstep keslv ichemslv nplane inner mxin
                                              tolin
   4 1 1 1 1 1 5 0.01
  dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
   SWEEP #3:
   nz iseq npm partStyle iswpdir iplstt iplend
   5 1 2 1 2 1 40
```

```
impl itmstep keslv ichemslv nplane inner mxin tolin 4 1 1 1 1 1 5 0.01
 dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
   SWEEP #4:
   nz iseq npm partStyle iswpdir iplstt iplend
   6 1 2 1 2 1 40
   impl itmstep keslv ichemslv nplane inner mxin
   4 1 1 1 1 5
                                            0.01
 dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
   SWEEP #5:
   nz iseq npm partStyle iswpdir iplstt iplend
   7 1 2 1 2 1 40
   impl itmstep keslv ichemslv nplane inner mxin
   4 1 1 1 1 5
                                            0.01
 dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
   SWEEP #6:
   nz iseq npm partStyle iswpdir iplstt iplend
   8 1 2 1 2 1 40
   impl itmstep keslv ichemslv nplane inner mxin
                                           tolin
 4 1 1 1 1 1 5 0.01
dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
   SWEEP #7:
   nz iseq npm partStyle iswpdir iplstt iplend
   11 1 2 1 3 1 20
   impl itmstep keslv ichemslv nplane inner mxin
   4 1 1 1 1 5 0.01
 dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
   SWEEP #8:
   nz iseq npm partStyle iswpdir iplstt iplend
              1 3 1 20
   12 1 2
   impl itmstep keslv ichemslv nplane inner mxin
                                           tolin
   4 1 1 1 1 5
                                           0.01
 dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
_____
BLOCK #7: global by fin - Turbulent B-L - sequence 1
 imcont nswp ncycle nwres mstage rtolr rtola
   0 8 5000 100 1 1.00e-03 1.00e-10
 mgstyle nitfine nitcrct nitsmth smthfac
                                   dtfac
   0 1 1 0 3.00e-01 1.00e+00
   SWEEP #1:
   impl itmstep keslv ichemslv nplane inner mxin
                                           tolin
   4 1 1 1 1 5 0.01
   dtmin dtmax irelu nremax tolreu
```

```
-1.00e-00 -1.00e-00 0 10 1.00e-01
 SWEEP #2:
 nz iseq npm partStyle iswpdir iplstt iplend
               1 2 1 96
 9 1 3
 impl itmstep keslv ichemslv nplane inner mxin tolin
 4 1 1 1 1 5 0.01
dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
 SWEEP #3:
 nz iseq npm partStyle iswpdir iplstt iplend
5 1 2 1 2 1 40
 impl itmstep keslv ichemslv nplane inner mxin
                                                tolin
 4 1 1 1 1 5
                                                 0.01

        dtmin
        dtmax
        irelu
        nremax
        tolreu

        -1.00e-00
        -1.00e-00
        0
        10
        1.00e-01

 SWEEP #4:
 nziseqnpmpartStyleiswpdiriplsttiplend61212140
 impl itmstep keslv ichemslv nplane inner mxin
4 1 1 1 1 1 5

dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
                                                 0.01
 SWEEP #5:
 impl itmstep keslv ichemslv nplane inner mxin
                                                  tolin
 4 1 1 1 1 5
                                                 0.01
dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
 SWEEP #6:
 impl itmstep keslv ichemslv nplane inner mxin
                                                  tolin
 4 1 1 1 1 5
                                                 0.01
dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
 SWEEP #7:
 nz iseq npm partStyle iswpdir iplstt iplend
 11 1 3 1 3 1 20
 impl itmstep keslv ichemslv nplane inner mxin
                                                  tolin
4 1 1 1 1 1 5

dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
 SWEEP #8:
 nz iseq npm partStyle iswpdir iplstt iplend
 12 1 3 1 3 1 20
 impl itmstep keslv ichemslv nplane inner mxin
4 1 1 1 1 1 5
dtmin dtmax irelu nremax tolreu
-1.00e-00 -1.00e-00 0 10 1.00e-01
                                                 0.01
```

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Vita

Carl Patrick Tilmann was born in Detroit, Michigan on March 30, 1964, the son of school teachers Robert C. Tilmann and Marilyn C. Tilmann. During his primary school

years, the family settled in the small township of Galien, Michigan, where he attended

through High School.

Carl's college education began at Ferris State University in Big Rapids, Michigan,

where he earned an Associate in Science degree, and decided that Engineering was his

calling. With this in mind, he transferred to Tri-State University in Angola, Indiana,

where he received a Bachelor of Science in Aerospace Engineering with High Honors. As

an undergraduate, he was active in the cooperative education program with the Air Force

at Wright-Patterson AFB. At the beginning of his last year at Tri-State, Carl persuaded

his sweetheart Christine to marry him - convincing her that he had only one more year of

college to complete. However, he was offered a research assistantship at the George Wash-

ington University/NASA Langley Joint Institute for the Advancement of Flight Sciences,

and Christine reluctantly agreed to move to Virginia. Upon completion of his graduate

research at NASA Langley, Carl accepted a position at the Wright Laboratory's Flight

Mechanics Division. After taking a few part-time classes at AFIT, Carl was selected to

participate in the Wright Laboratory/AFIT Work-Study Program, enabling him to pur-

sue a PhD. After his first year of full time study, Carl was selected to receive a tuition

scholarship from the Dayton Area Graduate Studies Institute (DAGSI) for the remainder

of his prgram at AFIT.

During Carl's time at AFIT, Christine and he have been blessed with two children.

Samuel Patrick was born on Carl's first day of full-time study, and George Carl was born

21 months later. Carl continues to serve as a research engineer at Wright Laboratory in

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